

# The Morphology of Complex Materials: MTEN 657 MWF 3:00-3:50 Baldwin 64 I Prof. Greg Beaucage

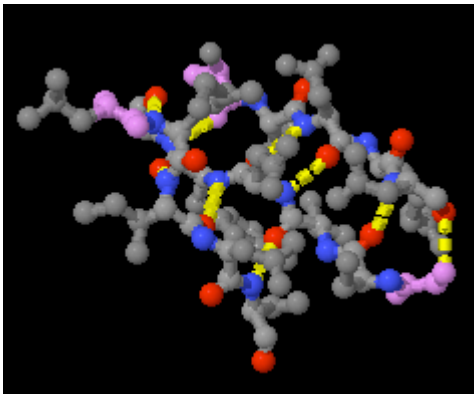
Course Requirements:

- Weekly Quiz (8 to 9 in quarter)
- Comprehensive Final (worth 3 quizzes)

-Old Quizzes will serve as homework  
(These have posted answers)

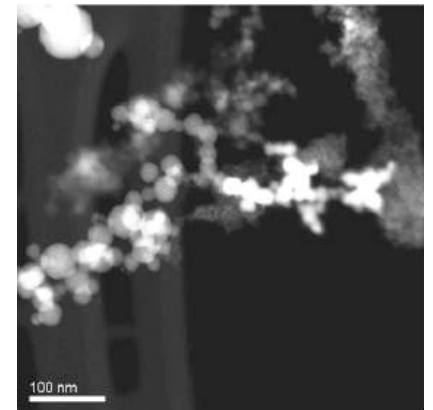
I may also assign other homework where it  
is needed

You can replace quiz grades with a (or  
several) report(s) on a topical area not  
covered in class but pertaining to the  
hierarchy of morphology for a complex  
material. Several examples are given on the  
web page.



$\beta$ -Sheet

[webhost.bridgew.edu/fgonga/proteins/beta.htm](http://webhost.bridgew.edu/fgonga/proteins/beta.htm)



Aggregated Nanoparticles  
from Lead Based Paint

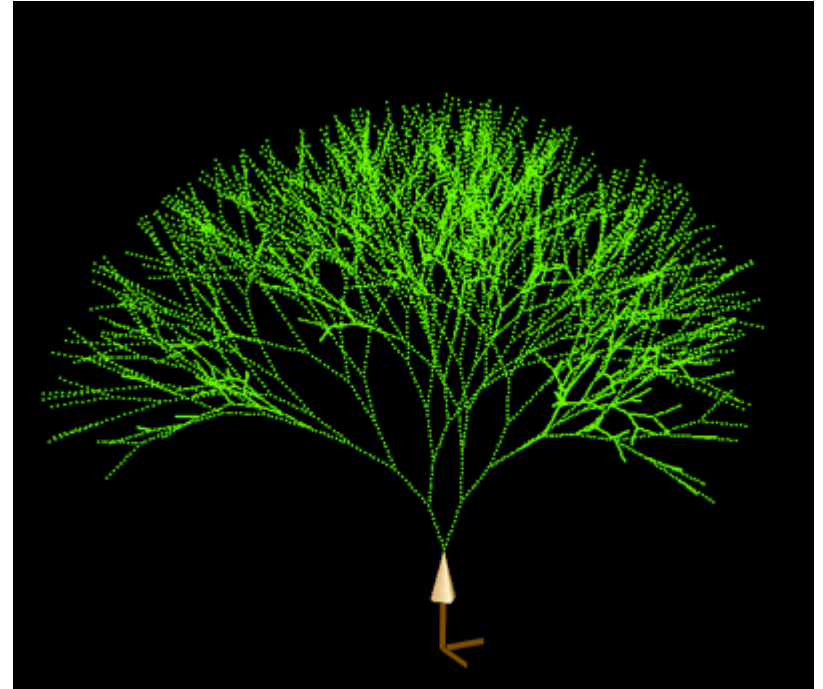
"Emerging Issues in Nanoparticle  
Aerosol Science and Technology (NAST)"  
NSF 2003

# Structural Hierarchy of Complex Materials



Consider that we would like to understand a forest, such as the Amazon Forest from a Structural Perspective in order to develop predictive capabilities and an understanding of the basic features to such a complex structure.

# Structural Hierarchy of Complex Materials



<http://www.eng.uc.edu/~gbeaucag/Classes/MorphologyofComplexMaterials/Overview.html>

Consider that we would like to understand a forest, such as the Amazon Forest from a Structural Perspective in order to develop predictive capabilities and an understanding of the basic features to such a complex structure.

- 1) The first logical step is to consider a base (primary) unit for the forest and
- 2) then devise a repetition or branching rule (fractal scaling law) to create trees (secondary structure).

We revise the scaling rules and primary unit until we produce the type of trees we are interested in.

# Structural Hierarchy of Complex Materials



<http://www.eng.uc.edu/~gbeaucag/Classes/MorphologyofComplexMaterials/Overview.html>

Consider that we would like to understand a forest, such as the Amazon Forest from a Structural Perspective in order to develop predictive capabilities and an understanding of the basic features to such a complex structure.

We could consider other types of trees in the same way.

3) Trees form clusters or groves (tertiary structure) that can follow a spacing and shape rule, for instance, redwoods grow in “fairy” rings or “cathedral” groups around an old tree.

# Structural Hierarchy of Complex Materials



Consider that we would like to understand a forest, such as the Amazon Forest from a Structural Perspective in order to develop predictive capabilities and an understanding of the basic features to such a complex structure.

- 4) Groupings of groves of trees interact with the environment to form forests (quaternary structures)
- 5) Higher levels of organization can be considered

# Structural Hierarchy of Complex Materials

-We have considered discrete “levels” of structure within a hierarchical model.

-In constructing the hierarchy is it natural to start from the smallest scale and to build up.

-We have borrowed from proteins in labeling the hierarchical levels primary, secondary, tertiary and quaternary.

-The hierarchical approach gives insight into how complex natural systems can be understood as if the structural levels acted independently in some respects.

-One of the main insights from hierarchical models is to understand in detail how and why structural levels are not independent and how they can interact to accommodate the environment.

-In this course we will consider the application of hierarchical models to understand complex molecular systems with the goal of understanding how the hierarchical approach can be expanded.

# Structural Hierarchy of Complex Materials

Topics we will cover:

- 1) Protein structure (the origin of the hierarchical concept) 3 weeks
- 2) DNA and RNA structure (first adaptation of the hierarchical approach)  
1 week
- 3) Polymer Chain Structure in Solution (a statistical hierarchy) 2 weeks
- 4) Hierarchy of Polymer Dynamics in Solution (a kinetic hierarchy) 1 week
- 5) Polymer Crystalline Structure (hierarchy in a structural material) 2 weeks
- 6) Branched Fractal Aggregates (hierarchy in a statistical structural material)  
1 week

# Structural Hierarchy of Complex Materials

Structural Hierarchy					
Order/Level	Forest	Protein	Polymer Statics	Polymer Dynamics	Fractal Aggregates
Primary	Twig	Amino Acid Sequence	Persistence Length	Kuhn Unit	Primary Particles
Secondary	Tree/Branching	$\alpha$ -Helix; $\beta$ -Sheet; Turns	Blob	Rouse Unit	Scaling Transitions
Tertiary	Grove/Cluster	Globular Structure	Coil	Coil	Aggregate
Quaternary	Forest	Complex Structure with many Proteins/ Metal Ions Etc.	Network/ Entanglements	Entanglements	Agglomerate



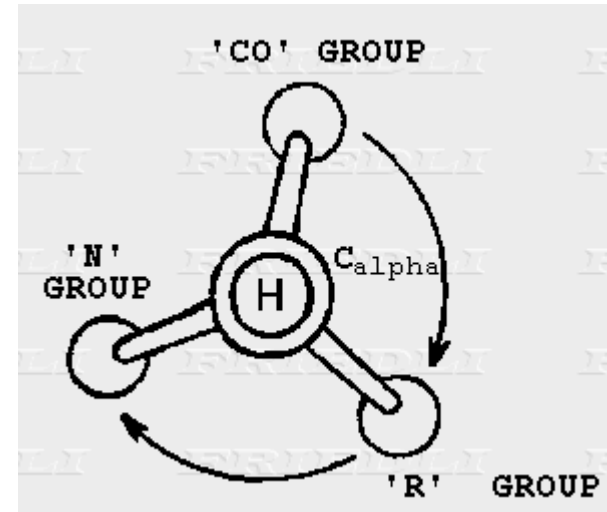
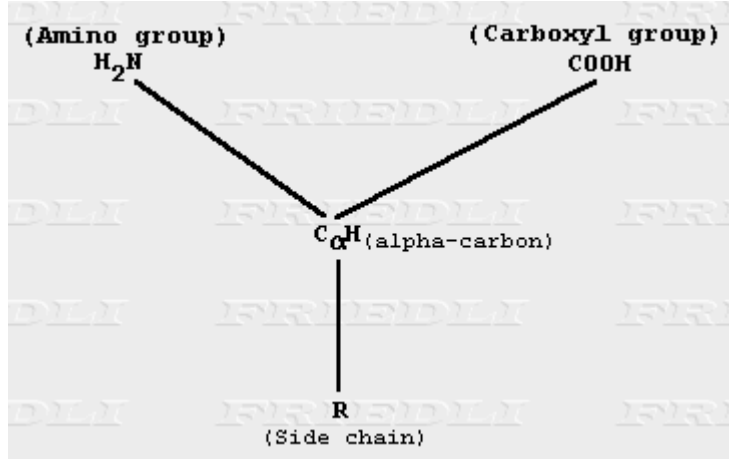
# **The Structural Hierarchy of Proteins**

## Size of proteins.html

<http://learn.genetics.utah.edu/content/begin/cells/scale/>

## Four Levels of Protein Structure.html

<http://www.youtube.com/watch?v=y8Z48RoRxHg&feature=related>



[http://www.friedli.com/herbs/phytochem/proteins.html#peptide\\_bond](http://www.friedli.com/herbs/phytochem/proteins.html#peptide_bond)

The  $\alpha$ -carbon is a chiral center  
it is always in an L-configuration spelling “CORN” in the Newman projection

There are 20 choices for the “R” group in nature. This makes an alphabet from which sequences of these 20 letters can code for any protein. Depending on the chemical functionality of the “R” groups different properties, polarity, hydrophobicity, ability to bond by disulfide linkages, hydrogen bonding and chain flexibility or rigidity can be imparted to the protein.

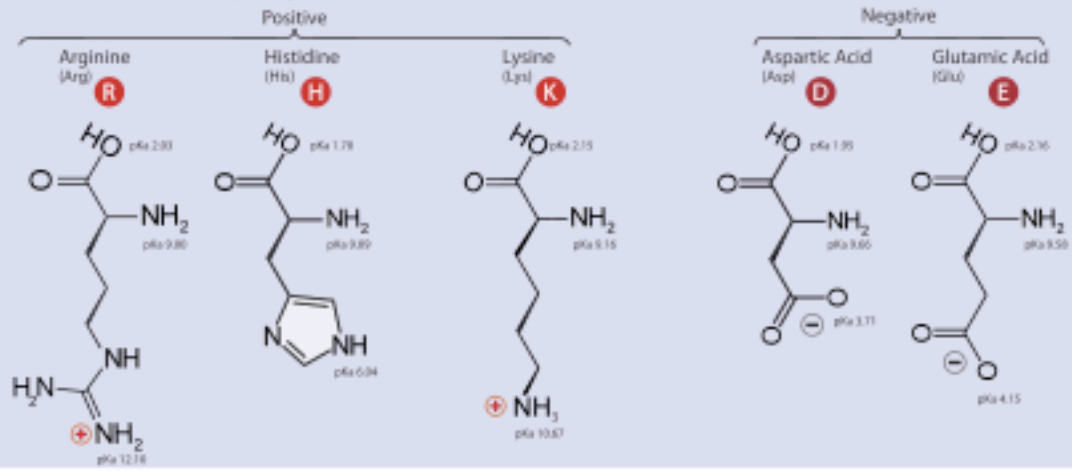
[Quick Look at Amino Acids.html](http://www.johnkyrk.com/aminoacid.html)

<http://www.johnkyrk.com/aminoacid.html>

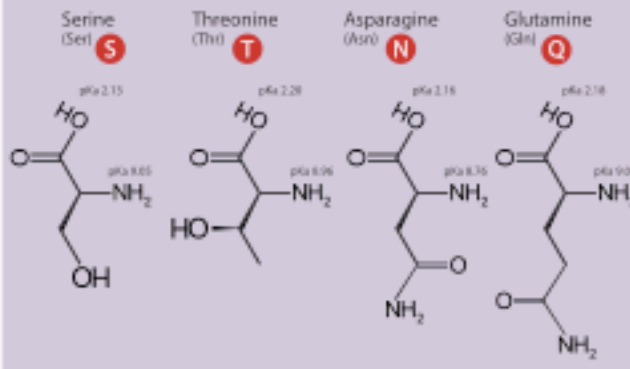
## Twenty-One Amino Acids

⊕ Positive ⊖ Negative  
 • Side chain charge at physiological pH 7.4

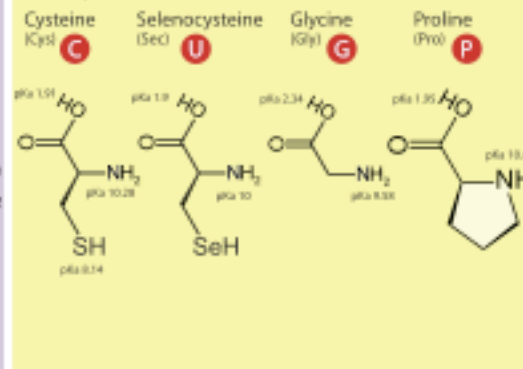
### A. Amino Acids with Electrically Charged Side Chains



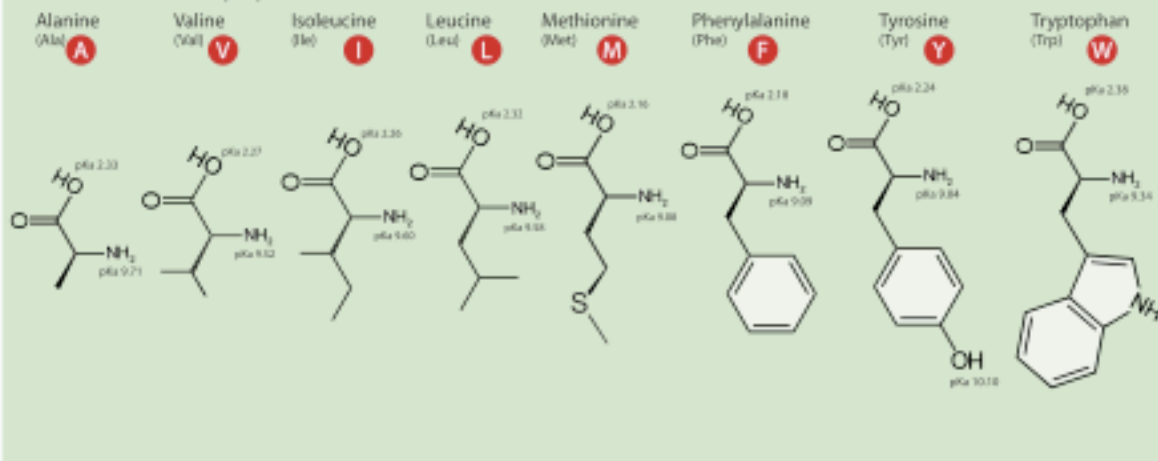
### B. Amino Acids with Polar Uncharged Side Chains



### C. Special Cases



### D. Amino Acids with Hydrophobic Side Chain



pKa Data: CRC Handbook of Chemistry, v. 2013

Dan Cojocari, Department of Medical Biophysics, University of Toronto, 2011

## Amino Acids.html

<http://www.bioscience.org/urlists/aminacid.htm>

## 3D Amino Acids

<http://www.mcb.ucdavis.edu/courses/bis102/Polar.html>

## More Amino Acids

<http://biology.clc.uc.edu/courses/bio104/protein.htm>

## Know These 5 Amino Acids Well

Methionine Start Amino Acid (usually removed in later steps)

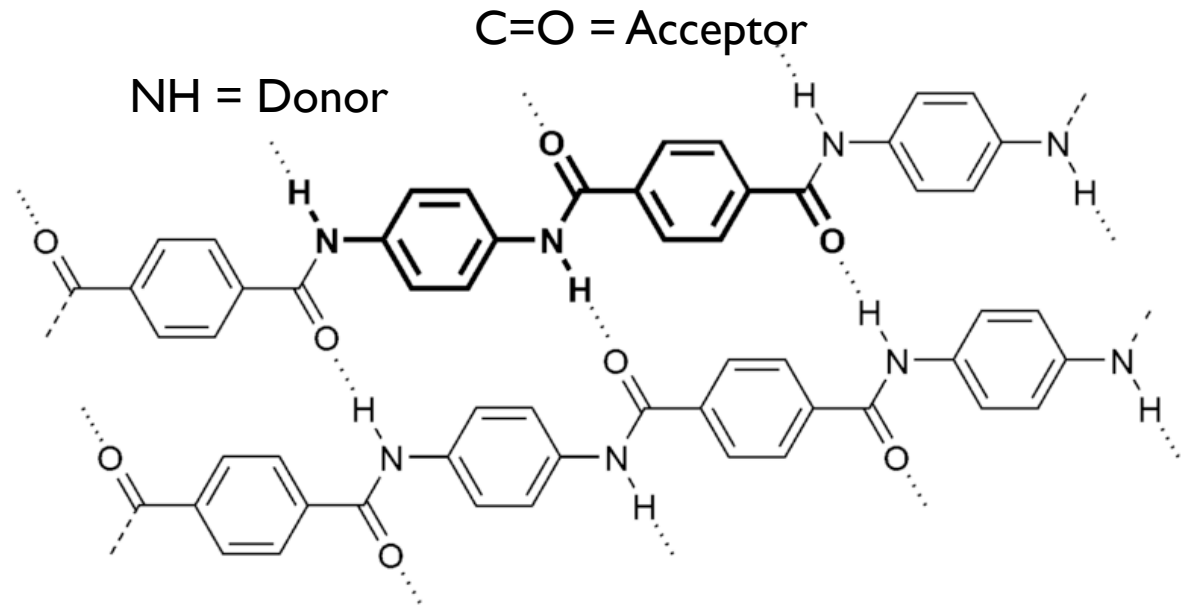
Glycine -H Flexible non-polar

Alanine -CH<sub>3</sub> Flexible non-polar

Proline 10-40% Cis Configuration depending on neighboring amino acid residues  
Found in Turns and at start of  $\alpha$ -helix

Cystine Disulfide Linkages (Hair is 5% cystine)

Hydrogen Bonding in Kevlar



Polyamides are similar to proteins

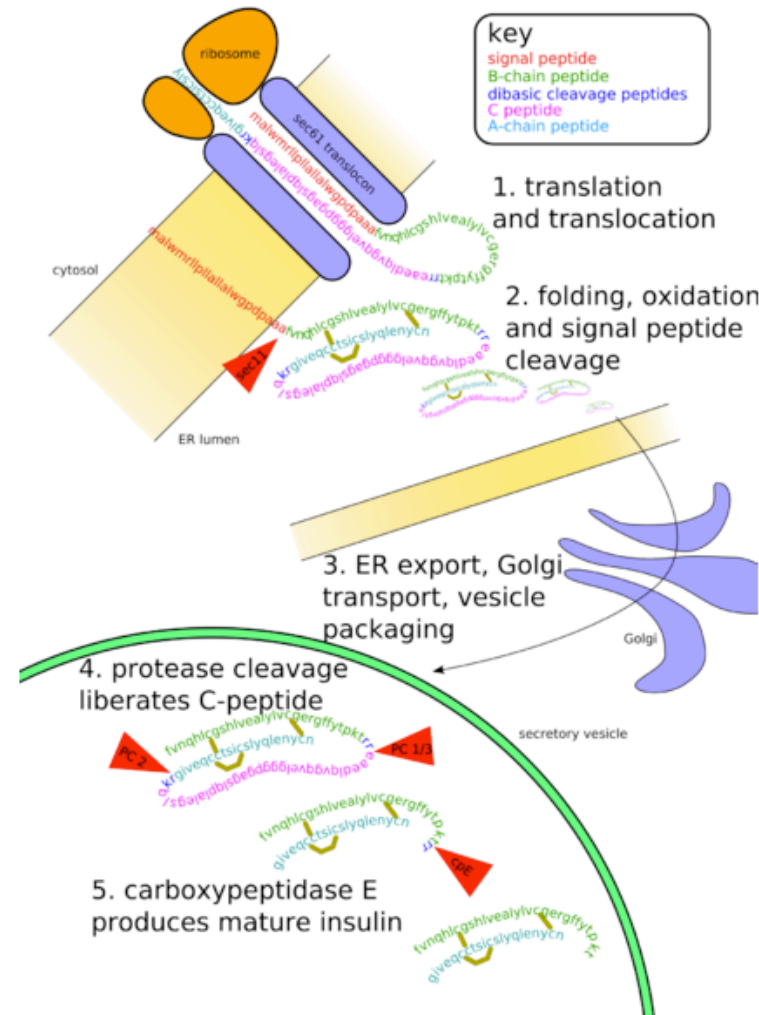
# The Genetic Code Links.html

<http://www.eng.uc.edu/~gbeauca/Classes/MorphologyofComplexMaterials/GeneticCode.html>

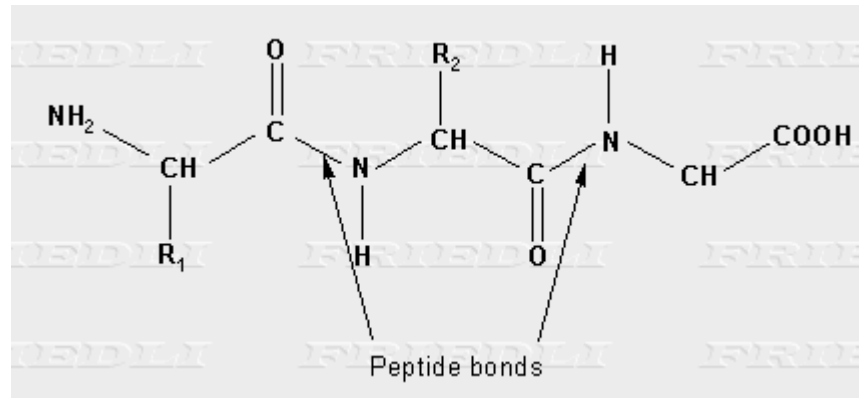
## Movie of Protein Synthesis

<http://nutrition.jbpub.com/resources/animations.cfm?id=14&debug=0>

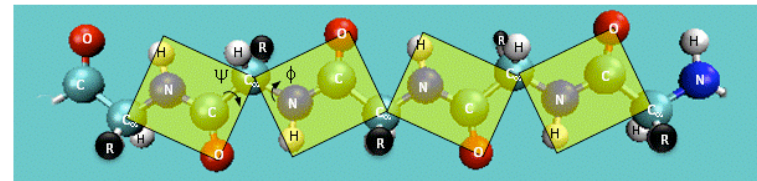
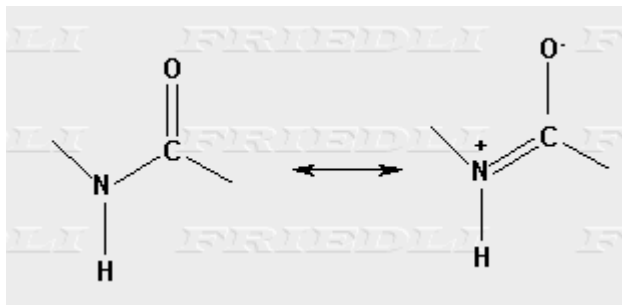
### Post Translational Modification of Insulin



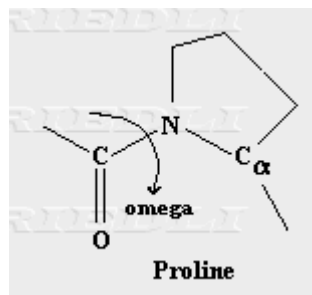
# The Peptide Bond



[http://www.friedli.com/herbs/phytochem/proteins.html#peptide\\_bond](http://www.friedli.com/herbs/phytochem/proteins.html#peptide_bond)



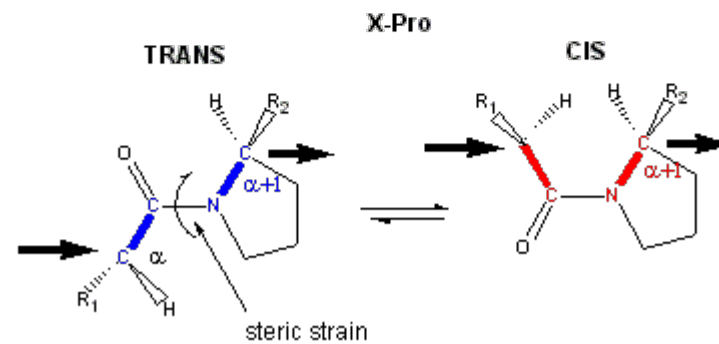
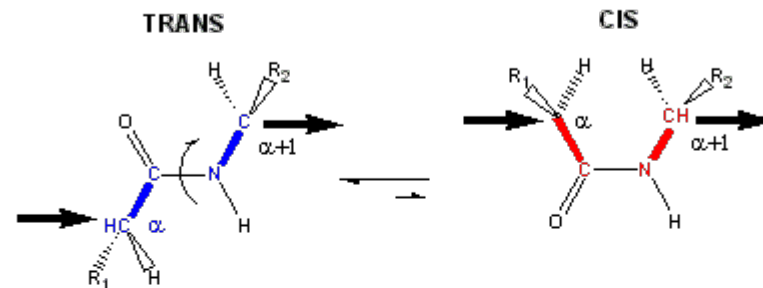
Resonance structures make the peptide group planar (like a card).



