Dependencies of the Heat of Formation

Reference State: Elemental ground state at STP has an enthalpy of formation of 0 \( \text{N}_2, \text{O}_2, \text{He} \) etc.

<table>
<thead>
<tr>
<th>Solids: Standard state is pure solid at 298.15 K, 1 bar.</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \Delta H_{298.15} )</td>
</tr>
<tr>
<td>kJ/mol</td>
</tr>
<tr>
<td>--------------------------------------------------------</td>
</tr>
<tr>
<td>Carbon (graphite) (298-1300 K)</td>
</tr>
<tr>
<td>Calcium carbonate, ( \text{CaCO}_3 )</td>
</tr>
<tr>
<td>Calcium oxide, ( \text{CaO} )</td>
</tr>
<tr>
<td>Glucose</td>
</tr>
<tr>
<td>Miscellaneous Gases</td>
</tr>
<tr>
<td>Nitrous oxide</td>
</tr>
<tr>
<td>Oxygen</td>
</tr>
<tr>
<td>Hydrogen (equilibrium)</td>
</tr>
<tr>
<td>Nitrogen</td>
</tr>
<tr>
<td>Carbon monoxide</td>
</tr>
<tr>
<td>Sulfur dioxide</td>
</tr>
<tr>
<td>Sulfur trioxide</td>
</tr>
<tr>
<td>Nitric oxide</td>
</tr>
<tr>
<td>Helium-4</td>
</tr>
<tr>
<td>Argon</td>
</tr>
<tr>
<td>Fluorine</td>
</tr>
<tr>
<td>Chlorine</td>
</tr>
<tr>
<td>Neon</td>
</tr>
<tr>
<td>Krypton</td>
</tr>
<tr>
<td>Bromine</td>
</tr>
<tr>
<td>Xenon</td>
</tr>
</tbody>
</table>

Generally, energy is released on formation of a molecule from the elements if the molecule is stable, so the heat of formation is generally negative. For unstable molecules such as NO which is a radical formed at high temperatures, the heat of formation is positive (endothermic).
Ellingham Diagrams

![Ellingham Diagrams](image)

**FIG. 5.** Thermodynamic calculations in the form of an Ellingham diagram allow discussions on accessible alloys and metals. The lines which lie below the flame process operating line indicate accessible metals at the corresponding temperature (copper, cobalt, nickel, and iron above 1500°C). Others, such as cerium, manganese are not accessible in the current CO/H₂ system.

*Aerosol Science and Technology, 44:161–172, 2010*
Copyright © American Association for Aerosol Research
ISSN: 0278-6826 print / 1521-7388 online
DOI: 10.1080/02786820903449665

**Chemical Aerosol Engineering as a Novel Tool for Material Science: From Oxides to Salt and Metal Nanoparticles**

Evagelos K. Athanassiou, Robert N. Grass, and Wendelin J. Stark

*Institute for Chemical and Bioengineering, ETH Zurich, Zurich, Switzerland*
Relative magnitude of heat of formation from elements, oxides, heat of fusion, heat of transition

Table 7.1 Magnitudes of enthalpies of various reactions of a ternary oxide using Mg$_2$SiO$_4$ as an example (after Navrotsky [1]).

<table>
<thead>
<tr>
<th>Reaction</th>
<th>Enthalpy (kJ mol$^{-1}$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>2Mg(s) + Si(s) + 2O$_2$(g) = Mg$_2$SiO$_4$ (olivine)</td>
<td>-2170.41</td>
</tr>
<tr>
<td>2MgO + SiO$_2$(s) = Mg$_2$SiO$_4$ (olivine)</td>
<td>-56.61</td>
</tr>
<tr>
<td>Mg$_2$SiO$_4$ (olivine) = Mg$_2$SiO$_4$ (liq.)</td>
<td>114</td>
</tr>
<tr>
<td>Mg$_2$SiO$_4$ (olivine) = Mg$_2$SiO$_4$ ($\beta$)</td>
<td>29.9</td>
</tr>
<tr>
<td>Mg$_2$SiO$_4$