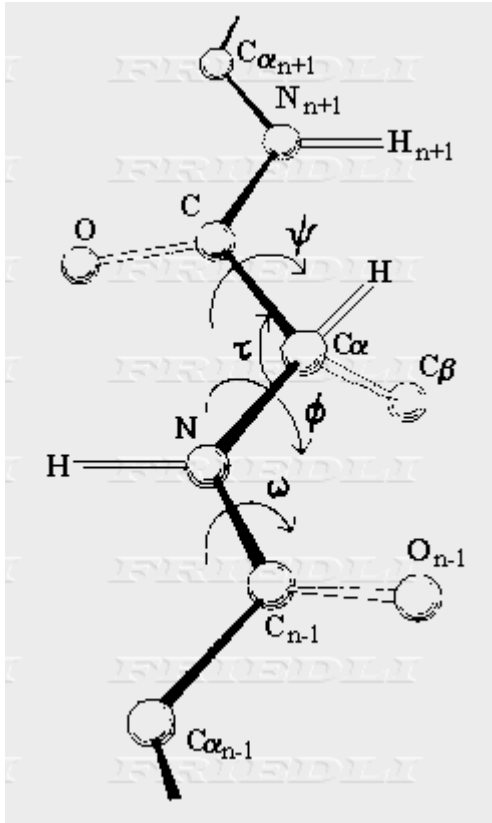
Proline is the exception  
Proline adds main chain curvature  
found in turns and at start of  $\alpha$ -helix

**PEPTIDE BONDS: CIS OR TRANS**

X-Y







The peptide linkage forms a planar structure with the two  $\alpha$ -carbons and the N, H, C and O atoms

PSI  $\psi$  is the rotation angle between the carboxyl C and the  $\alpha$ -carbon

PHI  $\phi$  is the rotation angle between N and the  $\alpha$ -carbon

Certain values of these two rotation angles are preferred in certain structures

So the angles serve as a map for the protein secondary structure

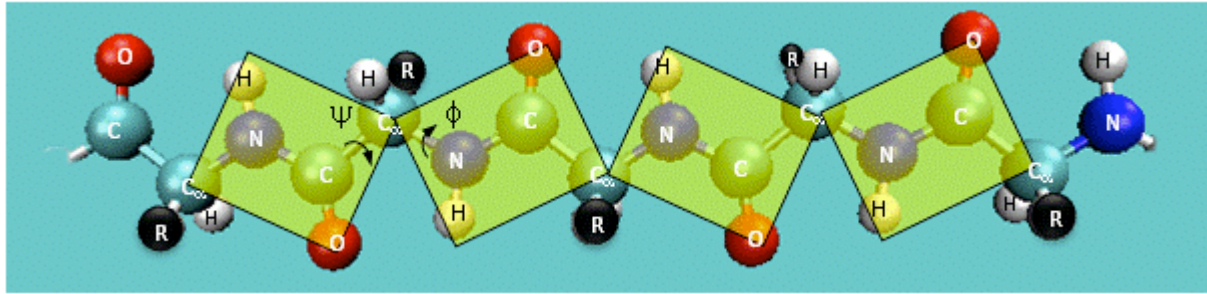
Fully Extended Chain (Planar Zig-Zag)

Phi/Psi 180, 180

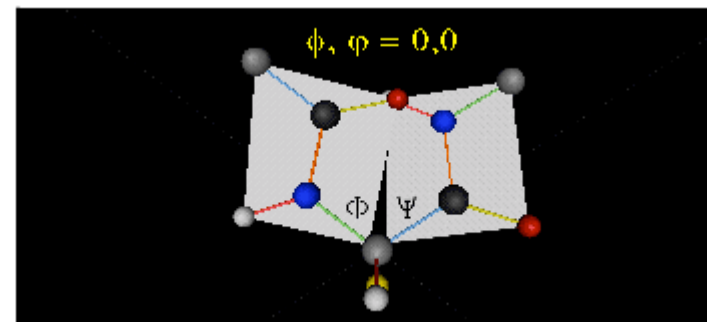
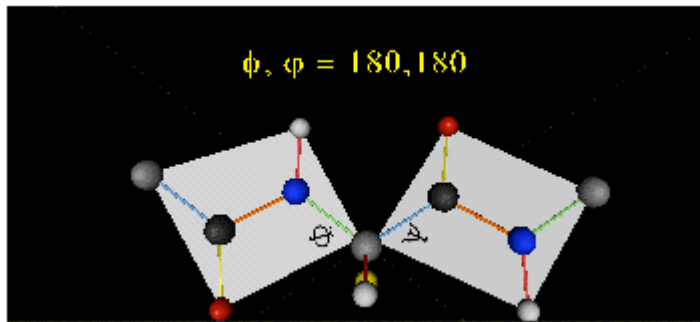
Parameters of regular secondary structures.  $n$  is the number of residues per helical turn,  $p$  is the helical pitch, and  $A$  is the atoms in H-bonded loop.

Structure	$\phi$	$\psi$	$n$	$p(\text{\AA})$	$A$	H-bond(CO,HN)
Right-handed alpha helix[3.6 <sub>13</sub> helix]	-57	-47	3.6	5.4	13	i,i+2
3 <sub>10</sub> -helix	-74	-4	3.0	6.0	10	i,i+3
pi-helix	-57	-70	4.4	5.0	16	i,i+4
Parallel beta strand	-119	113	2.0	6.4		
Antiparallel beta strand	-139	135	2.0	6.8		

[http://www.friedli.com/herbs/phytochem/proteins.html#peptide\\_bond](http://www.friedli.com/herbs/phytochem/proteins.html#peptide_bond)



<http://employees.csbsju.edu/hjakubowski/classes/ch331/protstructure/olunderstandconfo.html>



<http://visu.uwlax.edu/BioChem/Rotate.mov>

Phi rotation for Psi = 0

Psi rotation for Phi = 0

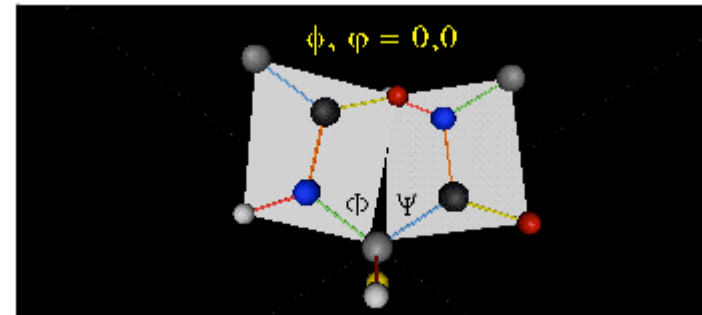
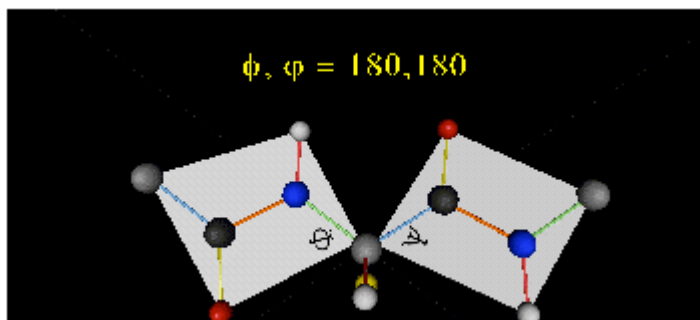


Figure: Ramachandran plot

The Ramachandran Plot.

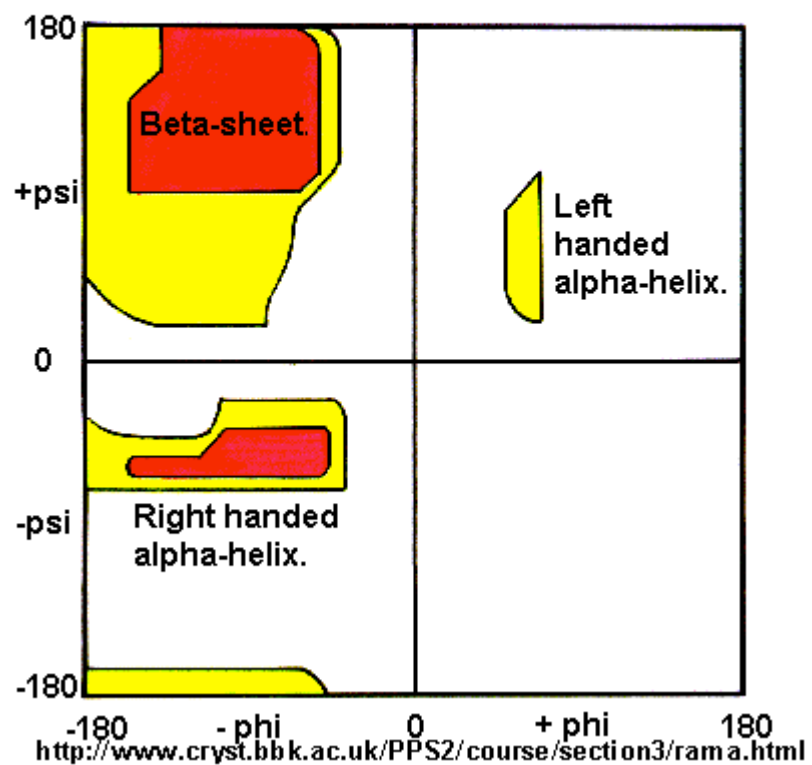
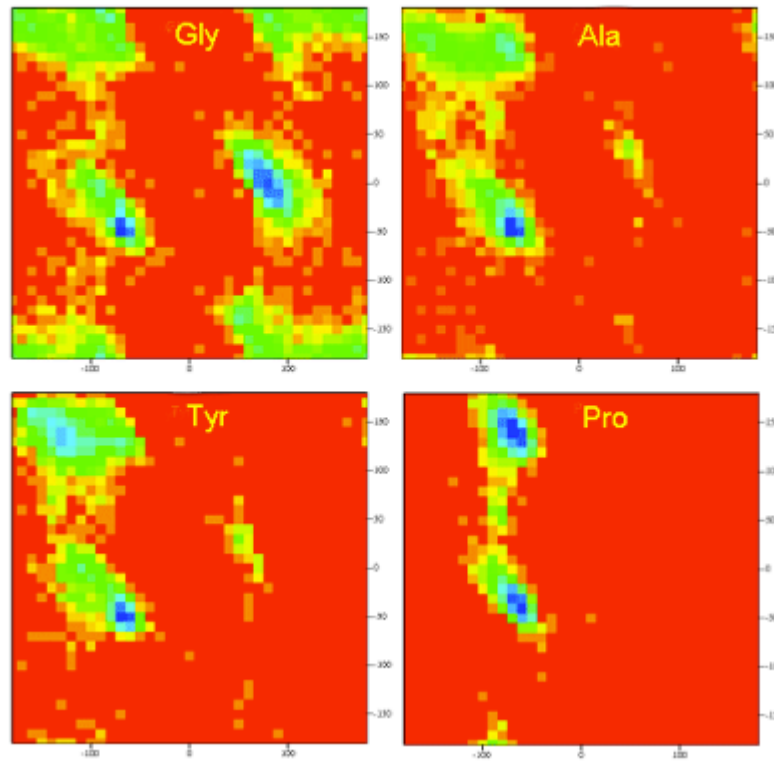


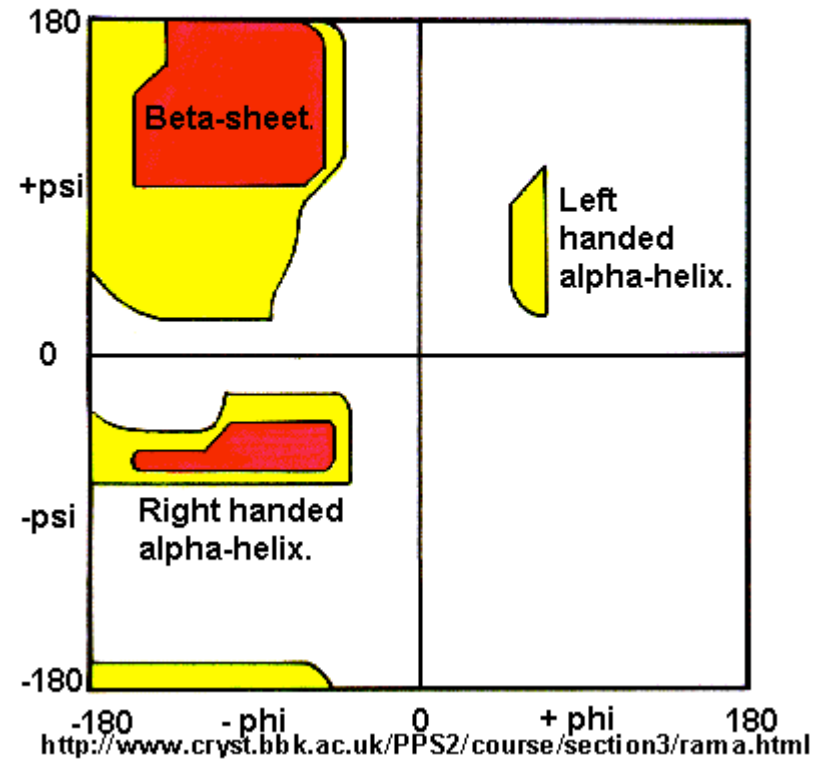
Figure: Ramachandran plots showing  $\phi/\psi$  angles for Gly, Ala, Tyr, and Pro in actual proteins



[Ramachandran Plots.html](#)

Figure: Ramachandran plot

The Ramachandran Plot.



# Lets Jump Ahead and Look at Protein Folding

## Folding Simple Dynamic Simulation.html

<http://intro.bio.umb.edu/111-112/111F98Lect/folding.html>

## More Complicated Simulation.html

<http://www.cs.ucl.ac.uk/staff/D.Jones/t42morph.html>

## Yet more complicated.html

<http://www.youtube.com/watch?v=meNEUTn9Atg>

## Small Protein Folding.html

[http://www.youtube.com/watch?v=\\_xF96sNWnK4&feature=related](http://www.youtube.com/watch?v=_xF96sNWnK4&feature=related)

## Another Small Protein Folding.html

<http://www.youtube.com/watch?v=E0TX3yMEZ8Y&feature=related>

## Where and When do Proteins Fold.html

<http://www.youtube.com/watch?v=BrUdCVwgJxc&feature=related>

## Entropy and Protein Folding.html

<http://www.youtube.com/watch?v=gaaiepNVyvE&feature=related>

## Folding a Protein by Hand.html

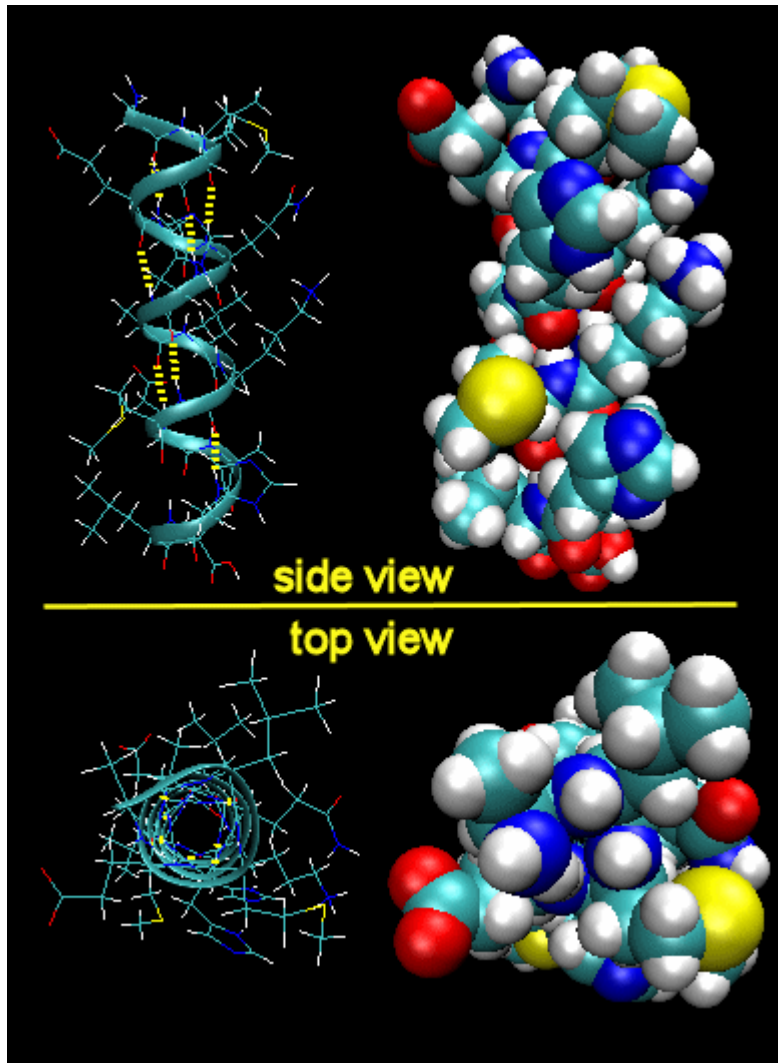
<http://www.youtube.com/watch?v=va92d9EiIQM&feature=related>

## Folding of Villin.html

<http://www.youtube.com/watch?v=leSwDKZQpok&feature=related>

**Secondary Structures of Proteins**  
 **$\alpha$ -Helix,  $\beta$ -Sheets, Turns**

## Right Handed $\alpha$ -Helix



pdb of  $\alpha$ -Helix

[http://employees.csbsju.edu/hjakubowski/Jmol/alpha\\_helix/alpha\\_helix.htm](http://employees.csbsju.edu/hjakubowski/Jmol/alpha_helix/alpha_helix.htm)

C=O from residue "i"  
hydrogen bonds with  
NH from residue "i+4"

Phi/Psi angles are -57, -47

Residues per turn = 3.6  
Rise per turn = 5.4 Å

### Amino Acids and Helix

Glycine too flexible

Proline too rigid

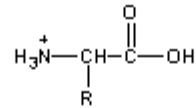
Short H-Bonding (Ser, Asp, Asn) Disrupt Coil

Long H-Bonding are OK

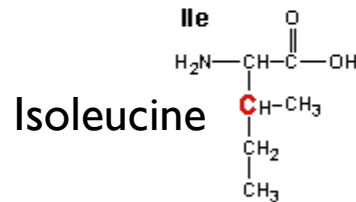
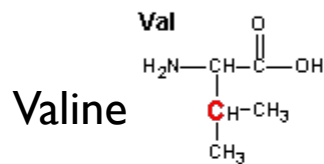
Branches at  $\alpha$ -C Disrupt Coil (Val, Ile)

<http://employees.csbsju.edu/hjakubowski/classes/ch331/protstructure/olunderstandconfo.html>

## AMINO ACID PROPENSITIES FOR SECONDARY STRUCTURE



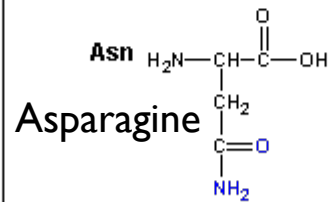
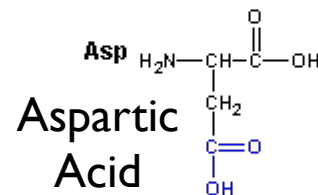
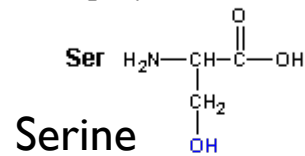
Branched at  $\text{C}_\beta$



Branch at  $\text{C}_\beta$   
**destablizes  $\alpha$  helix**

**OK in  $\beta$  Sheet**  
side chain projects  
out of plan of main  
chain

No branch at  $\text{C}_\beta$  and  
R group can form H bonds

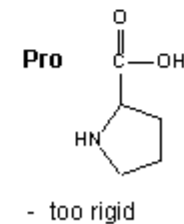
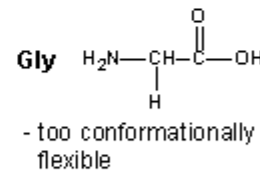


**destablizes  $\alpha$  helix**  
H Bond donor/acceptors  
compete with main chain

No branch at  $\text{C}_\beta$  and R  
group can't form H bonds

**OK in  $\alpha$  Sheet**  
side chain projects  
out of

Exceptions:

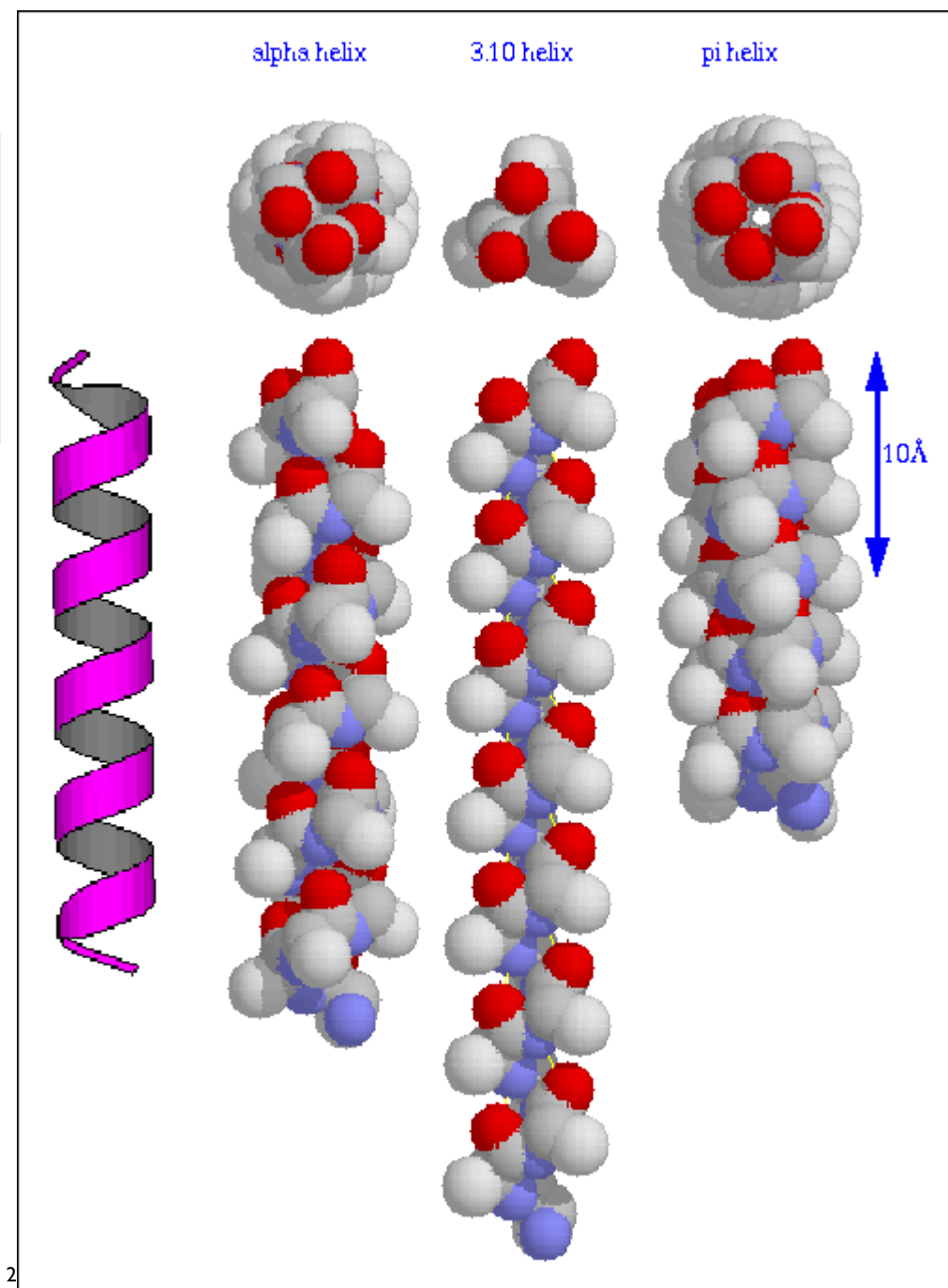
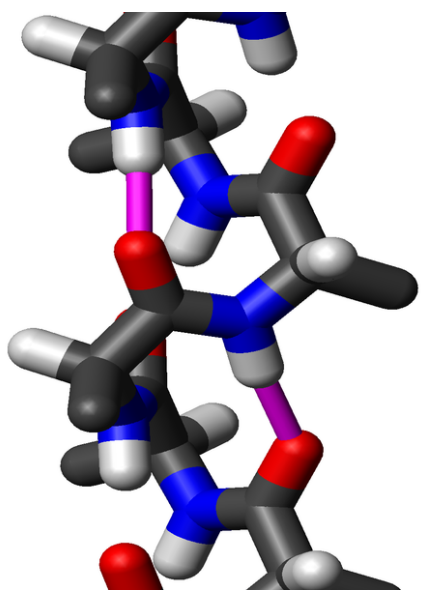




## Other Types of Helices

Helix Type	H bond btw $i^{\text{th}}$ and $i^{\text{th}}+X$ AA, where X =	Residue/turn	Rise (Angstrom)/turn
$3_{10}$	3	3	6
a	4	3.6	5.4
p	5	4.3	4.7

$3_{10}$  helix

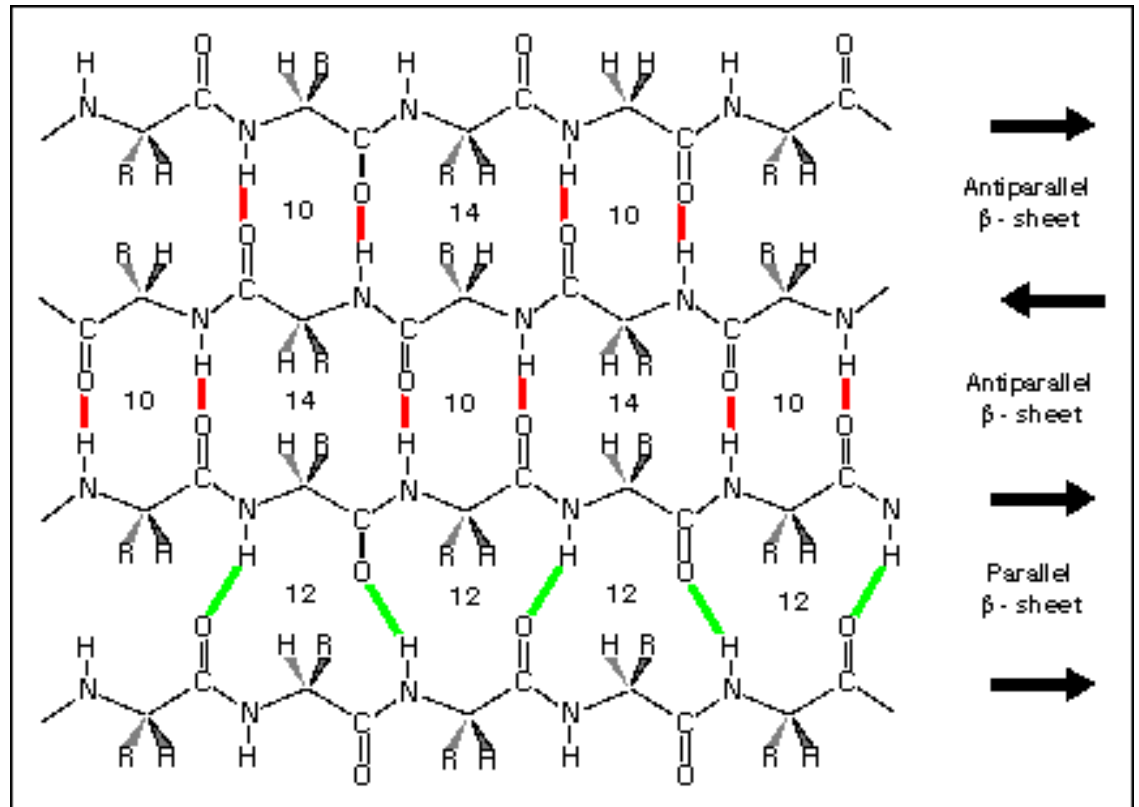


## $\beta$ -Sheets

	Phi	Psi
Parallel	-119	+113
Anti-Parallel	-139	+135
$\alpha$ -Helix	-57	-47
Extended	$\pm 180$	$\pm 180$

### Rippled Sheets

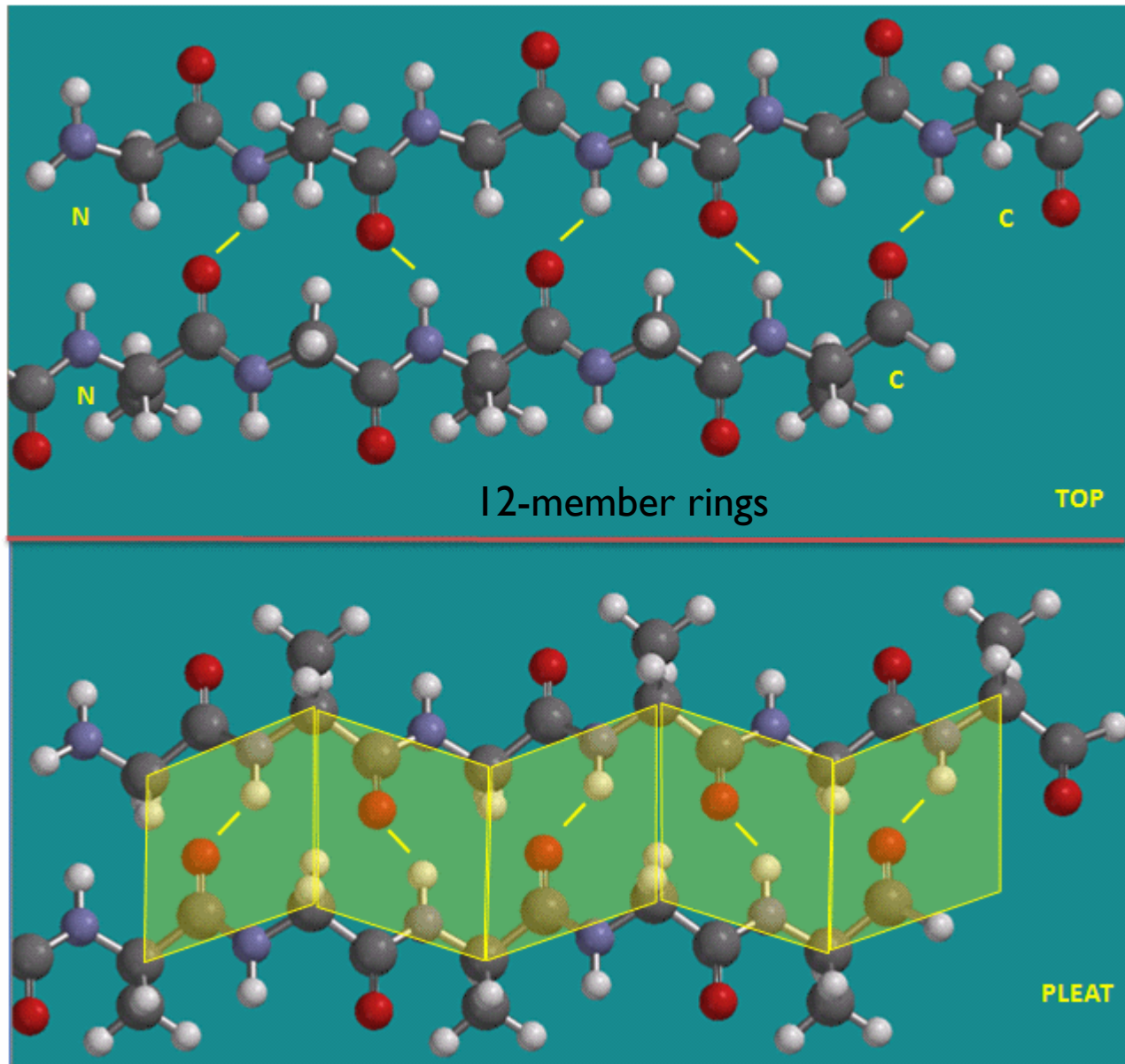
H-Bonding between strands in Sheet  
 H-Bonding within strand in Helix



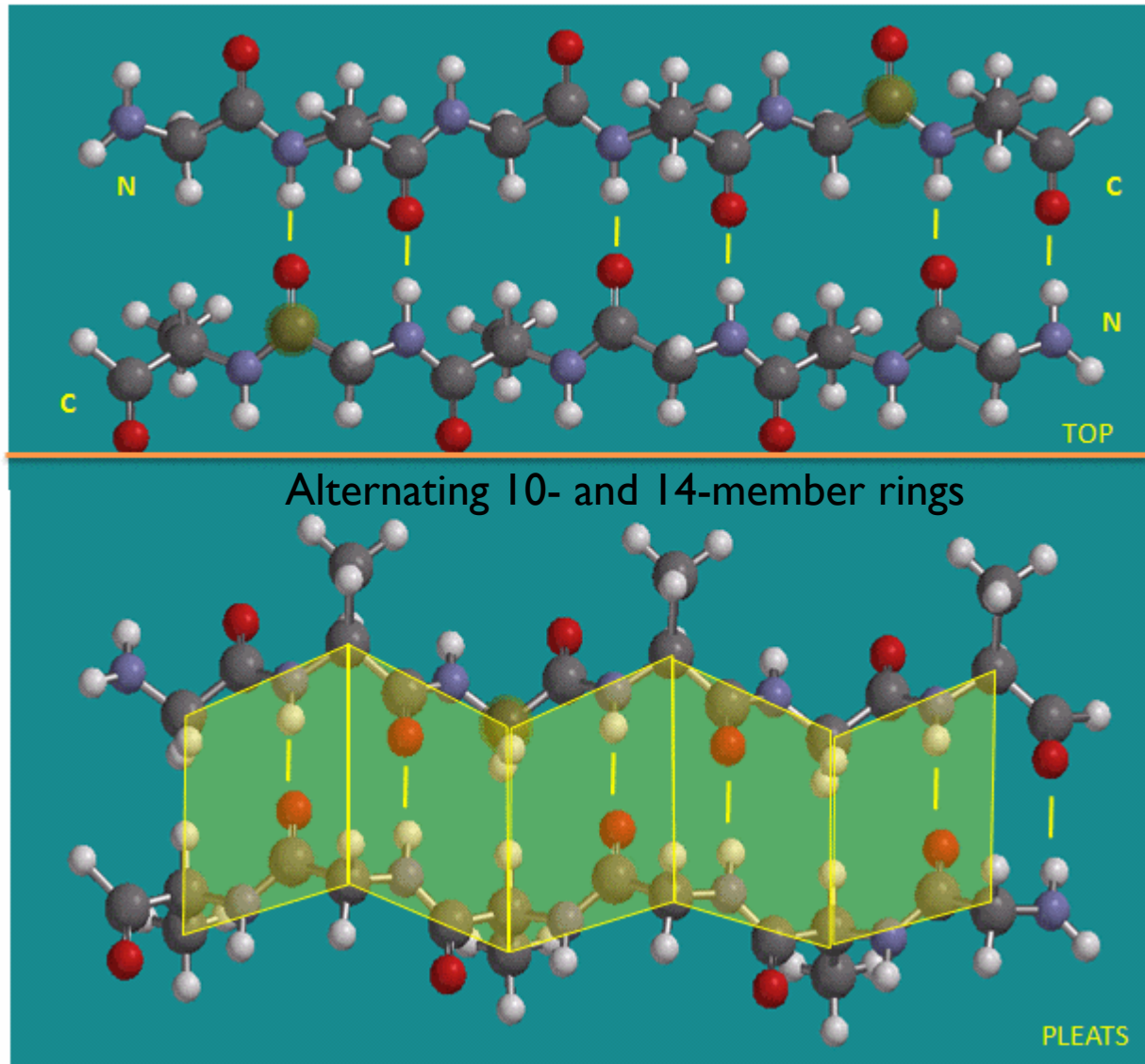
Parallel => 12 member rings

Anti-Parallel => 14 and 10 member rings alternating

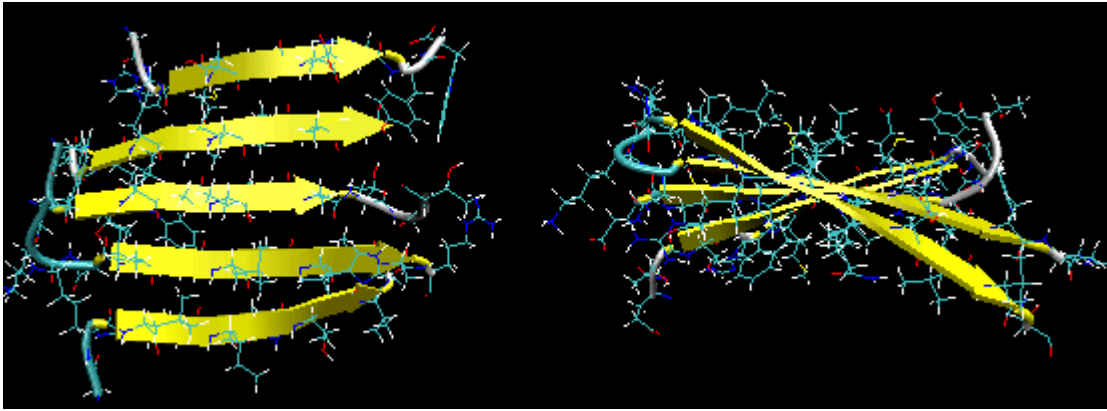
# Parallel $\beta$ -Sheets



## Anti-Parallel $\beta$ -Sheets



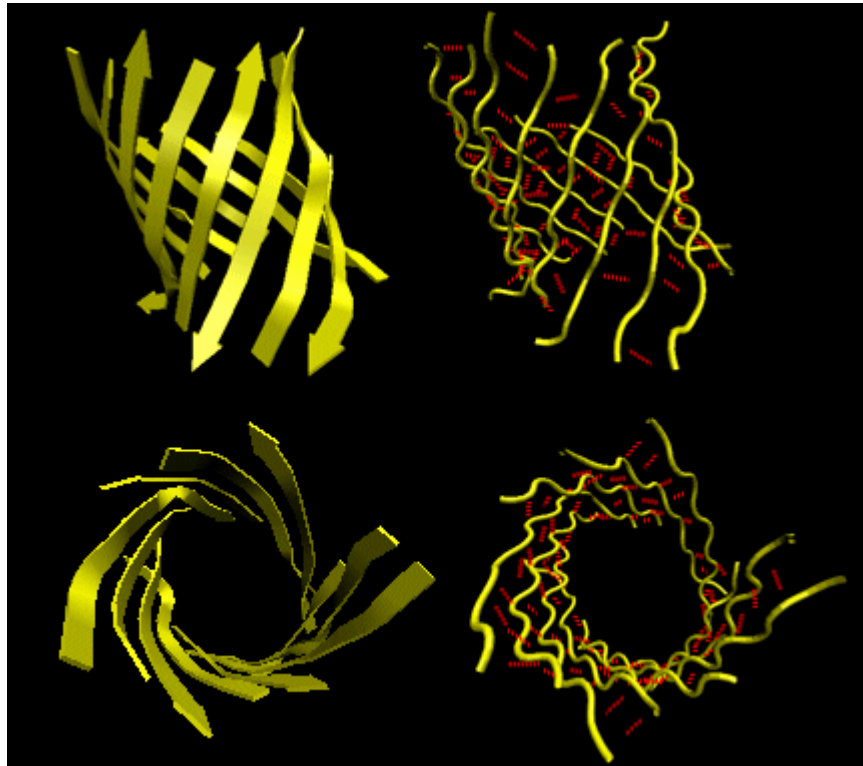
## Twisted $\beta$ -Sheet/Saddle



## Twisted $\beta$ -Saddle

[http://employees.csbsju.edu/hjakubowski/Jmol/Twisted%20Beta%20Sheet/Twisted\\_Beta\\_Sheet.htm](http://employees.csbsju.edu/hjakubowski/Jmol/Twisted%20Beta%20Sheet/Twisted_Beta_Sheet.htm)

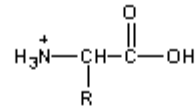
## $\beta$ -Barrel



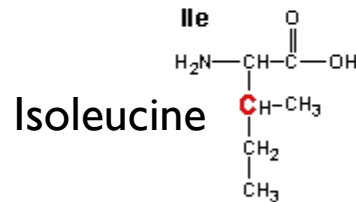
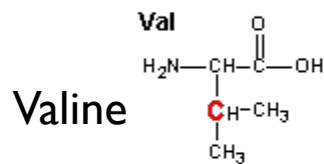
## $\beta$ -Barrel

[http://employees.csbsju.edu/hjakubowski/Jmol/beta\\_barrel\\_tpi/Beta\\_Barrel\\_tpi.htm](http://employees.csbsju.edu/hjakubowski/Jmol/beta_barrel_tpi/Beta_Barrel_tpi.htm)

## AMINO ACID PROPENSITIES FOR SECONDARY STRUCTURE



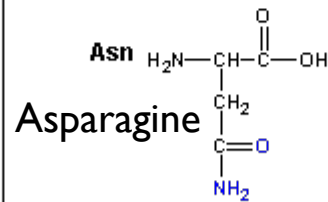
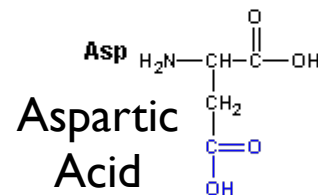
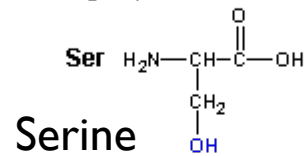
Branched at  $\text{C}_\beta$



Branch at  $\text{C}_\beta$   
**destablizes  $\alpha$  helix**

**OK in  $\beta$  Sheet**  
side chain projects  
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No branch at  $\text{C}_\beta$  and  
R group can form H bonds

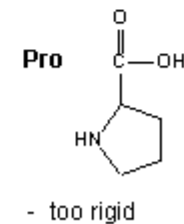
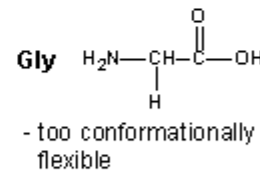


**destablizes  $\alpha$  helix**  
H Bond donor/acceptors  
compete with main chain

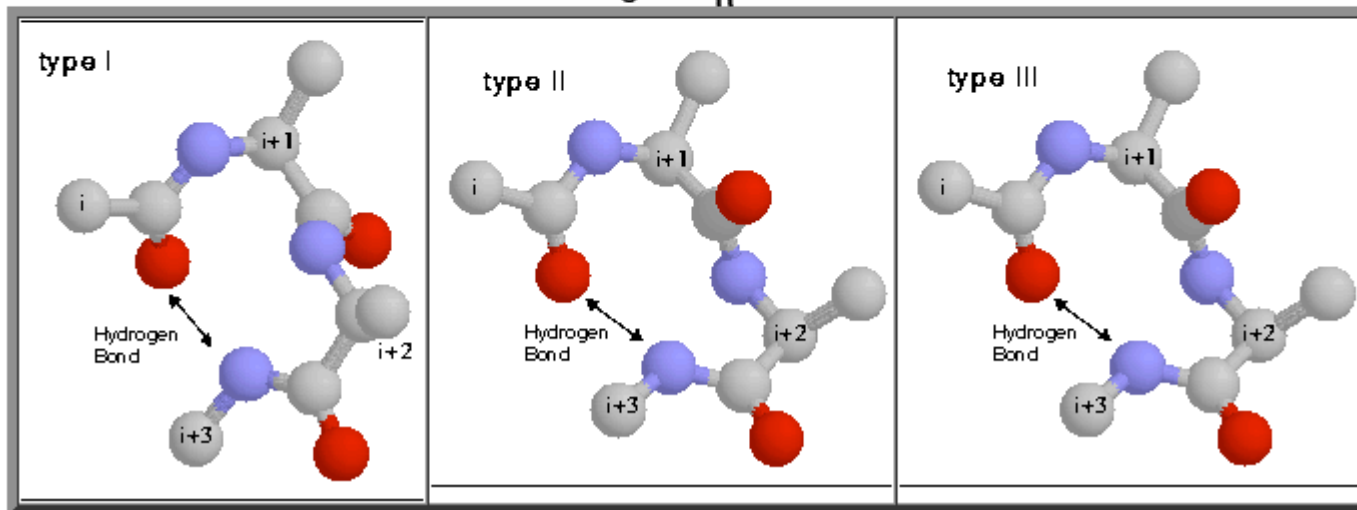
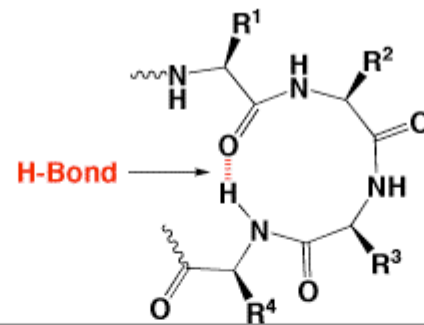
No branch at  $\text{C}_\beta$  and R  
group can't form H bonds

**OK in  $\alpha$  Sheet**  
side chain projects  
out of

Exceptions:



# $\beta$ -Turns

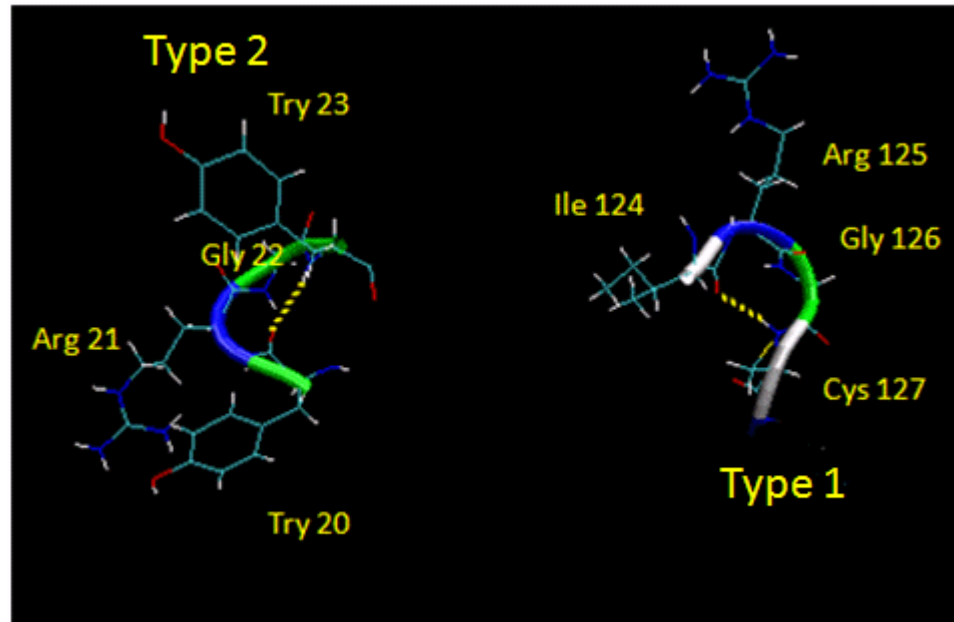


# $\beta$ -Turns

## Reverse Turn

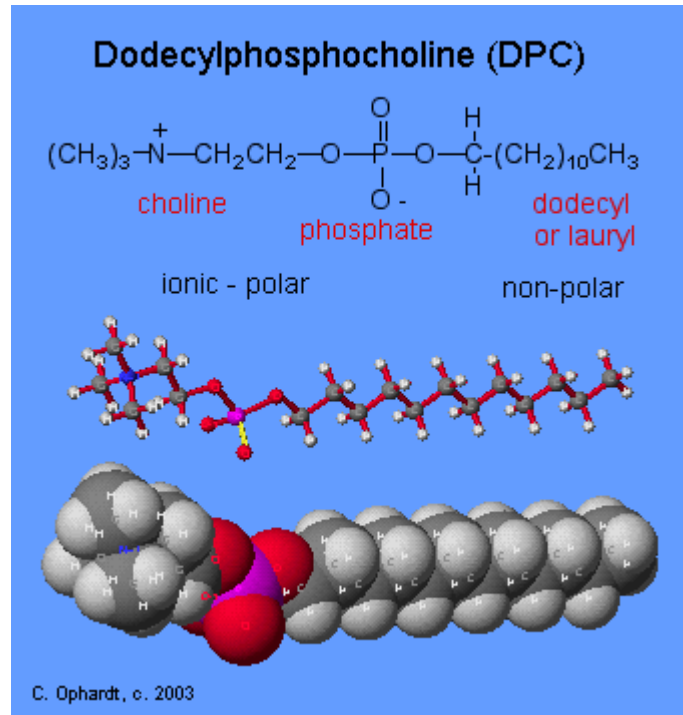
<http://employees.csbsju.edu/hjakubowski/Jmol/RevTurnTryInhib/revturnTrpInhib.htm>

### Type 2 and Type 1 Reverse Turns





# Micelles (Vesicle)



## Dodecylphosphocholine (DPC) Micelle

<http://employees.csbsju.edu/hjakubowski/Jmol/Micelle/micelle.htm>

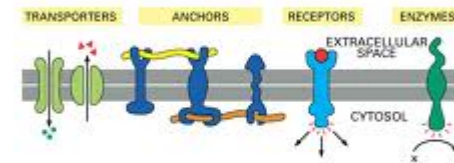
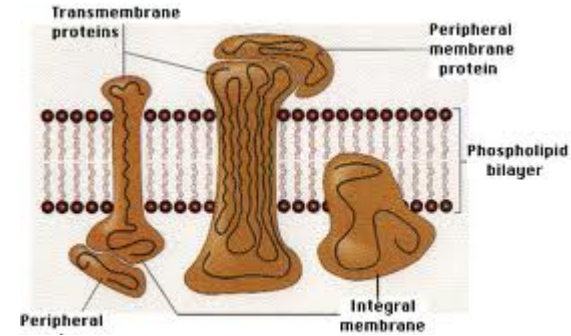


Figure 11-20 Essential Cell Biology, 6e, © 2004 Garland Science



*The Materials Science  
and Engineering  
Graduate Program*

**Materials Science and Engineering  
Graduate Seminar Series**

**January 12, 2012  
Baldwin 544/644  
2:00 - 2:50 pm**

*The Design of Vesicles*

Dr. Michael R. Weaver  
Analytic Discovery  
Procter & Gamble Corporation

## Protein with a buried hydrophobic group

<http://employees.csbsju.edu/hjakubowski/Jmol/HAAPBJmol/HAAPBBovineBuryF10.htm>

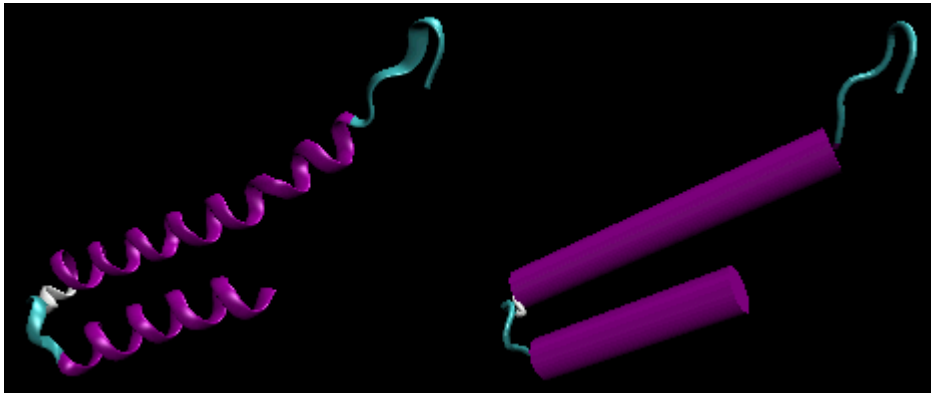
~50% of amino acids are in well defined secondary structures  
27% in  $\alpha$ -helix and 23% in  $\beta$ -sheets

Native state proteins have a packing density slightly higher than FCC/HCP 0.75 vs 0.74  
Organic liquids 0.6-0.7 Synthetic Polymer Chain in Solution ~0.001  
So the transition from an unfolded protein in solution to a native state protein  
involves a densification of about 750 to 1000 times.

Nonpolar 83% internal, Charged 54% exposed, uncharged 63% internal

# Super-Secondary Structures

## Common motifs



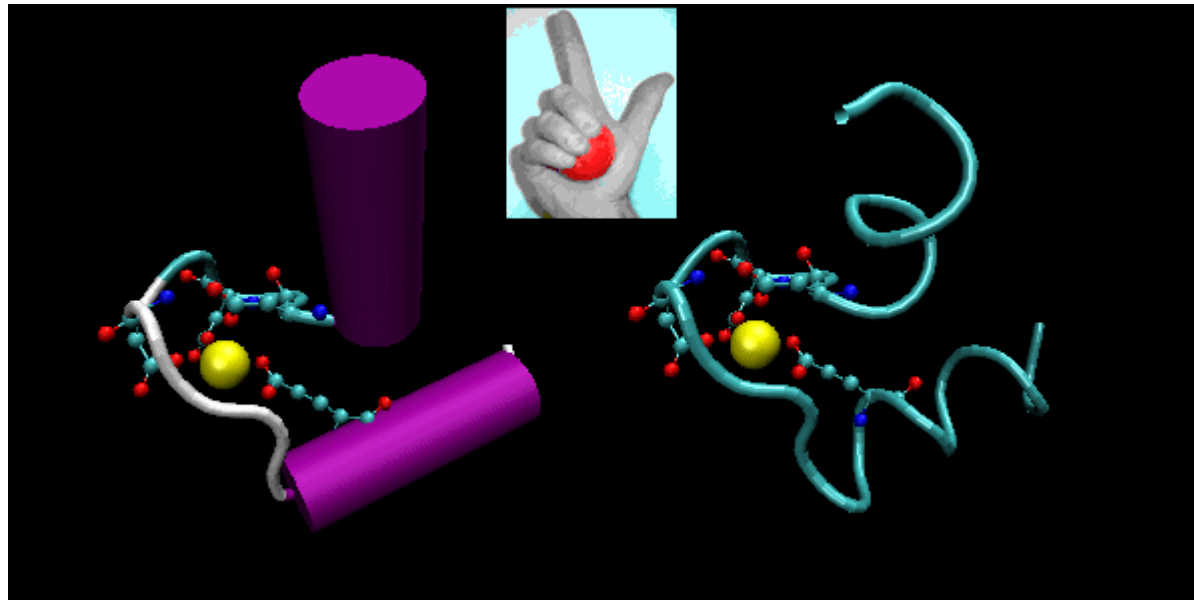
DNA and Calcium Binding sites

Helix-Loop-Helix

[http://employees.csbsju.edu/hjakubowski/Jmol/Lambda\\_Repressor/Lambda\\_Repressor.htm](http://employees.csbsju.edu/hjakubowski/Jmol/Lambda_Repressor/Lambda_Repressor.htm)

EF-Hand

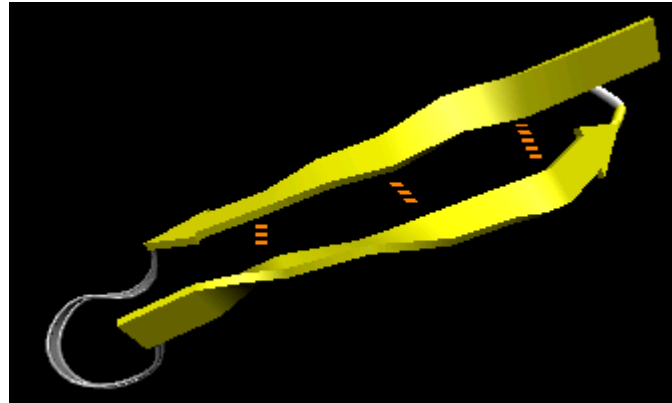
[http://employees.csbsju.edu/hjakubowski/Jmol/Calmodulin\\_EF\\_Hand/Calmodulin\\_EF\\_Hand.htm](http://employees.csbsju.edu/hjakubowski/Jmol/Calmodulin_EF_Hand/Calmodulin_EF_Hand.htm)



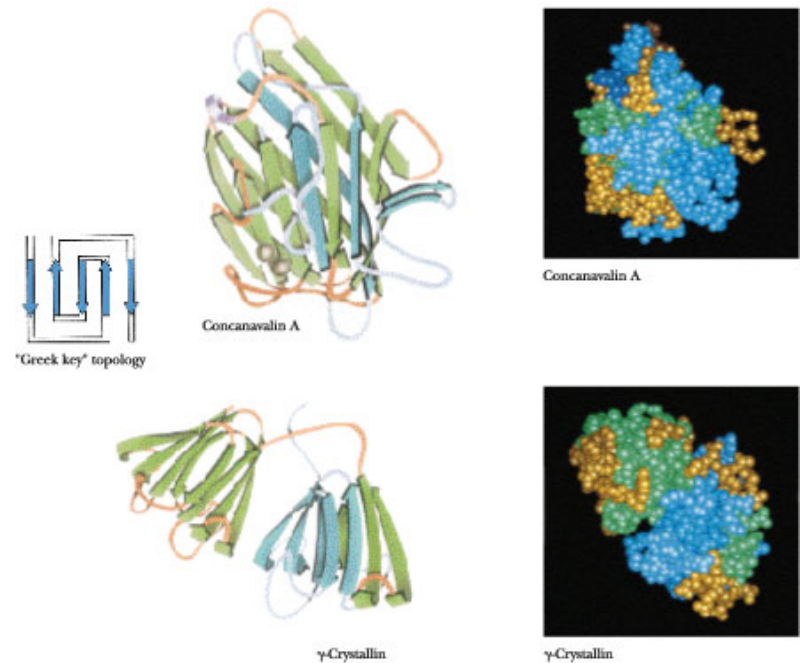
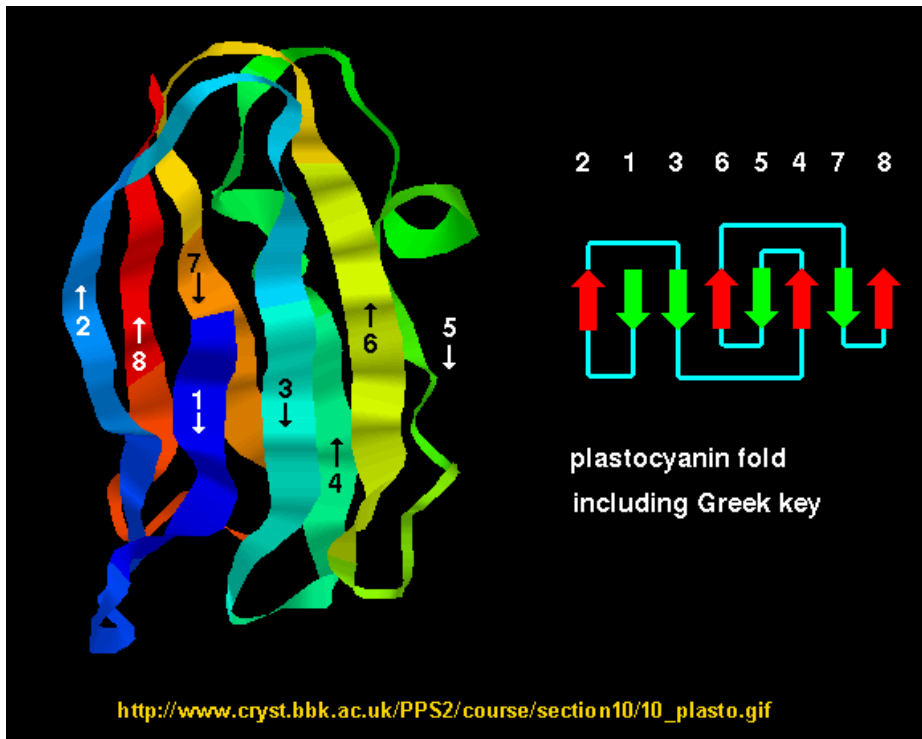
# Super-Secondary Structures

## $\beta$ -Hairpin or Beta-Beta in Anti-Parallel Structures

[http://employees.csbsju.edu/hjakubowski/Jmol/Bovine%20Pancreatic%20Trypsin%20Inhibitor/Bovine\\_Pancreatic\\_Trypsin\\_Inhibitor.htm](http://employees.csbsju.edu/hjakubowski/Jmol/Bovine%20Pancreatic%20Trypsin%20Inhibitor/Bovine_Pancreatic_Trypsin_Inhibitor.htm)

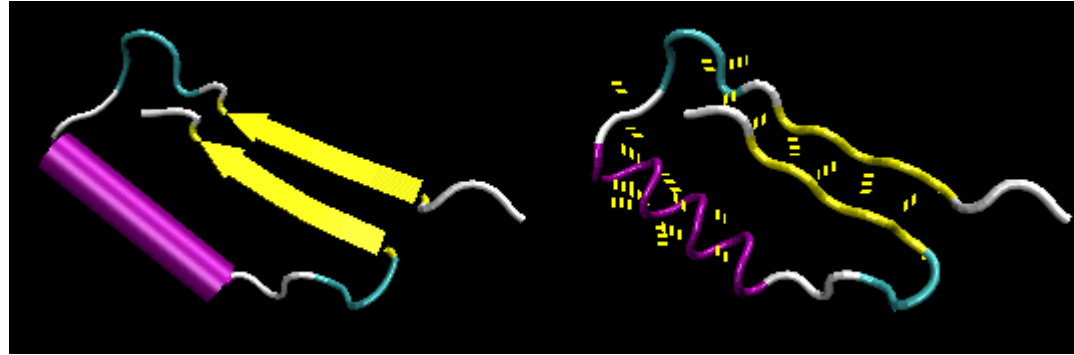


## Greek Key Motif



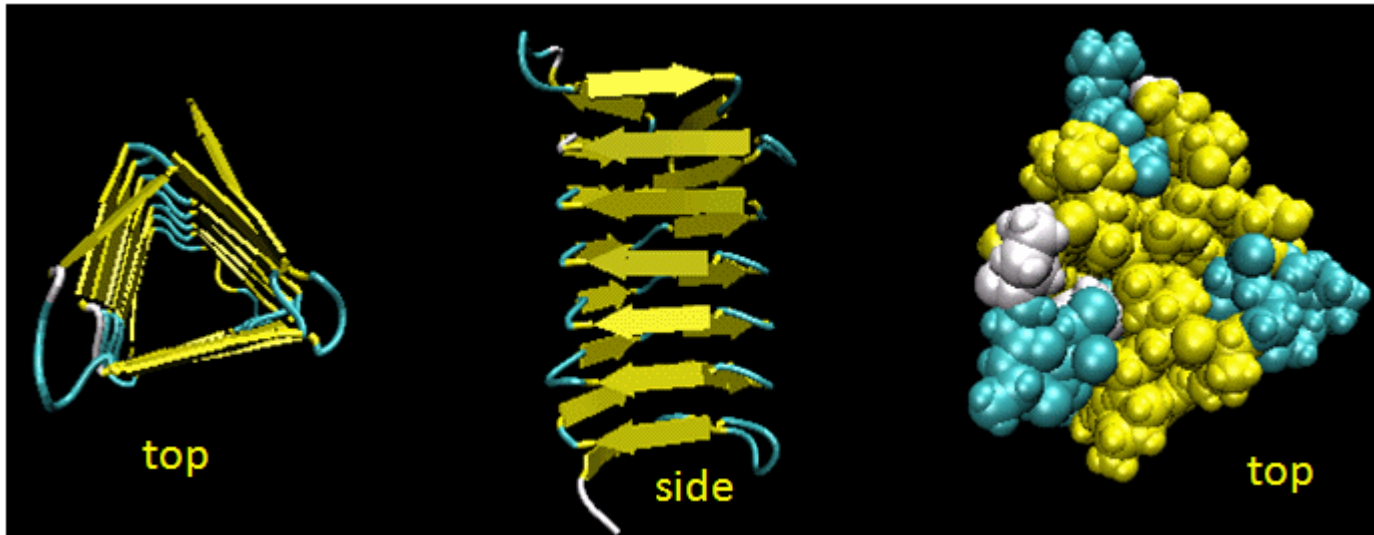
## Beta-Alpha-Beta (to connect two parallel $\beta$ -sheets)

[http://employees.csbsju.edu/hjakubowski/Jmol/BETA-ALPHA-BETA\\_MOTIFF/BETA-ALPHA-BETA\\_MOTIFF.htm](http://employees.csbsju.edu/hjakubowski/Jmol/BETA-ALPHA-BETA_MOTIFF/BETA-ALPHA-BETA_MOTIFF.htm)



## $\beta$ -Helicies (seen in pathogens, viruses, bacteria)

<http://cti.itc.virginia.edu/~cmg/Demo/pdb/ap/ap.htm>



Vibrio cholerae	cholera
Helicobacter pylori	ulcers
Plasmodium falciparum	malaria
Chlamydia trachomatis	VD
Chlamydophilia pneumoniae	respiratory infection
Trypanosoma brucei	sleeping sickness
Borrelia burgdorferi	Lymes disease
Bordetella parapertussis	whooping cough
Bacillus anthracis	anthrax
Neisseria meningitides	meningitis
Legionella pneumophila	Legionaire's disease

## **Many $\beta$ -Topologies**

[http://www.cryst.bbk.ac.uk/PPS2/course/section10/all\\_beta.html](http://www.cryst.bbk.ac.uk/PPS2/course/section10/all_beta.html)



## 3 Classes of Proteins (Characteristic Secondary Structures)

### $\alpha$ -Proteins

#### Cytochrome B562

[http://employees.csbsju.edu/hjakubowski/jmol/Cytochrome\\_B562/Cytochrome\\_B562.htm](http://employees.csbsju.edu/hjakubowski/jmol/Cytochrome_B562/Cytochrome_B562.htm)

#### Met-Myoglobin

<http://employees.csbsju.edu/hjakubowski/jmol/Met-Myoglobin>

### $\alpha\beta$ -Proteins

#### Triose Phosphate Isomerase

[http://employees.csbsju.edu/hjakubowski/jmol/Triose%20Phosphate%20Isomerase/TRIOSE\\_PHOSPHATE\\_ISOMERASE.htm](http://employees.csbsju.edu/hjakubowski/jmol/Triose%20Phosphate%20Isomerase/TRIOSE_PHOSPHATE_ISOMERASE.htm)

#### Hexokinase

<http://employees.csbsju.edu/hjakubowski/jmol/Hexokinase/HEXOKINASE.htm>

### $\beta$ -Proteins

#### Superoxide Dismutase

[http://employees.csbsju.edu/hjakubowski/jmol/Superoxide%20Dismutase/SUPEROXIDE\\_DISMUTASE.htm](http://employees.csbsju.edu/hjakubowski/jmol/Superoxide%20Dismutase/SUPEROXIDE_DISMUTASE.htm)

#### Human IgG I Antibody

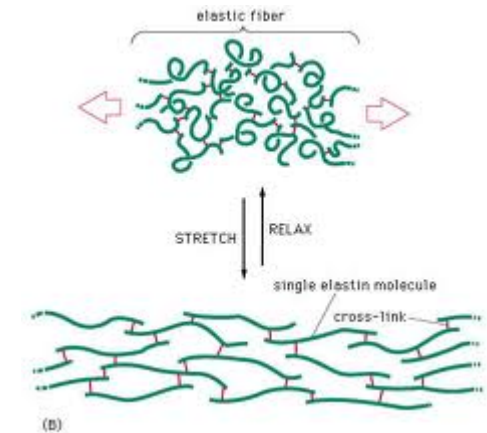
[http://employees.csbsju.edu/hjakubowski/jmol/Human%20Antibody%20Molecule-IgG1/Human\\_Antibody\\_Molecule%20AD\\_IgG1.htm](http://employees.csbsju.edu/hjakubowski/jmol/Human%20Antibody%20Molecule-IgG1/Human_Antibody_Molecule%20AD_IgG1.htm)

#### Retinol Binding Protein

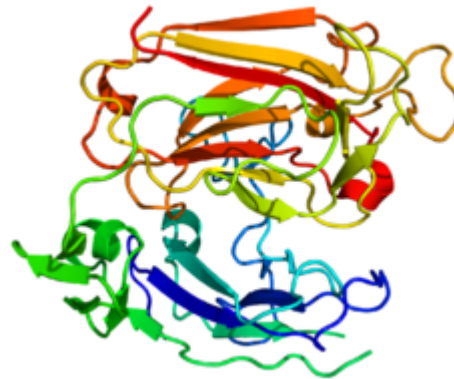
[http://employees.csbsju.edu/hjakubowski/jmol/Retinol%20Binding%20Protein/RETINOL\\_BINDING\\_PROTEIN.htm](http://employees.csbsju.edu/hjakubowski/jmol/Retinol%20Binding%20Protein/RETINOL_BINDING_PROTEIN.htm)

## Fibrillar (elastic) versus Globular Proteins

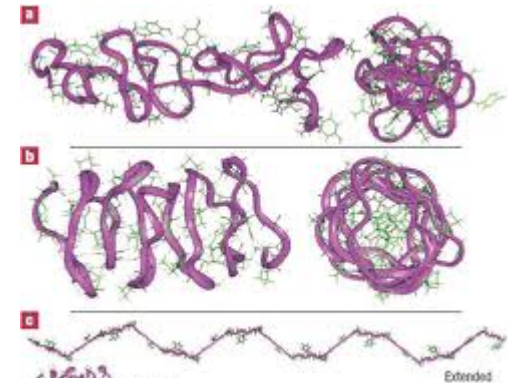
Elastin (Blood Vessels)  $\beta$ -sheets and  $\alpha$ -helices with  $\beta$ -turns



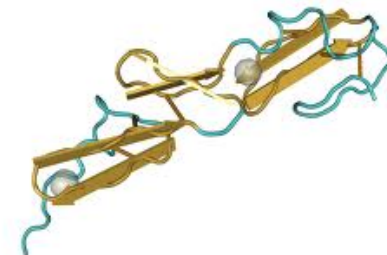
Resilin (Insect Wings)



Silk (Spiders etc.)  $\beta$ -sheets and  $\alpha$ -helices with  $\beta$ -turns



Fibrillin (Cartilage) - Folded  $\beta$ -Sheet like and Accordion

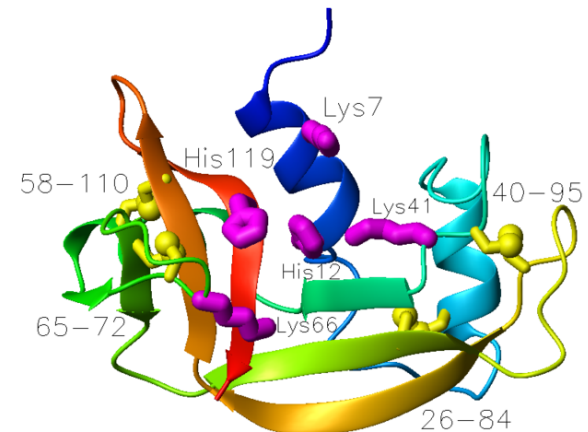


## Tertiary Structure and Protein Folding

Consider a protein of 100 residues each with two bond angles  $\Phi$  and  $\psi$  that can take 3 positions each so 9 conformations. The chain has  $9^{100} = 2.7 \times 10^{95}$  conformations. Even with  $10^{-13}$ s to change a conformation, it would take  $8.4 \times 10^{74}$  years to probe all conformations (that is along time).  
Such a protein folds in less than a second.  
This is called Levinthal's Paradox.

The key to resolving Levinthal's Paradox is to limit the choices.

Disulfide bonds are a major limiting factor,  
Consider Ribonuclease (RNase A) (an enzyme that degrades RNA)  
Having 4 disulfide bonds that serve as tethers for the folding process.



## RNase A

<http://www.rcsb.org/pdb/explore/jmol.do?structureId=7RSA&bionumber=1>

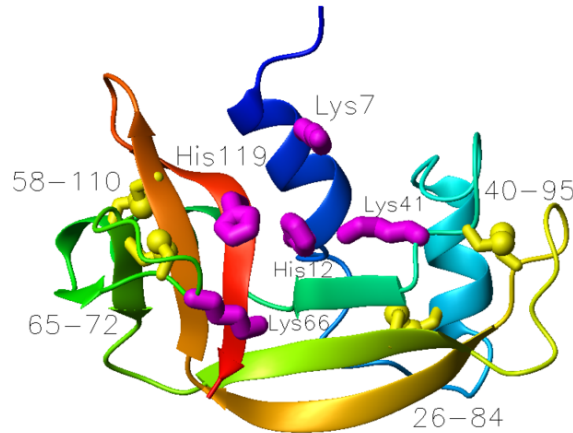
Folds “like a taco” to bind with the RNA substrate

Armour purified 1 kilo and gave it away for study

124 residues 13.7 kDa

Polycation that binds with polyanionic RNA

Positive charges are in the taco cleft.



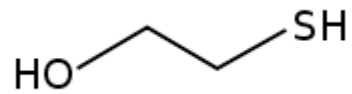
Nobel Prize Lecture published as:

Anfinsen, C.B. (1973) "Principles that govern the folding of protein chains." Science 181 223-230.

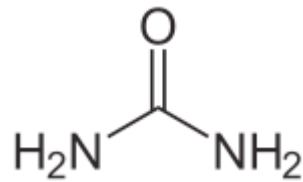
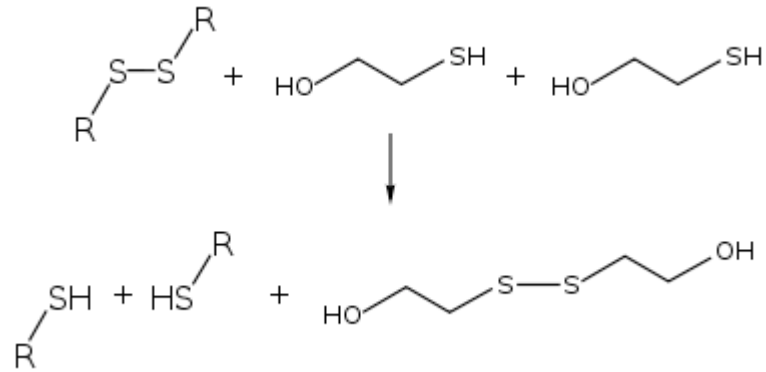
Anfinsen Postulate: For Small Globular Proteins the  
Tertiary Structure is determined only by the amino acid  
sequence

## RNase Structure

<http://employees.csbsju.edu/hjakubowski/Jmol/RNase/RNase.htm>

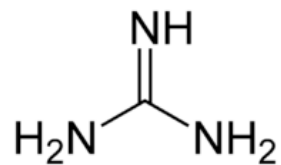


**β-Mercapto Ethanol**



**Urea**

Competes with H-Bonds  
Denatures (Destablizes) Proteins



**Guanidine-HCl**

Competes with H-Bonds  
Denatures (Destablizes) Proteins

**Figure: Anfinsen Experiment: Folding of RNase**

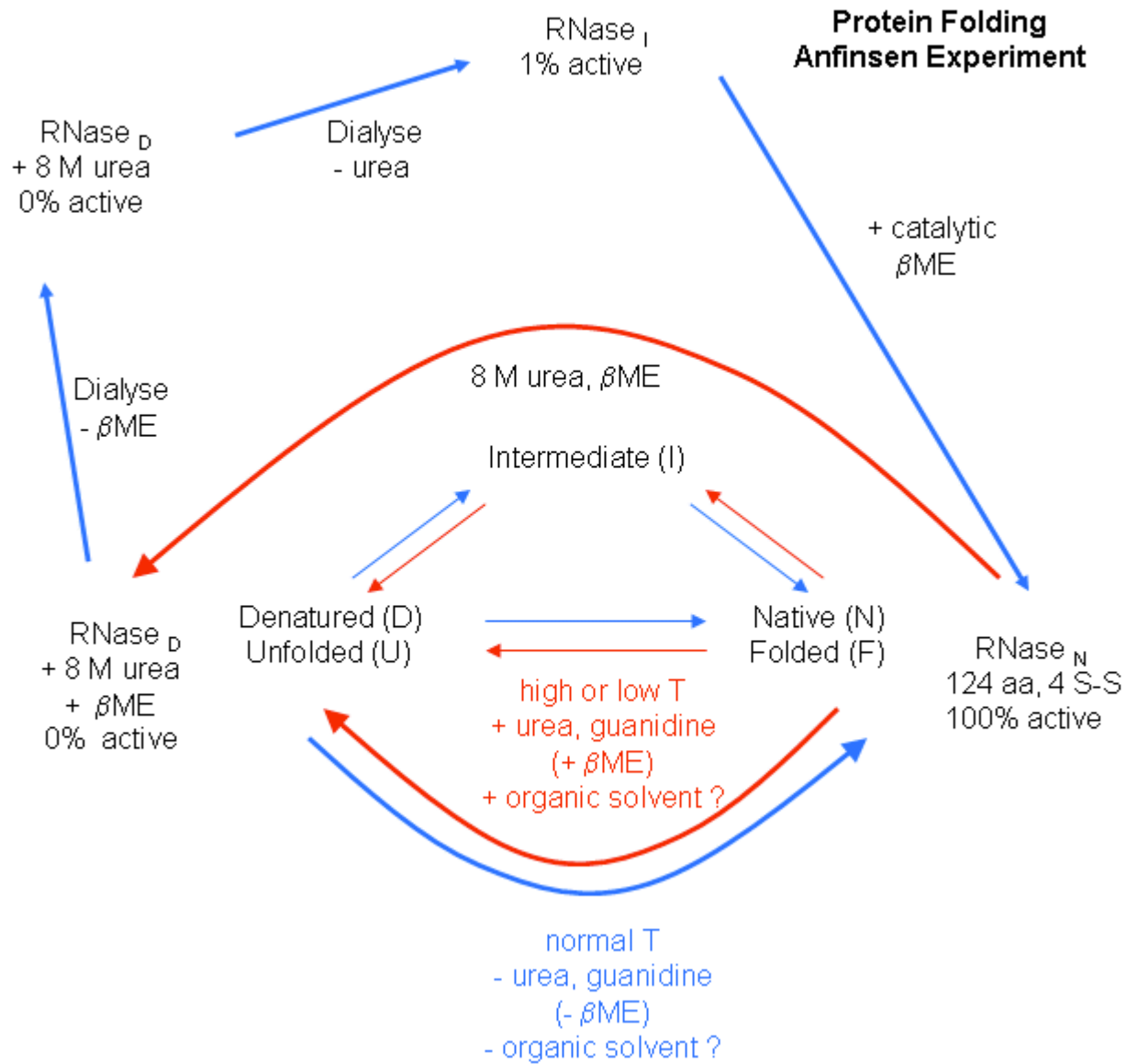
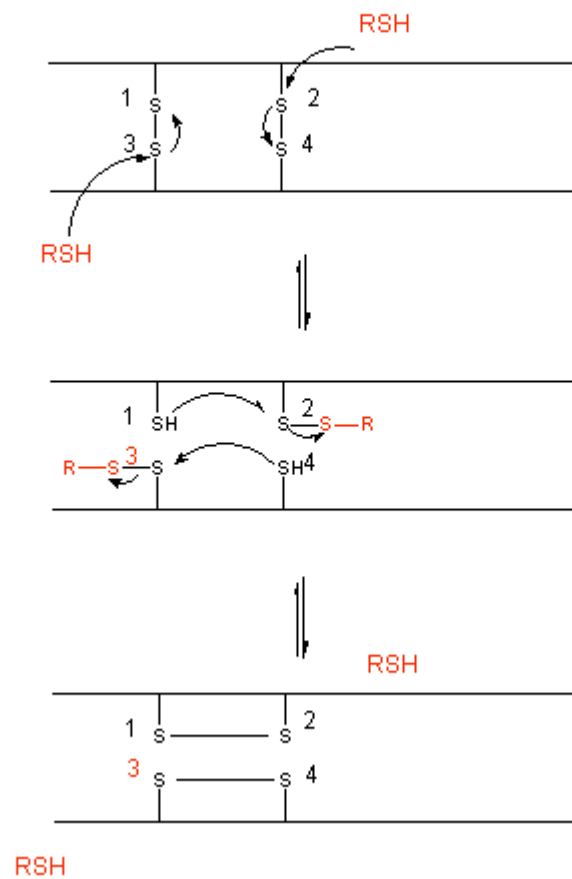


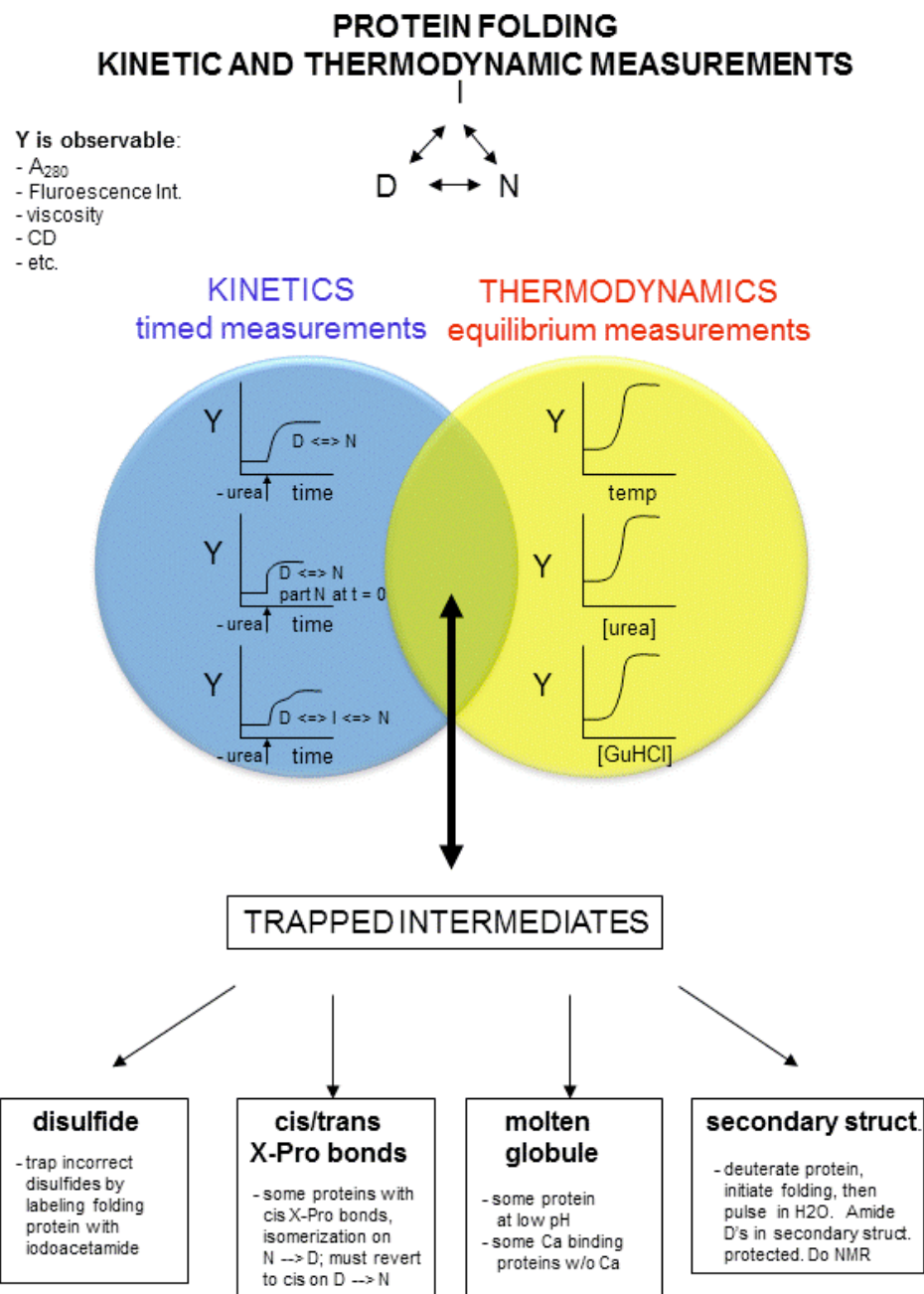
Figure: CATALYTIC SHUFFLING OF DISULFIDES WITH BETA-MERCAPTOETHANOL

Disulfide Shuffling using catalytic [ $\beta$ -mercaptoethanol]



<http://employees.csbsju.edu/hjakubowski/classes/ch331/protstructure/olprotfold.html>

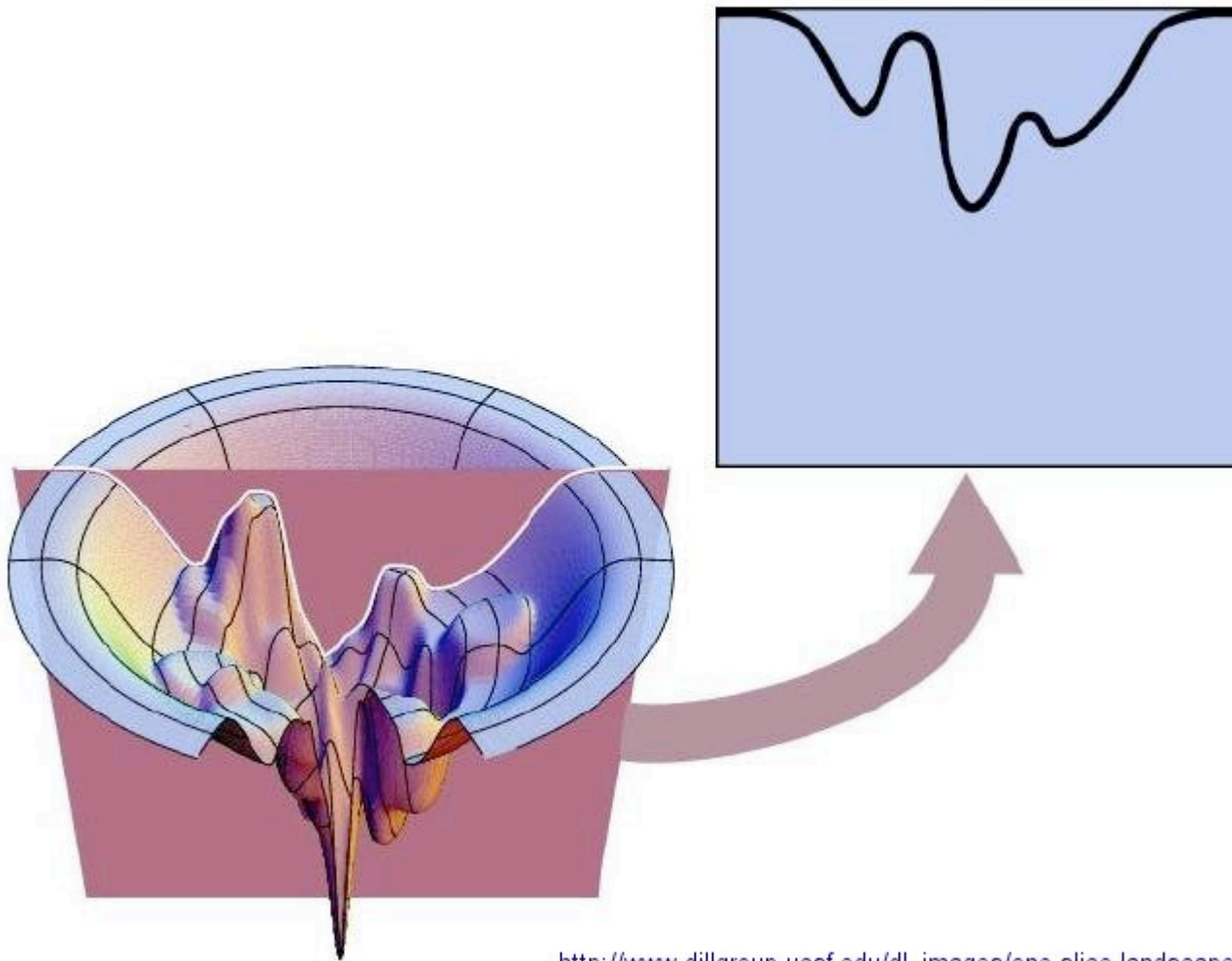
**Figure: Kinetic and thermodynamic measurements of proteins stability and folding**





# Native state is a “Global Minimum in Free Energy” Folding Process Occurs on an Energy “Funnel”

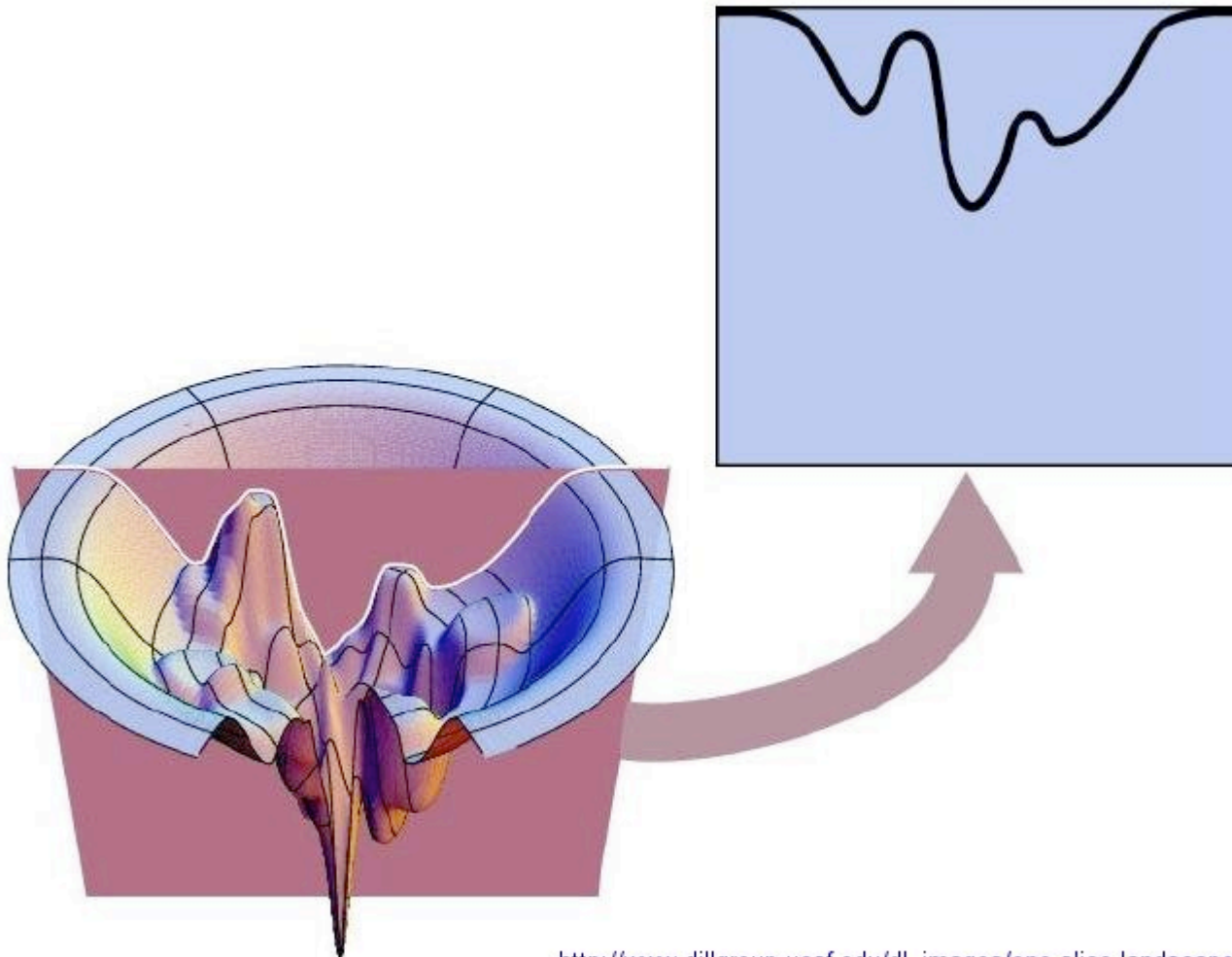
Figure: Protein Folding Landscape: One View from Ken Dill



[http://www.dillgroup.ucsf.edu/dl\\_images/one-slice-landscape.jpg](http://www.dillgroup.ucsf.edu/dl_images/one-slice-landscape.jpg)

**Folding does not occur by a single pathway, but is a statistical process of searching the energy landscape for minima**  
**For large proteins we see intermediates, molten globules, non-biologically active dense states**

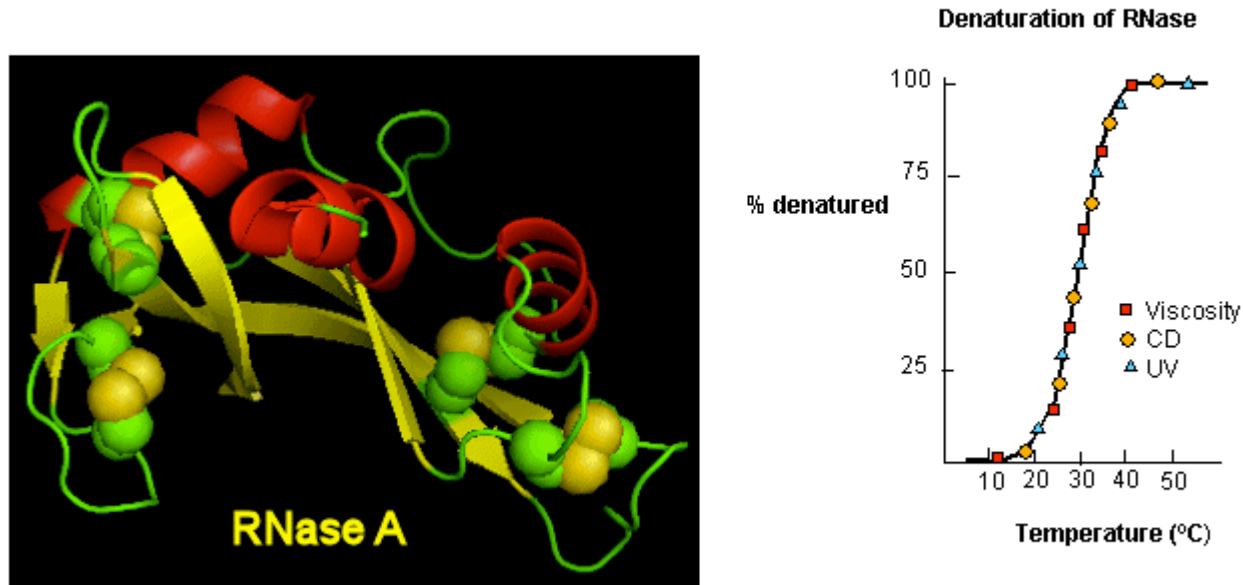
**Figure: Protein Folding Landscape: One View from Ken Dill**



[http://www.dillgroup.ucsf.edu/dl\\_images/one-slice-landscape.jpg](http://www.dillgroup.ucsf.edu/dl_images/one-slice-landscape.jpg)

## Simple proteins undergo a cooperative process

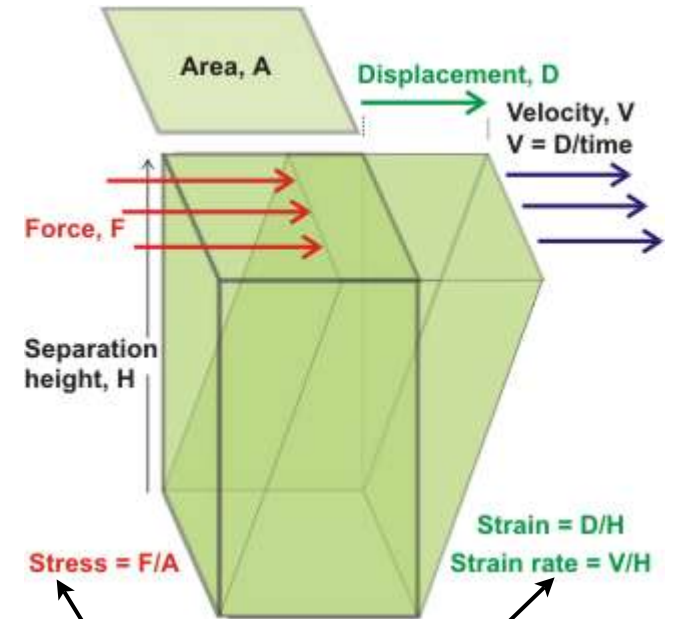
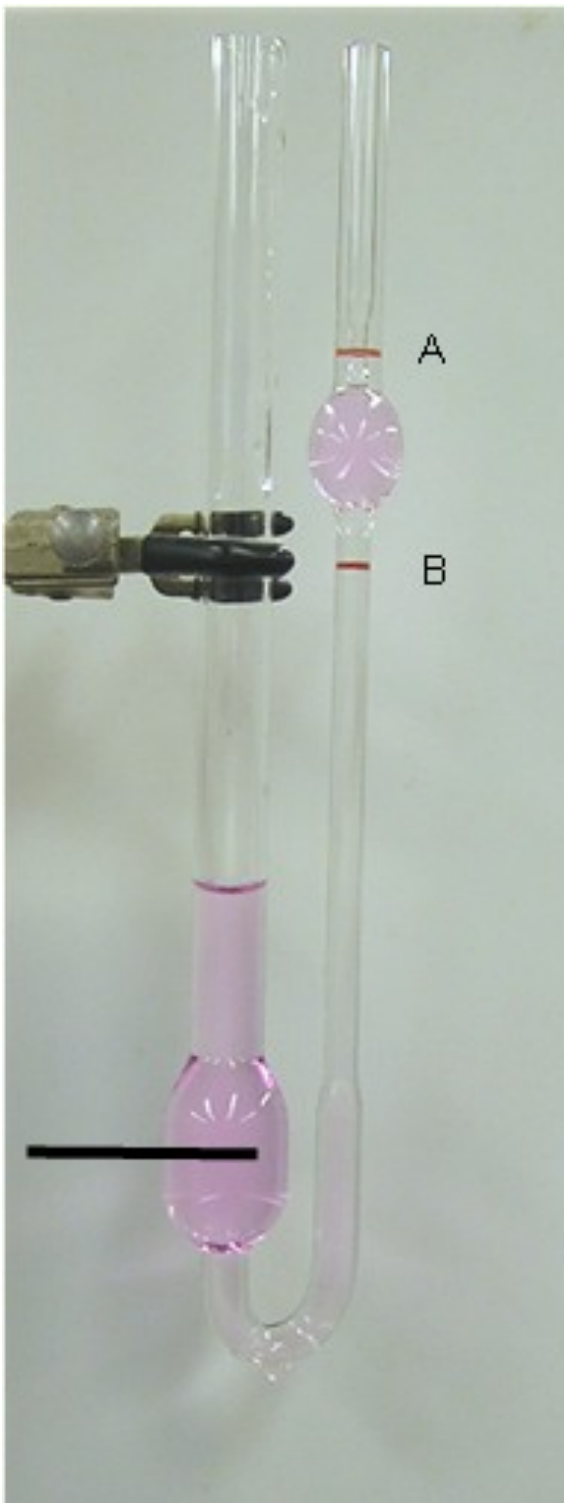
Figure: Reversible denaturation



after Ginsburg and Carroll, *Biochemistry* 4, pg 2159 (1965)

y-axis could be  
viscosity (hydrodynamic radius),  
circular dichroism,  
fluorescence,  
diffusion coefficient (hydrodynamic radius) from dynamic light scattering,  
radius of gyration from static light scattering

# Viscosity



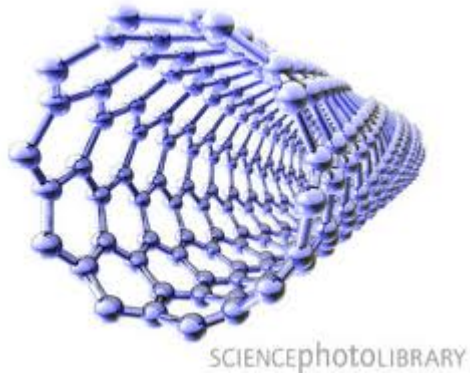
$$\tau = \eta \dot{\gamma}$$

$$\eta_s = \eta_0 (1 + [\eta]\phi)$$

$$[\eta] \approx \frac{V_{Molecule}}{M_{Molecule}}$$

Native state has the smallest volume

## Mass Fractal Dimension, $1 \leq d_f \leq 3$



Mass  $\sim$  Size<sup>1</sup>

1-d

$d_f = 1$



Mass  $\sim$  Size<sup>2</sup>

2-d

$d_f = 2$



Mass  $\sim$  Size<sup>3</sup>

3-d

$d_f = 3$

## Mass Fractal Dimension, $1 \leq d_f \leq 3$

### Random (Brownian) Walk $\theta$ -Solvent Condition

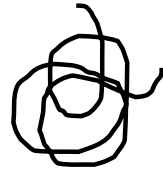
$$\text{Mass} \sim \text{Size}^2 \qquad 2\text{-d} \qquad d_f = 2$$



### Self-Avoiding Walk/Expanded Coil Good Solvent Condition

$$\text{Mass} \sim \text{Size}^{1.67} \qquad d_f = 5/3$$

In the collapse transition from an expanded coil to a native state for a protein of 100 residues ( $N = \text{Mass} = 100$ )  
Size  $\sim 15.8$  for Expanded Coil (10 for Gaussian) and 4.6 for Native State  
For  $N = 10000$  this becomes 251 : 100 : 21.5  
For large proteins the change in size is dramatic (order of 10x)



## 1) Mass Fractal dimension, $d_f$ .

$$z = \alpha \left( \frac{2R}{d_p} \right)^{d_f}$$

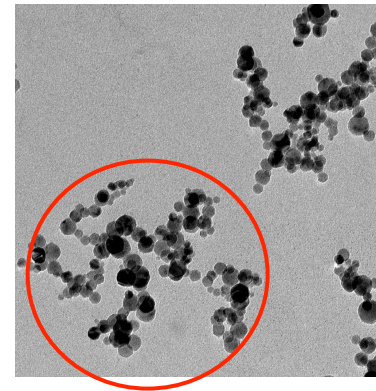
$z$  is mass/DOA  
 $d_p$  is bead size  
 $R$  is coil size

**Random aggregation (right)  $d_f \sim 1.8$ ;**  
**Randomly Branched Gaussian  $d_f \sim 2.5$ ;**  
**Self-Avoiding Walk  $d_f = 5/3$**

**Problem:**

**Disk  $d_f = 2$**

**Gaussian Walk  $d_f=2$**

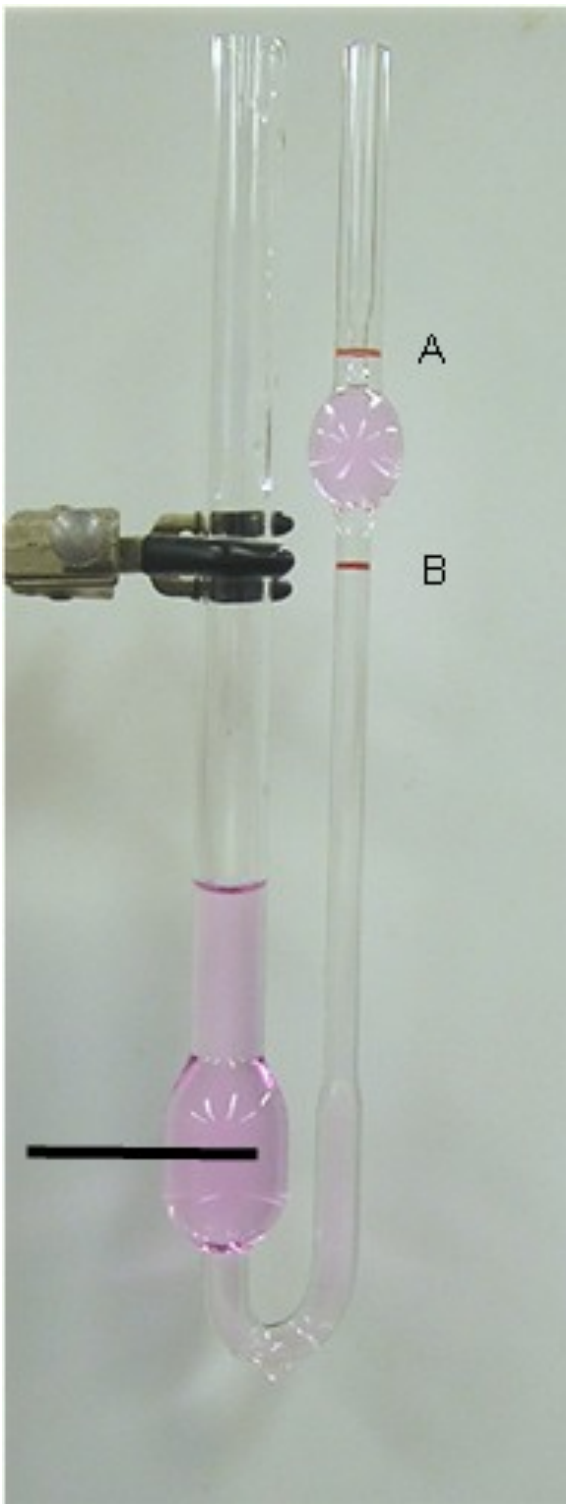


Nano-titania from Spray Flame

$$2R/d_p = 10, \alpha \sim 1, z \sim 220$$

$$d_f = \ln(220)/\ln(10) = 2.3$$

**A Measure of Branching is not Given.**



## Viscosity

$$\eta_s = \eta_0 (1 + [\eta]\phi)$$

$$[\eta] \approx \frac{V_{Molecule}}{M_{Molecule}}$$

For the Native State Mass  $\sim \rho V_{Molecule}$

Einstein Equation (for Suspension of 3d Objects)

$$\eta_s = \eta_0 (1 + 2.5\phi)$$

For “Gaussian” Chain Mass  $\sim \text{Size}^2 \sim V^{2/3}$

$$V \sim \text{Mass}^{3/2}$$

For “Expanded Coil” Mass  $\sim \text{Size}^{5/3} \sim V^{5/9}$

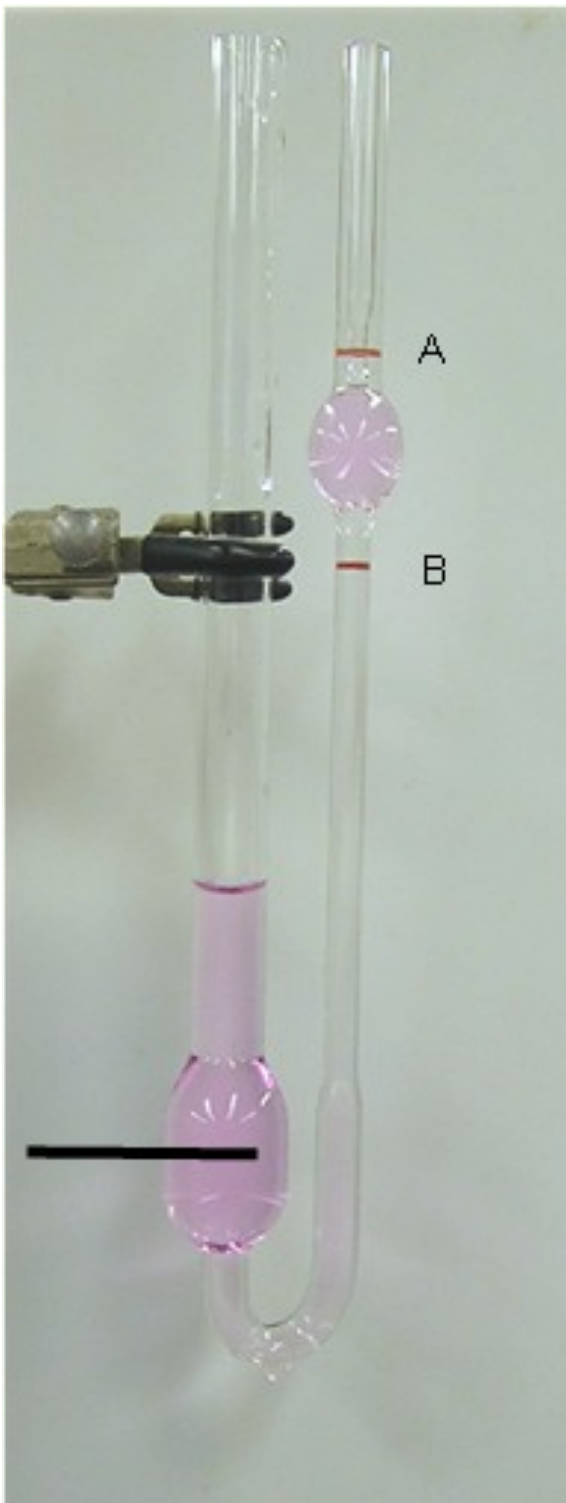
$$V \sim \text{Mass}^{9/5}$$

For “Fractal” Mass  $\sim \text{Size}^{df} \sim V^{df/3}$

$$V \sim \text{Mass}^{3/df}$$

$$[\eta] \sim M_{Molecule}^{\frac{3}{df}-1}$$





## Viscosity

$$\eta_s = \eta_0 (1 + [\eta]\phi)$$

$$[\eta] \approx \frac{V_{Molecule}}{M_{Molecule}}$$

For the Native State Mass  $\sim \rho V_{Molecule}$

Einstein Equation (for Suspension of 3d Objects)

$$\eta_s = \eta_0 (1 + 2.5\phi)$$

For “Gaussian” Chain Mass  $\sim \text{Size}^2 \sim V^{2/3}$   
 $V \sim \text{Mass}^{3/2}$

“Size” is the  
**“Hydrodynamic Size”** For “Expanded Coil” Mass  $\sim \text{Size}^{5/3} \sim V^{5/9}$   
 $V \sim \text{Mass}^{9/5}$

For “Fractal” Mass  $\sim \text{Size}^{df} \sim V^{df/3}$   
 $V \sim \text{Mass}^{3/df}$

$$[\eta] \sim M_{Molecule}^{\frac{3}{df}-1}$$

# Circular Dichroism

## Light Polarization

<http://www.enzim.hu/~szia/cddemo/edemo0.htm?CFID=1025184&CFTOKEN=88815524>

## CD Spectroscopy for Proteins

[http://www.cryst.bbk.ac.uk/PPS2/course/section8/ss-960531\\_21.html](http://www.cryst.bbk.ac.uk/PPS2/course/section8/ss-960531_21.html)

<http://www.ruppweb.org/cd/cdtutorial.htm>

## Wikipedia on CD

[http://en.wikipedia.org/wiki/Circular\\_dichroism](http://en.wikipedia.org/wiki/Circular_dichroism)

$\Delta\varepsilon = \varepsilon_L - \varepsilon_R$  Molar Circular Dichroism (c = molar concentration)

$\Delta A = cl\Delta\varepsilon$  Difference in Absorption

$[\theta] = 3298.2\Delta\varepsilon$  Degrees of Ellipticity

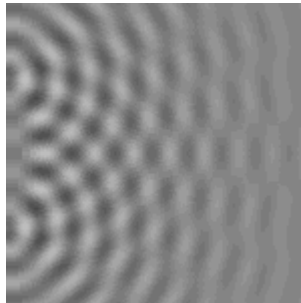
These change with the extent and nature of secondary structure such as helices

## Examples of CD

[http://www.ap-lab.com/circular\\_dichroism.htm](http://www.ap-lab.com/circular_dichroism.htm)



Binary Interference Yields Scattering Pattern.

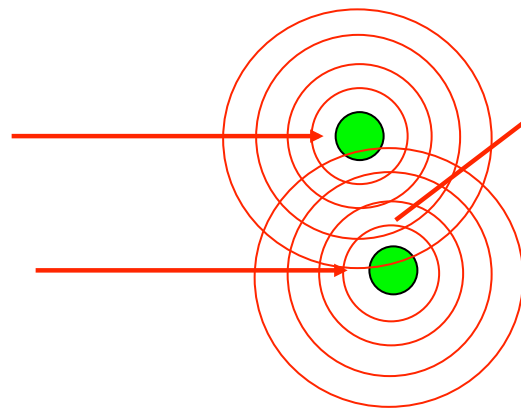


$$I(q) \sim N n_e^2$$

$n_e$  Reflects the density of a Point generating waves

$N$  is total number of points

## The Scattering Event



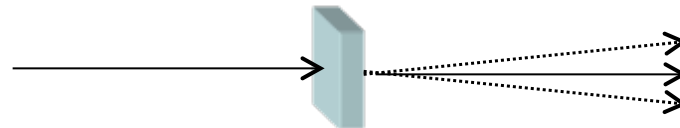
$I(q)$  is related to amount  $Nn^2$

$q$  is related to size/distances

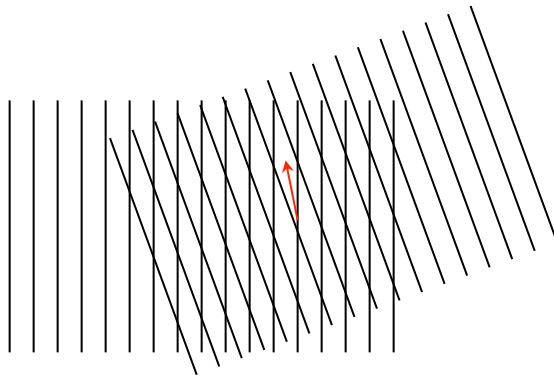
$$q = \frac{4\pi}{\lambda} \sin\left(\frac{\theta}{2}\right)$$

$$d = \frac{2\pi}{q}$$

- 2) Rather than consider specific structures, we can consider *general scattering laws* by which all scatters are governed under the premises that 1) “Particles” have a size and 2) “Particles” have a surface.



## Binary Interference Yields Scattering Pattern.



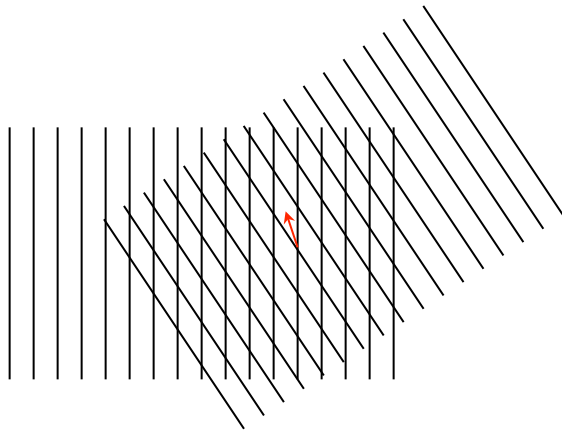
-Consider that an in-phase wave scattered at angle  $\theta$  was in phase with the incident wave at the source of scattering.

-This can occur for points separated by  $r$  such that

$$|r| = 2\theta/|q|$$

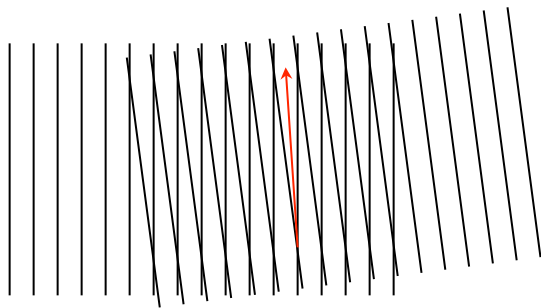
$$- q = \frac{4\pi}{\lambda} \sin \frac{\theta}{2}$$

Binary Interference Yields Scattering Pattern.



-For high  $\theta$ ,  $r$  is small

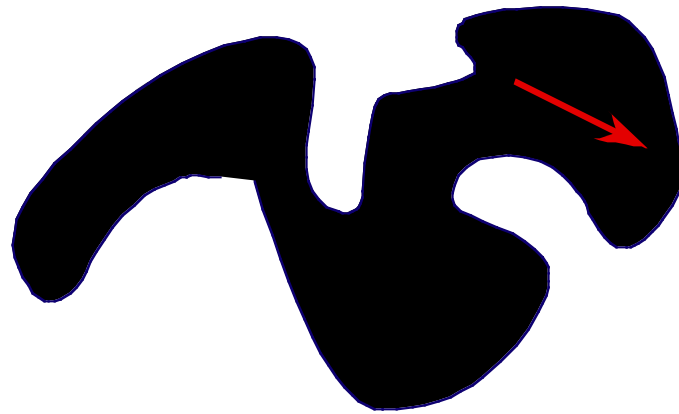
Binary Interference Yields Scattering Pattern.



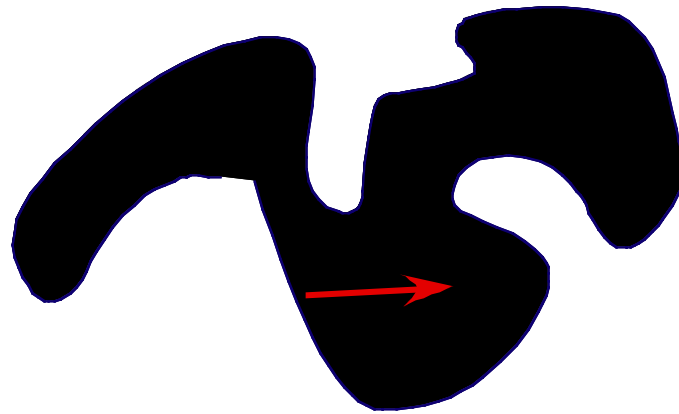
-For small  $\theta$ ,  $r$  is large



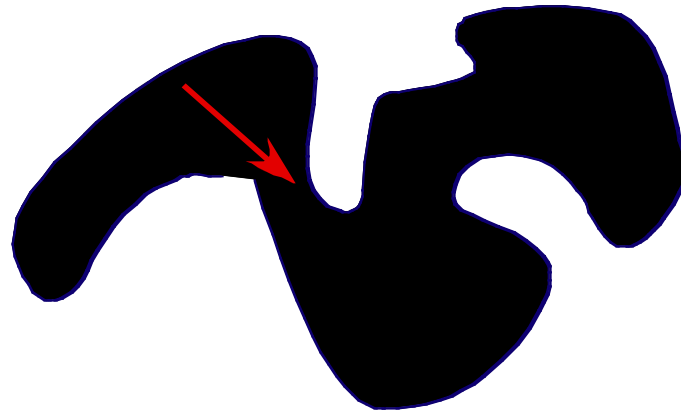
For an isotropic sample we consider scattering as arising from the probability of the random placement of a vector  $r$  in the scattering phase.



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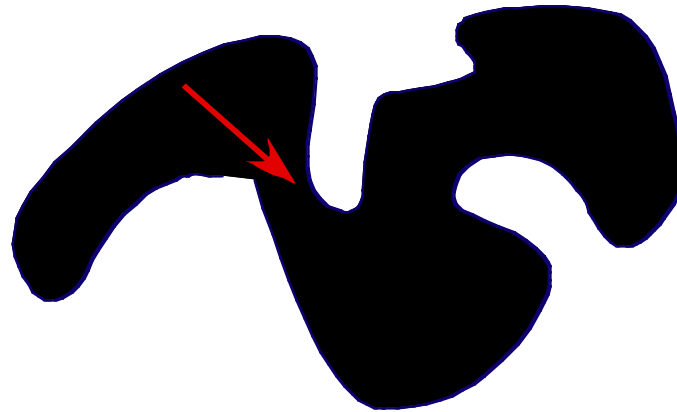


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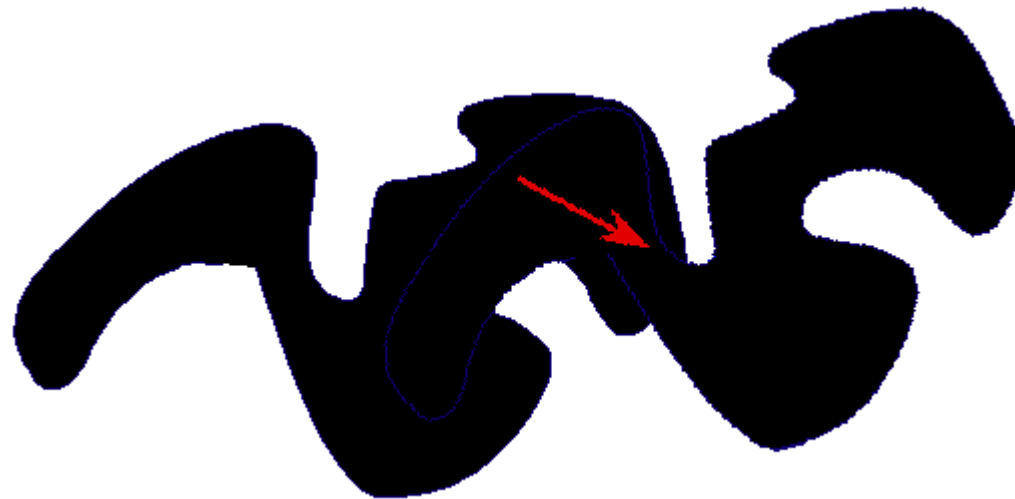
Rather than random placement of the vector we can hold  
The vector fixed and rotate the particle

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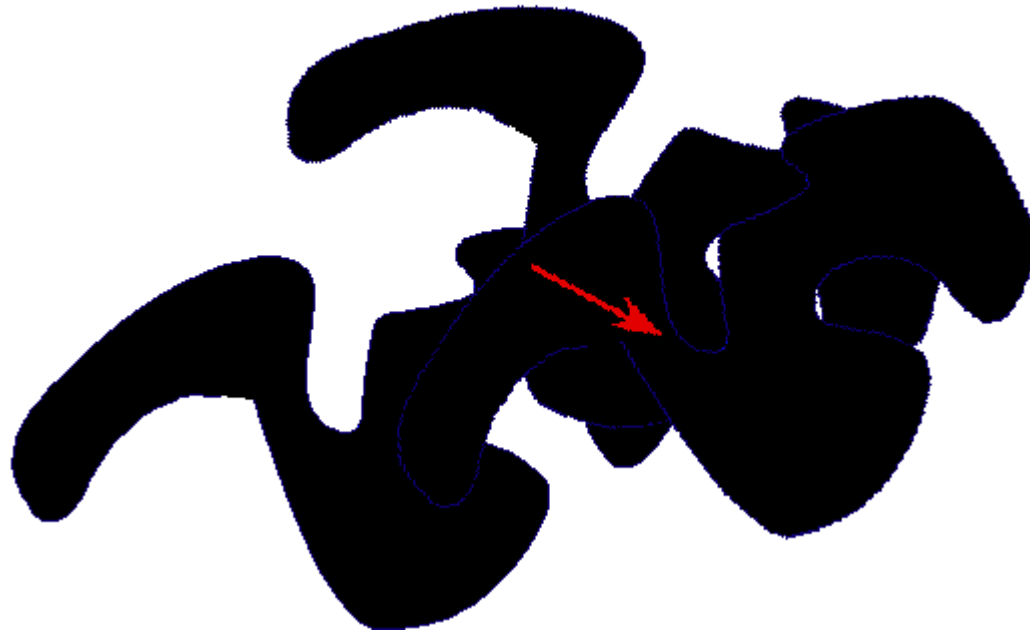
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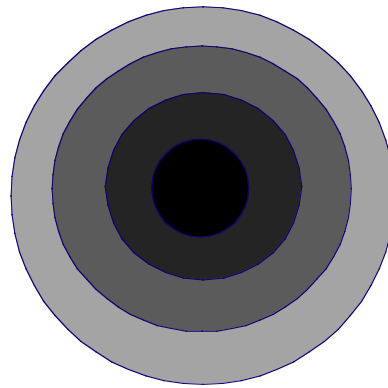
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Rather than random placement of the vector we can hold  
The vector fixed and rotate the particle

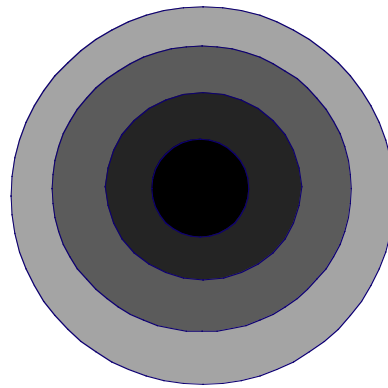
The particle becomes a probability density function from the center of mass.



That follows a Gaussian Distribution.

$$p(r) = \exp\left(\frac{-3r^2}{4R_g^2}\right)$$

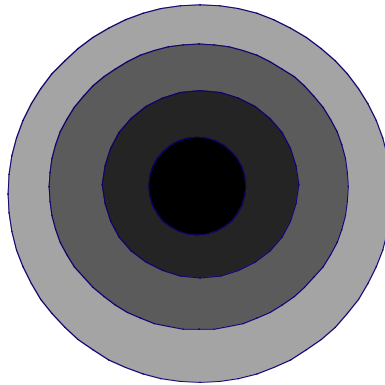
The particle becomes a probability density function from the center of mass.



Whose Fourier Transform is Guinier's Law.

$$p(r) = \exp\left(\frac{-3r^2}{4R_g^2}\right) \quad \Rightarrow \quad I(q) = G \exp\left(-\frac{q^2 R_g^2}{3}\right)$$
$$G = Nn_e^2$$

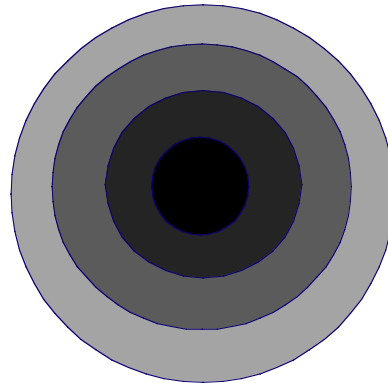




Guinier's Law Pertains to a Particle with no Surface.

$$p(r) = \exp\left(\frac{-3r^2}{4R_g^2}\right) \quad \Rightarrow \quad I(q) = G \exp\left(-\frac{q^2 R_g^2}{3}\right)$$
$$G = Nn_e^2$$

**Any** "Particle" can be Approximated as a Gaussian probability distribution in this context.



$$p(r) = \exp\left(\frac{-3r^2}{4R_g^2}\right) \quad \Rightarrow \quad I(q) = G \exp\left(-\frac{q^2 R_g^2}{3}\right)$$
$$G = N n_e^2$$

Guinier's Law can be thought of as the  
***First Premise of Scattering:***  
***All "Particles" have a size reflected by the radius of gyration.***

## Static Light Scattering for Radius of Gyration

Consider binary interference at a distance “r” for a particle with arbitrary orientation  
 Rotate and translate a particle so that two points separated by r lie in the particle for all rotations  
 and average the structures at these different orientations

Guinier's Law

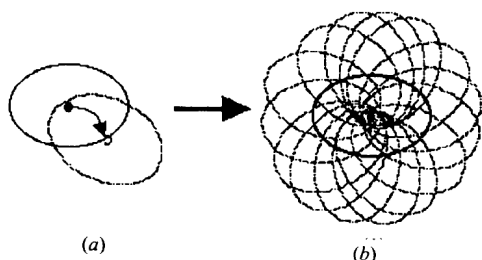


Fig. 4. Averaging of a particle about the origin of the vector  $r$  in analogy to random translations and rotations of the particle about the origin of  $r$ . In (a), a single rotation and a single translation are considered. In (b), the superposition of a number of such translations and rotations in random directions leads to a Gaussian distribution of scattering density  $\rho(r)$ .

$$\gamma_{Gaussian}(r) = \exp\left(-3r^2/2\sigma^2\right) \quad \text{Binary Autocorrelation Function}$$

$$\sigma^2 = \frac{\sum_{i=1}^N (x_i - \mu)^2}{N-1} = 2R_g^2$$

$$I(q) = I_e N n_e^2 \exp\left(-R_g^2 q^2 / 3\right)$$

Lead Term is

$$I(0) = N n_e^2$$

$$I(1/r) \sim N(r) n(r)^2$$

Scattered Intensity is the Fourier Transform of  
 The Binary Autocorrelation Function

$$\gamma_0(r) = 1 - \frac{S}{4V} r + \dots$$

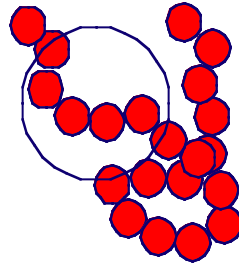
$$\exp\left(\frac{-3r^2}{4R_g^2}\right) \approx 1 - \frac{3r^2}{4R_g^2} + \dots$$

$$r \Rightarrow 0 \quad \text{then} \quad \frac{d(\gamma_{Gaussian}(r))}{dr} \Rightarrow 0$$

A particle with no surface



At intermediate sizes the chain is “self-similar”



$$Mass \sim Size^{d_f}$$

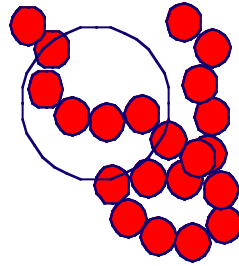
$$z \sim \left( \frac{R_2}{R_1} \right)^{d_f}$$

At intermediate sizes the chain is “self-similar”

$$I(q) \sim N n_e^2$$

N = Number of Intermediate Spheres in the Aggregate

$n_e$  = Mass of inter. sphere



$$I(q) \sim N n_e^2$$

$$N \sim \left( \frac{R_2}{r_{\text{int}}} \right)^{d_f}$$

$$n_e \sim \left( \frac{r_{\text{int}}}{R_1} \right)^{d_f}$$

$$N n_e^2 \sim \left( \frac{r_{\text{int}}}{R_1} \right)^{d_f} \left( \frac{R_2}{R_1} \right)^{d_f} \Rightarrow I(q) \sim \left( \frac{R_2}{R_1^2} \right)^{d_f} q^{-d_f}$$

## The Debye Scattering Function for a Polymer Coil

$$I(Q) = \frac{2}{Q^2} (Q - 1 + \exp(-Q))$$

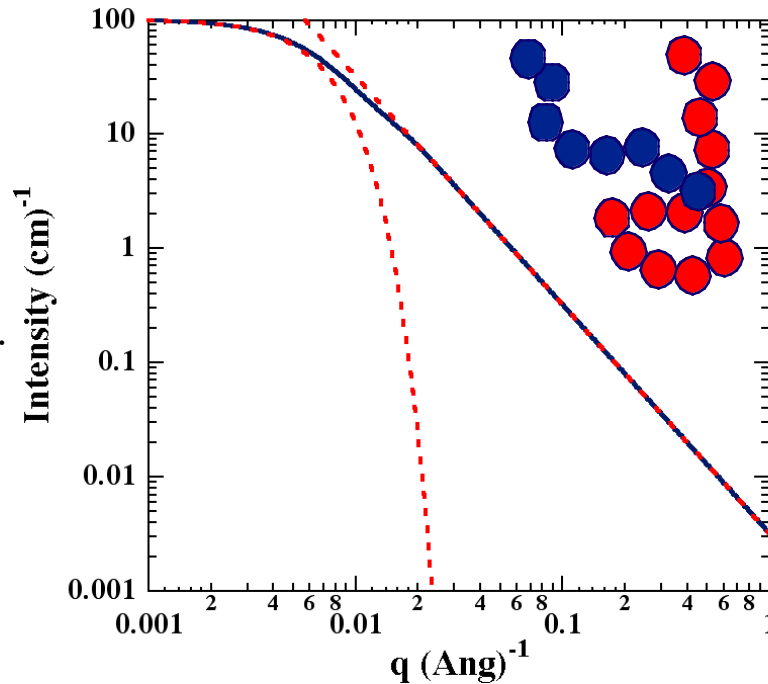
$$Q = q^2 R_g^2$$

For  $qR_g \ll 1$

$$\exp(-Q) = 1 - Q + \frac{Q^2}{2!} - \frac{Q^3}{3!} + \frac{Q^4}{4!} - \dots$$

$$I(q) = 1 - \frac{Q}{3} + \dots \approx \exp\left(-\frac{q^2 R_g^2}{3}\right)$$

Guinier's Law!



## The Debye Scattering Function for a Polymer Coil

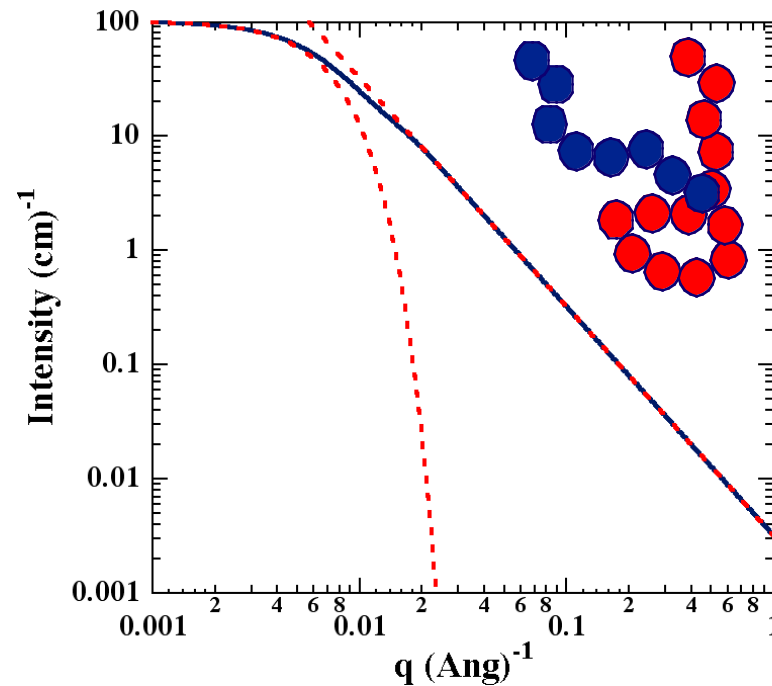
$$I(Q) = \frac{2}{Q^2} (Q - 1 + \exp(-Q))$$

$$Q = q^2 R_g^2$$

For  $qR_g \gg 1$

$$I(Q) = \frac{2}{Q} = \frac{2}{q^2 R_g^2} \sim q^{-d_f}$$

$$d_f = 2$$







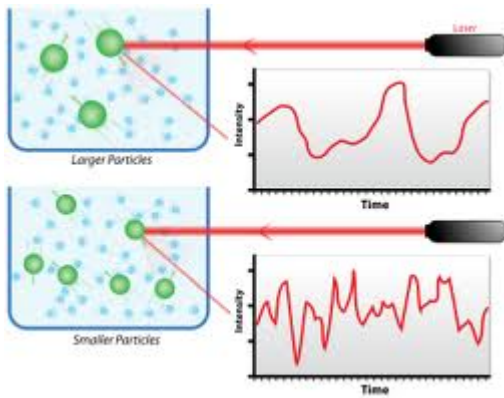
For static scattering  $\rho(r)$  is the binary spatial auto-correlation function

We can also consider correlations in time, binary temporal correlation function  
 $g_I(q, \tau)$

For dynamics we consider a single value of  $q$  or  $r$  and watch how the intensity changes with time  
 $I(q, t)$

We consider correlation between intensities separated by  $t$   
We need to subtract the constant intensity due to scattering at different size scales  
and consider only the fluctuations at a given size scale,  $r$  or  $2\pi/r = q$

# Dynamic Light Scattering



$$g^2(q; \tau) = \frac{\langle I(t)I(t + \tau) \rangle}{\langle I(t) \rangle^2}$$

$$g^2(q; \tau) = 1 + \beta [g^1(q; \tau)]^2$$

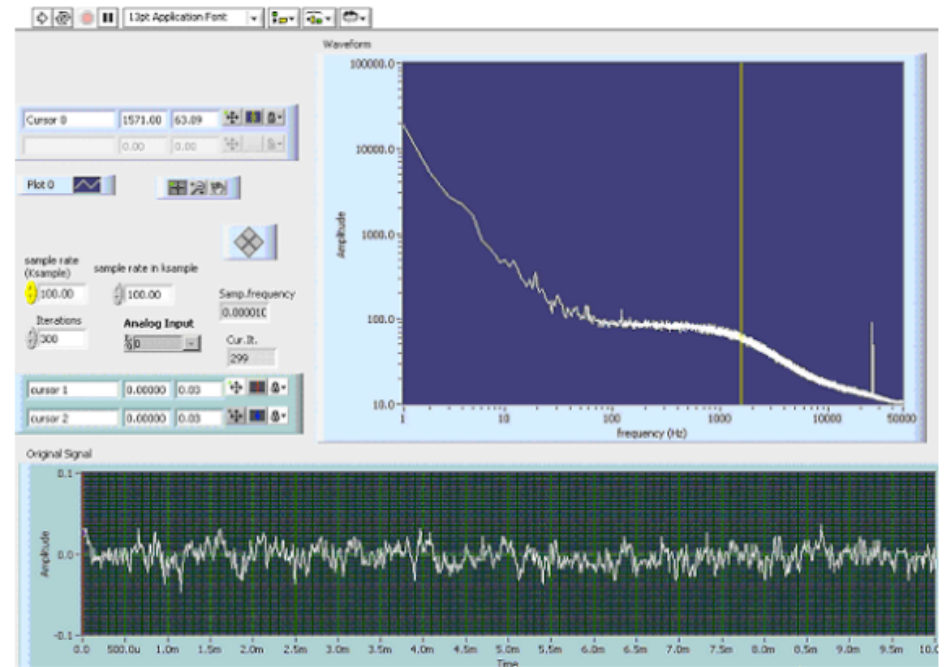
$$q = \frac{4\pi n_0}{\lambda} \sin\left(\frac{\theta}{2}\right)$$

$$g^1(q; \tau) = \exp(-\Gamma\tau)$$

$$\Gamma = q^2 D_t$$

$$D = k_B T / 6\pi\eta a$$

$a = R_H = \text{Hydrodynamic Radius}$



# Dynamic Light Scattering

## my DLS web page

<http://www.eng.uc.edu/~gbeaucag/Classes/Physics/DLS.pdf>

## Wiki

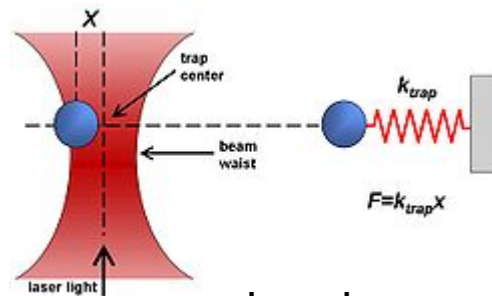
[http://webcache.googleusercontent.com/search?q=cache:eY3xhiX117IJ:en.wikipedia.org/wiki/Dynamic\\_light\\_scattering+&cd=1&hl=en&ct=clnk&gl=us](http://webcache.googleusercontent.com/search?q=cache:eY3xhiX117IJ:en.wikipedia.org/wiki/Dynamic_light_scattering+&cd=1&hl=en&ct=clnk&gl=us)

## Wiki Einstein Stokes

[http://webcache.googleusercontent.com/search?q=cache:yZDPRbqZ1BIJ:en.wikipedia.org/wiki/Einstein\\_relation\\_\(kinetic\\_theory\)+&cd=1&hl=en&ct=clnk&gl=us](http://webcache.googleusercontent.com/search?q=cache:yZDPRbqZ1BIJ:en.wikipedia.org/wiki/Einstein_relation_(kinetic_theory)+&cd=1&hl=en&ct=clnk&gl=us)



## Optical Tweezers



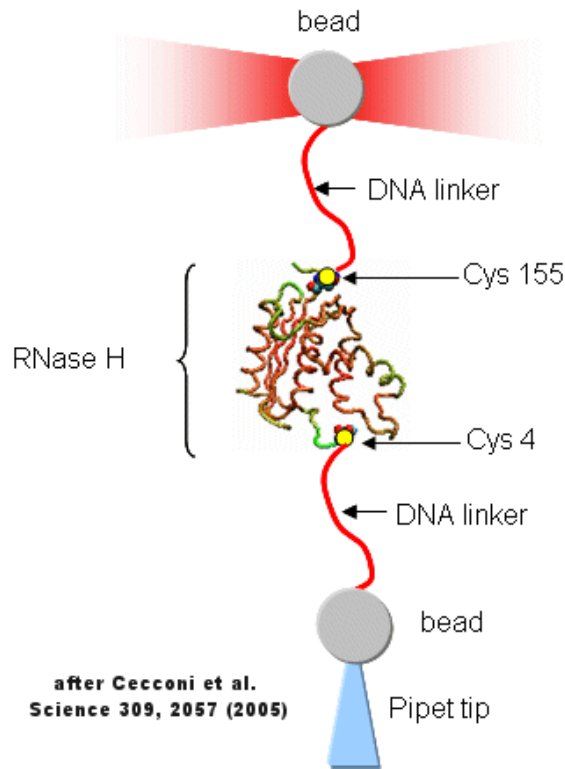
Dielectric particles are attracted to the center of a focused beam  
Scattering Force moves particles downstream

Force can be controlled with intensity of laser

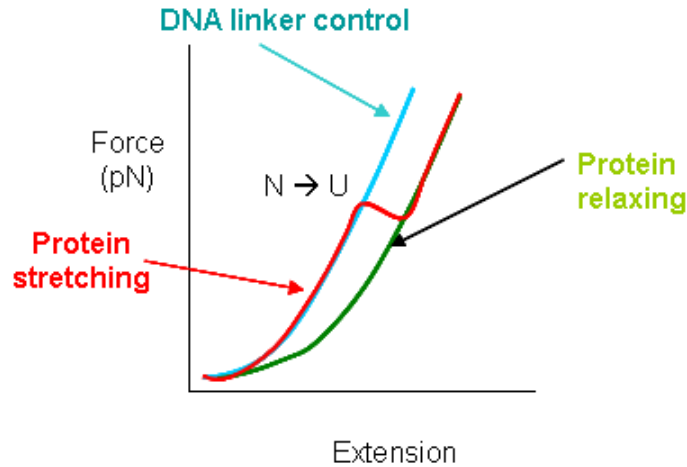
# Stretching of a single protein (RNase)

[Link to Paper at Science](http://www.sciencemag.org/content/309/5743/2057)

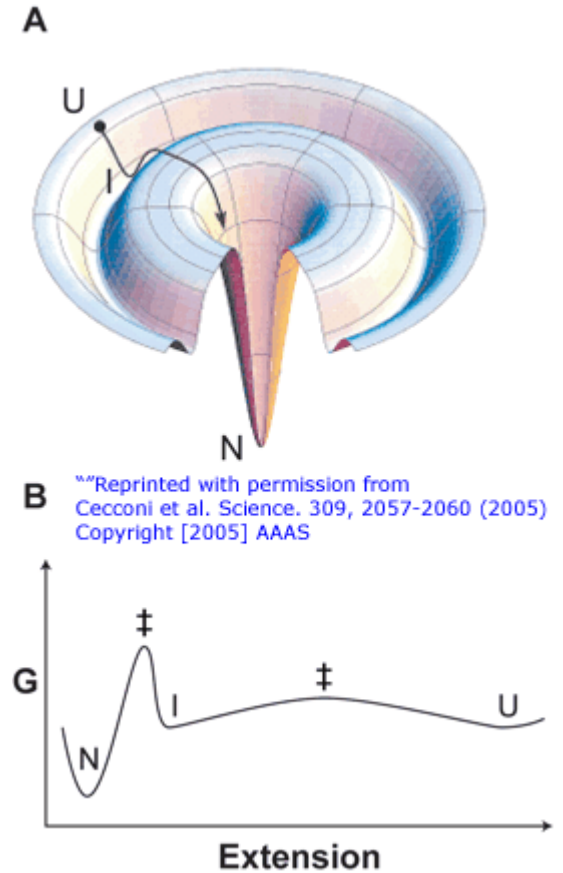
<http://www.sciencemag.org/content/309/5743/2057>



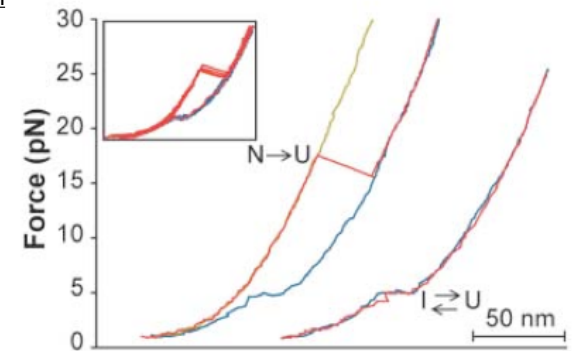
## RNase H Folding Transitions: Optical Trap



Blue: Stretch just DNA linker molecules  
 Red: Stretch DNA and Protein  
 Green: Release tension on Protein/DNA



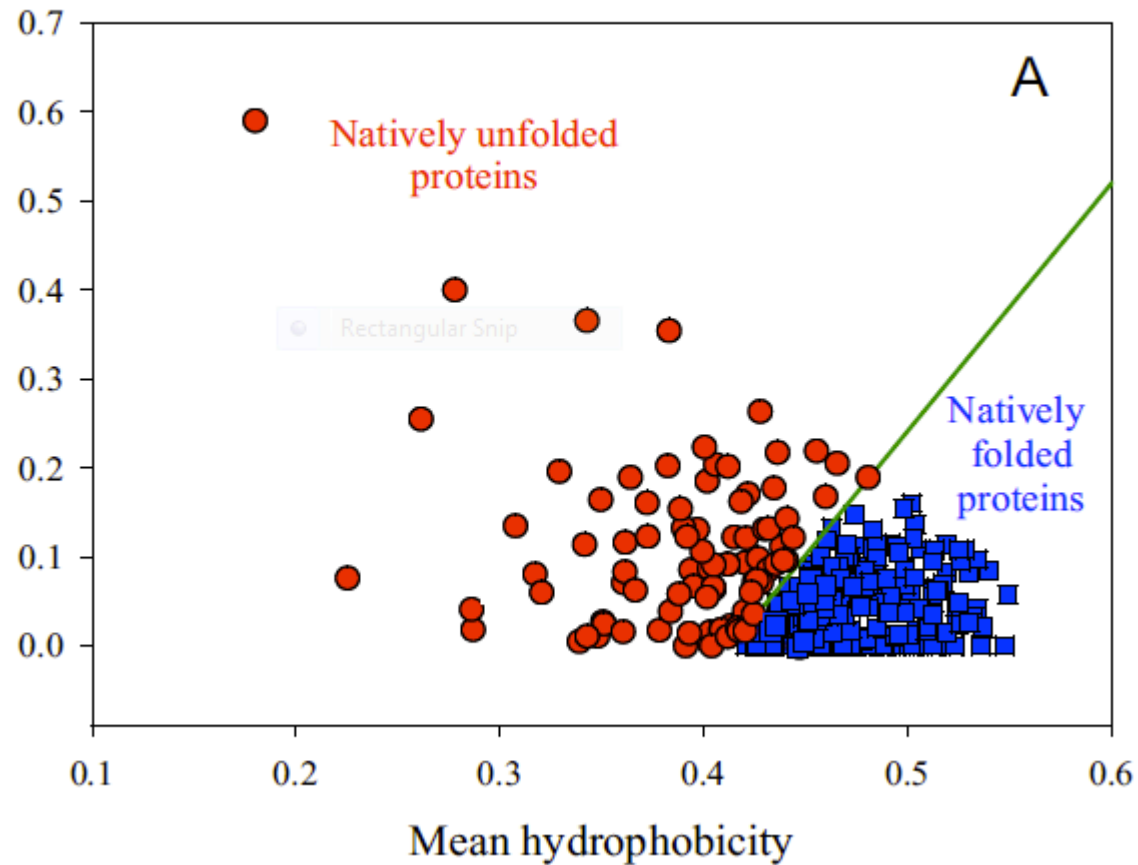
<http://employees.csbsju.edu/hjakubowski/classes/ch331/protstructure/olprotfold.html>



# Natively Unfolded Proteins

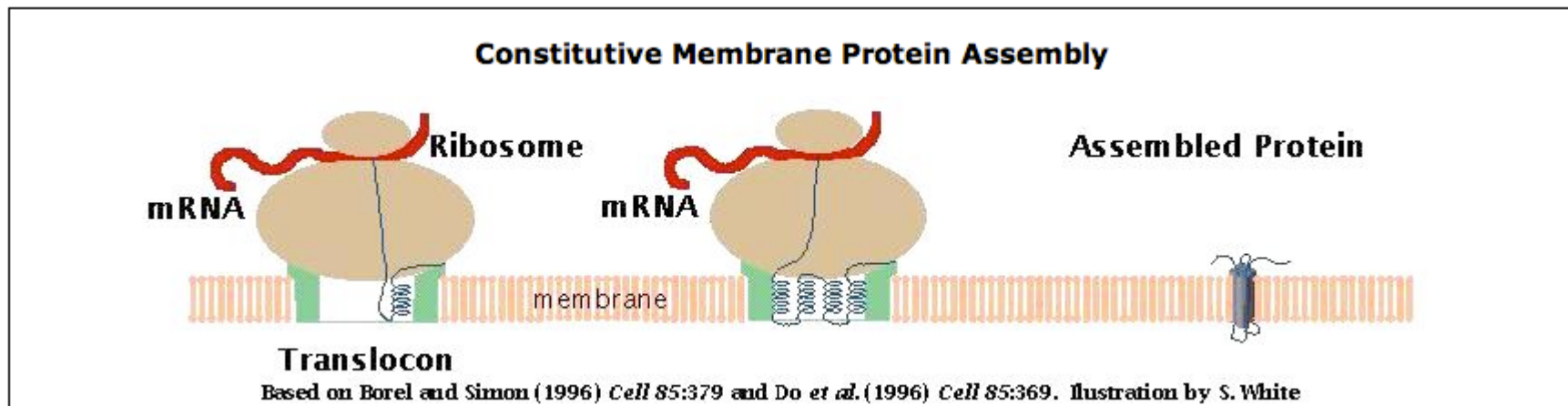
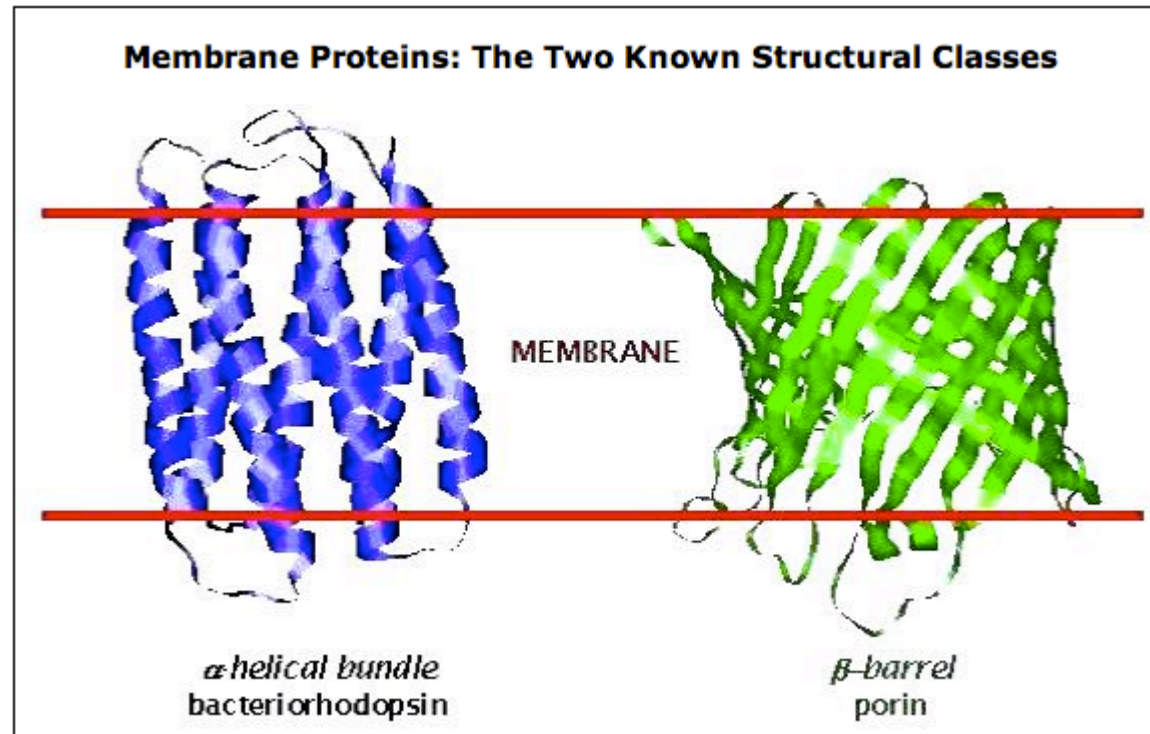
It's been estimated that over half of all native proteins have regions (greater than 30 amino acids) that are disordered, and upwards of 20% of proteins are completely disordered.

**Figure: Characteristics of Intrinsically Disordered Proteins**

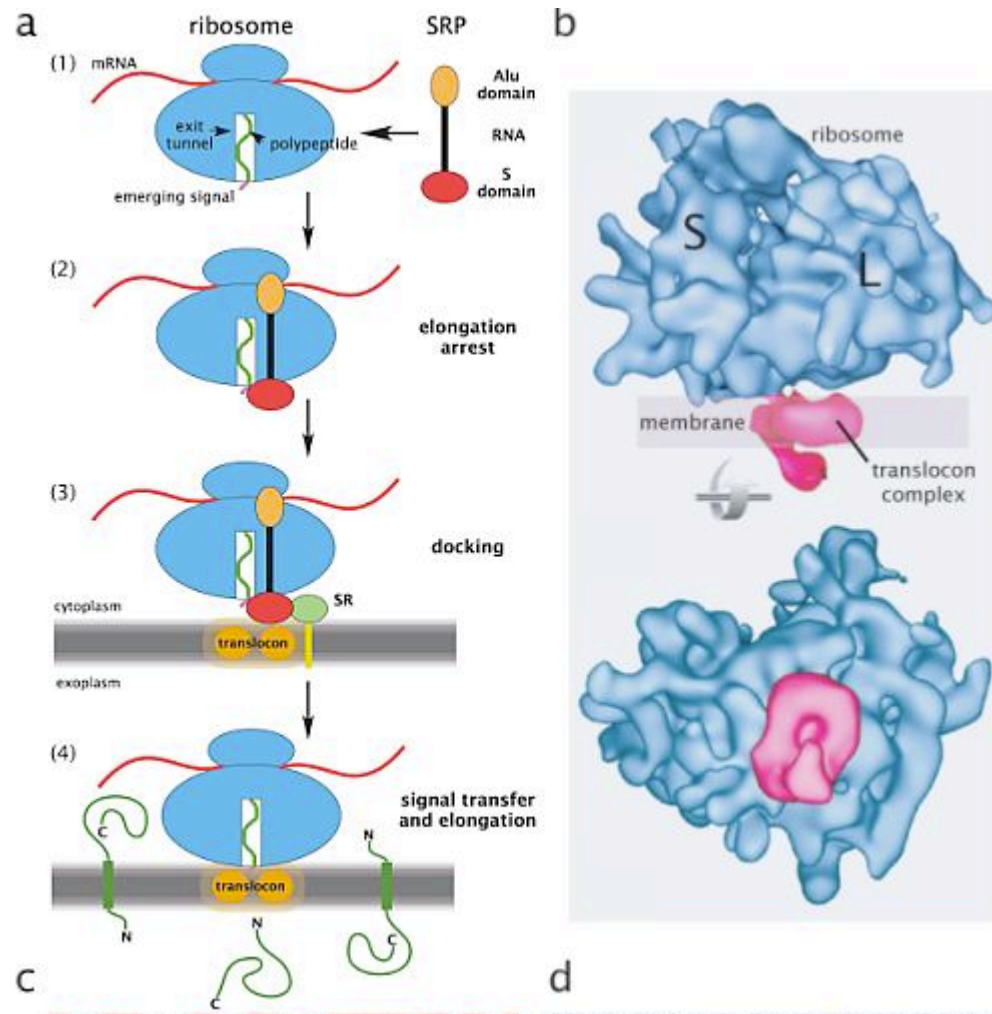




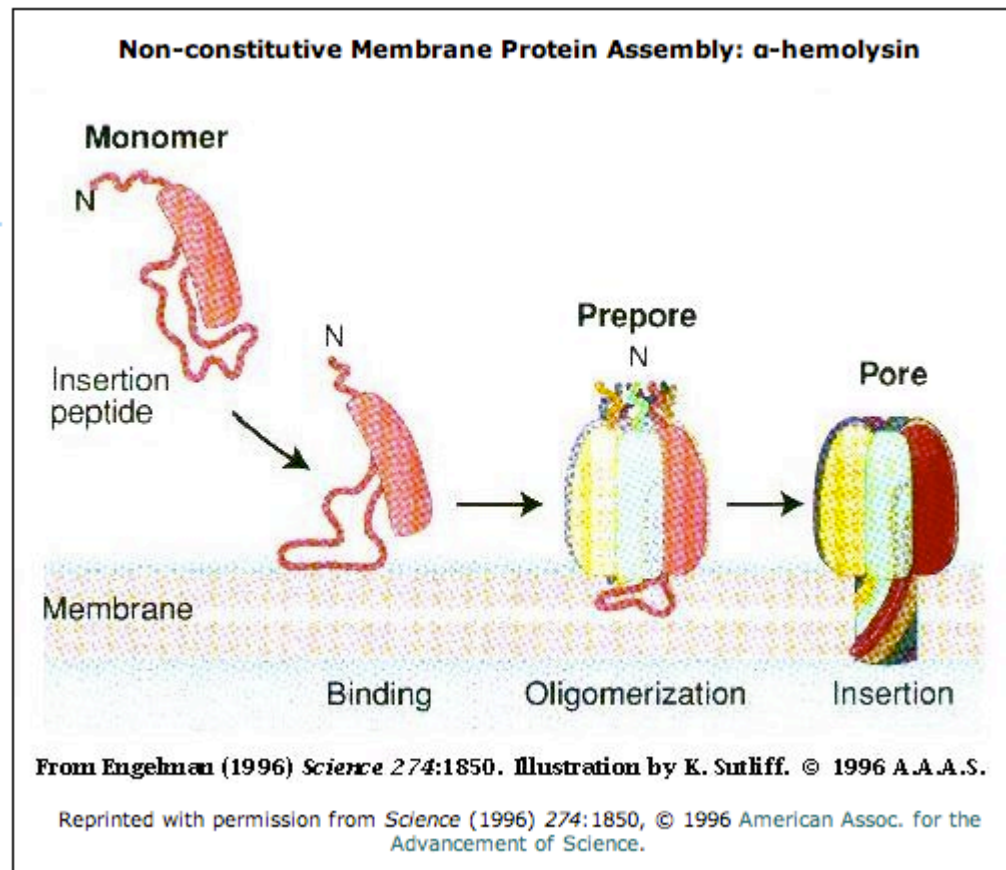
# Membrane Proteins

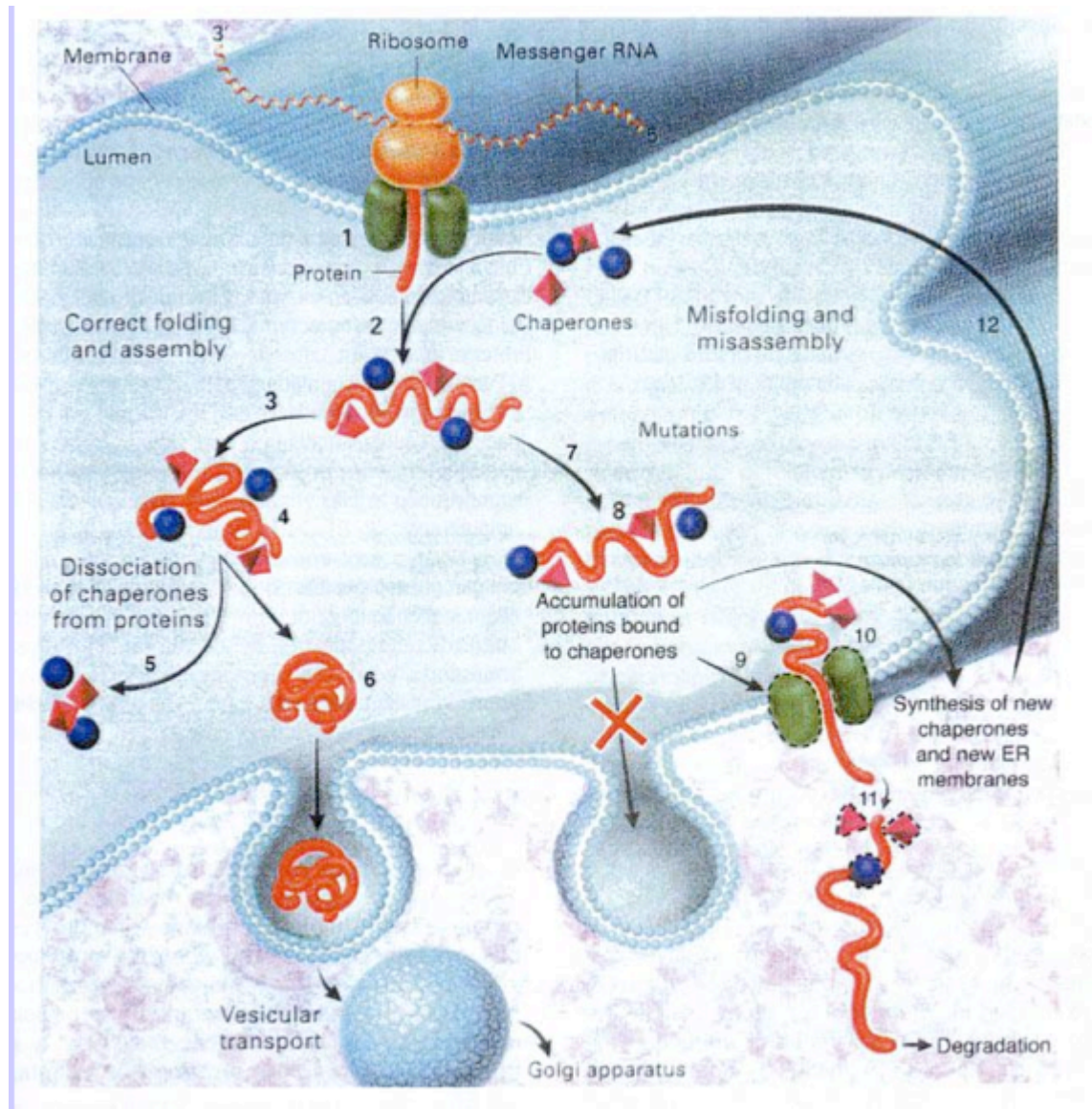


[http://blanco.biomol.uci.edu/mp\\_assembly.html](http://blanco.biomol.uci.edu/mp_assembly.html)



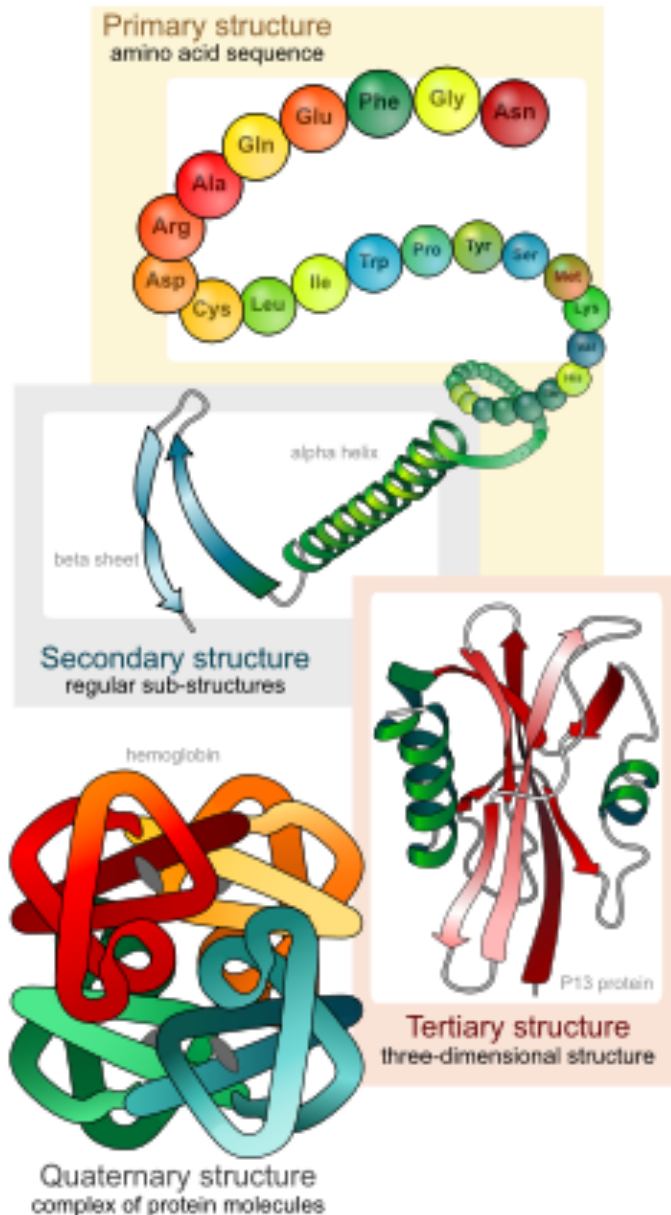
[http://blanco.biomol.uci.edu/translocon\\_machinery.html](http://blanco.biomol.uci.edu/translocon_machinery.html)





<http://www.portfolio.mvm.ed.ac.uk/studentwebs/session2/group5/introliz.htm>

# Quaternary Structures

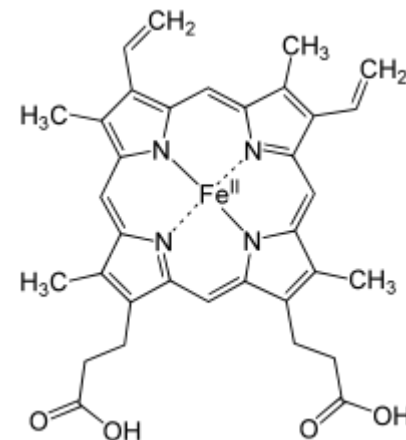


Electron transport chain is part of the ATP/ADP energy generation pathway for cells. This involves many tertiary protein structures. For instance, Complex III is a quaternary structure of 9 proteins.

[http://proteopedia.org/wiki/index.php/Complex\\_III\\_of\\_Electron\\_Transport\\_Chain](http://proteopedia.org/wiki/index.php/Complex_III_of_Electron_Transport_Chain)

[http://en.wikipedia.org/wiki/Electron\\_transport\\_chain](http://en.wikipedia.org/wiki/Electron_transport_chain)

## Heme B group



## Quaternary Structure Page

[http://proteopedia.org/wiki/index.php/Main\\_Page](http://proteopedia.org/wiki/index.php/Main_Page)

### Ribosome

<http://proteopedia.org/wiki/index.php/Ribosome>

### Role of Ribosome

<http://www.cytochemistry.net/cell-biology/ribosome.htm>

### Ribosome in Action

<http://www.youtube.com/watch?v=JmI8CFBWcDs>

### Poly(A) Polymerase

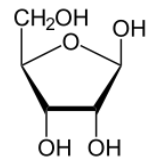
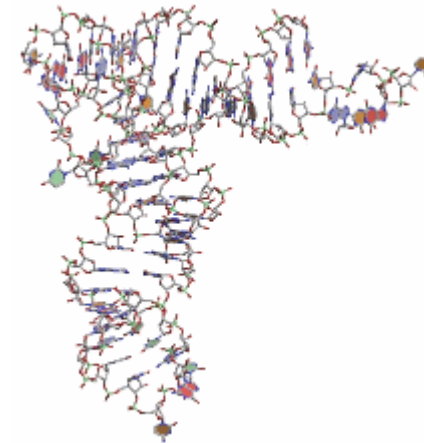
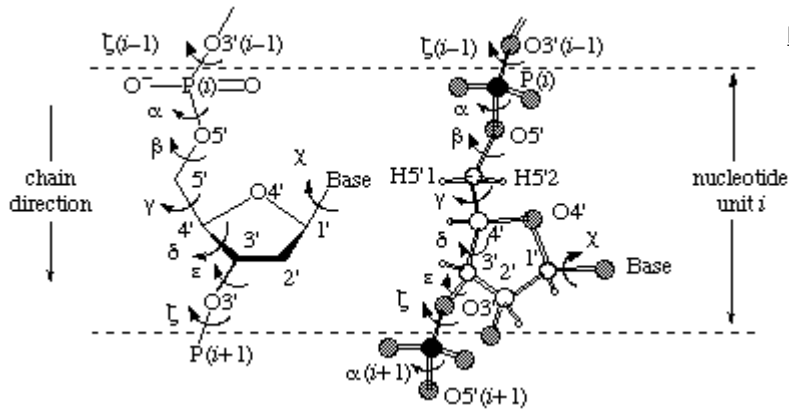
<http://proteopedia.org/wiki/index.php/2q66>

## DNA/Protein Quaternary Structures

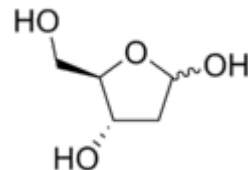
[http://www.biochem.ucl.ac.uk/bsm/prot\\_dna/prot\\_dna\\_cover.html](http://www.biochem.ucl.ac.uk/bsm/prot_dna/prot_dna_cover.html)

# RNA structure

<http://www.rnabase.org/primer/>

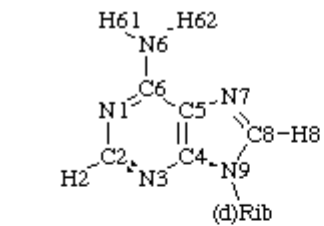


Ribose

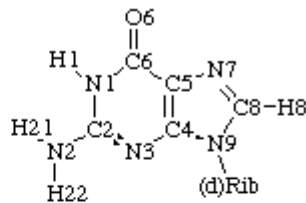


Deoxyribose

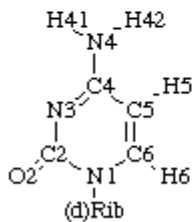
t-RNA (Folded Structure)



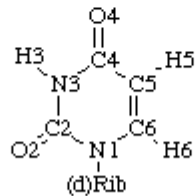
adenosine (and deoxyadenosine)



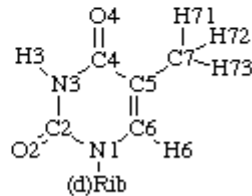
guanosine (and deoxyguanosine)



cytosine (and deoxycytosine)

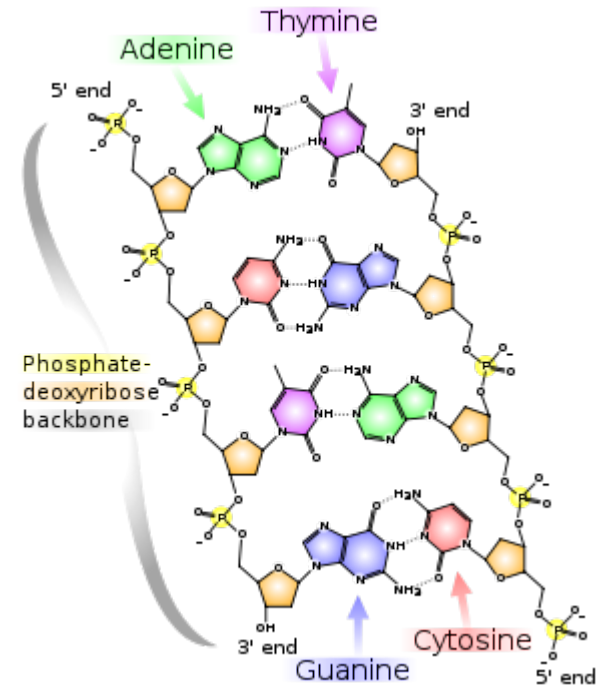


uridine (and deoxyuridine)



ribosylthymine (and thymidine)

DNA



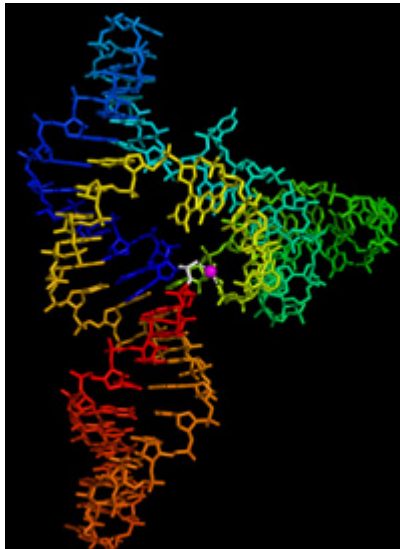


If it takes DNA/RNA to template a protein and proteins to make/control DNA/RNA  
Which came first Proteins or Nucleic Acids?

## RNA World Hypothesis:

[http://en.wikipedia.org/wiki/RNA\\_world\\_hypothesis](http://en.wikipedia.org/wiki/RNA_world_hypothesis)

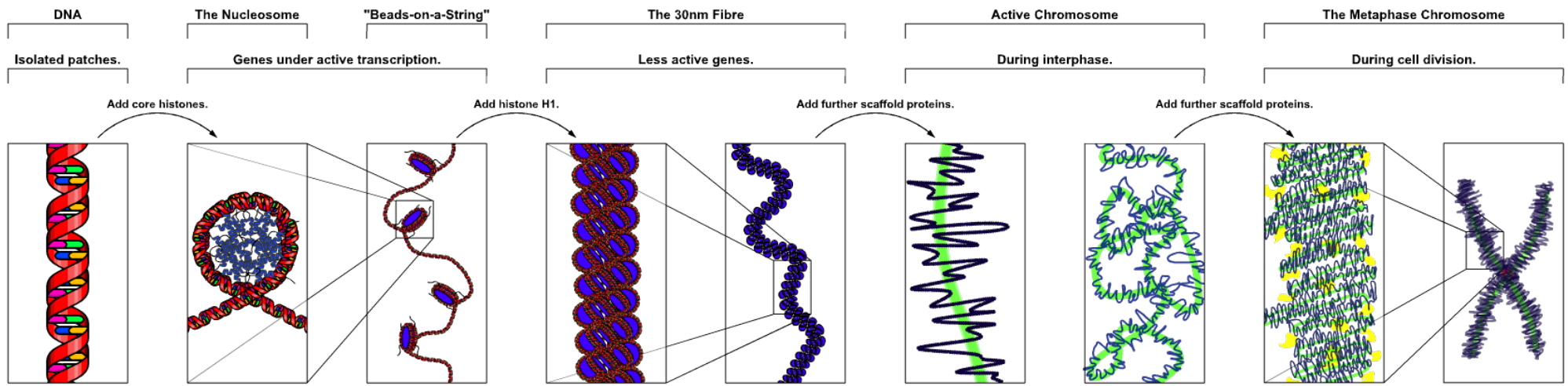
<http://exploringorigins.org/rna.html>

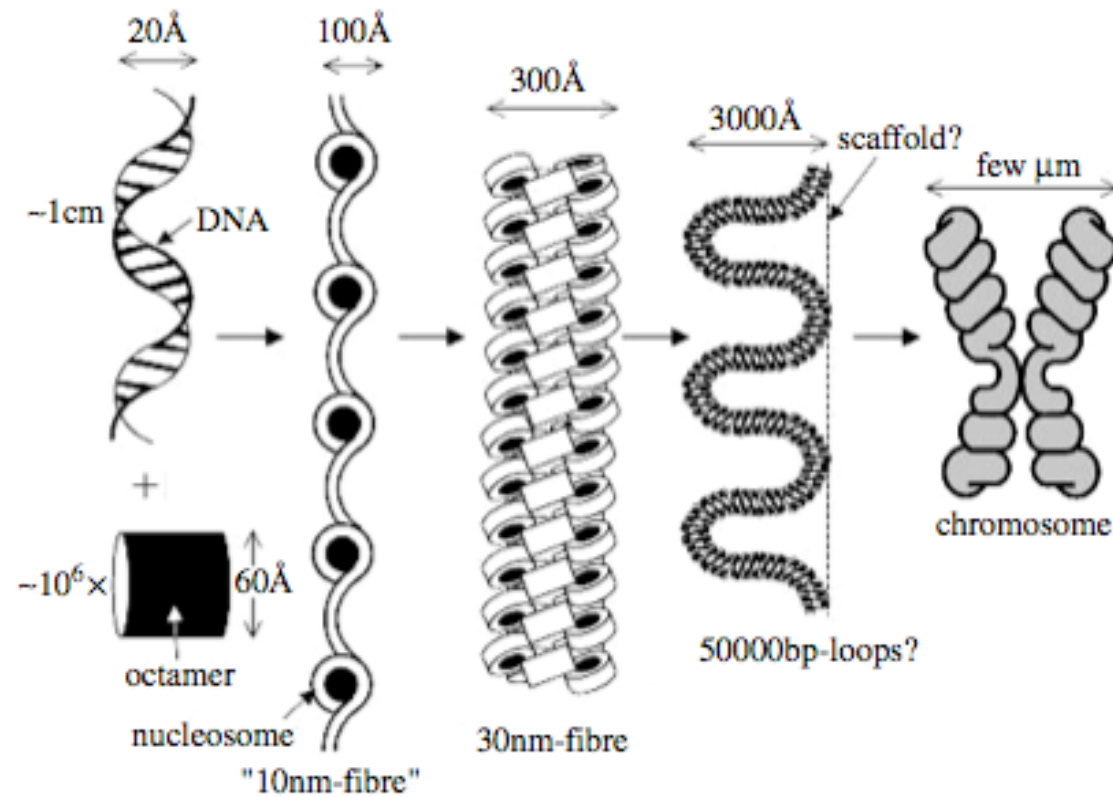


L1 Ligase Ribozyme

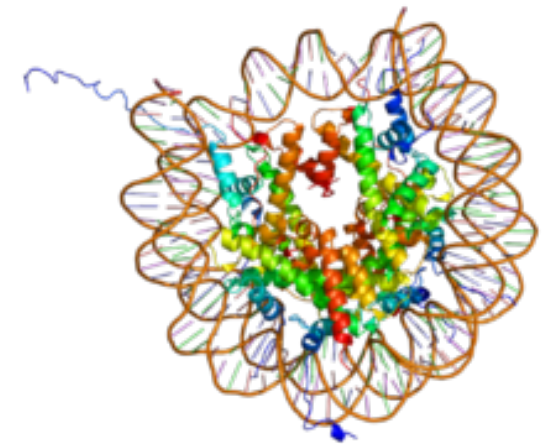


# Hierarchy of a Chromosome





## Core Histone



**Figure 1.** Steps of the DNA compaction into chromatin. The DNA molecule of length  $\sim 1\text{ cm}$  is compacted with the help of  $10^6$  histone octamers leading to a 10 000-fold reduction of its original length (see text for details).

It is instructive to draw a comparison between the structure and function of chromatin and that of a daily-life example: the library. As the nucleus stores a long one-dimensional string of bp, so the library contains a huge one-dimensional string of letters, the text written down in all of its books. A book like [1] contains  $\sim 10$  km of text, a library with 10 000 books stores roughly 100 000 km of text! How can the user find and retrieve the little piece of information of interest? The way this is handled is that the text is folded in a hierarchical fashion in lines, pages, books and shelves. This makes it relatively easy, with the help of a few markers, to find the corresponding text passage. Furthermore, all the text is stored in a dense fashion but the book of interest can be taken out of the shelve and opened at the appropriate page without perturbing the rest of the library. Apparently, the result of this hierarchical structure is a relatively high efficiency in storing a huge amount of information in a relatively small space and, at the same time, having high accessibility to it.

<http://www.eng.uc.edu/~gbeauca/Classes/MorphologyofComplexMaterials/Physics%20of%20Chromatin%20Schissel%202003.pdf>

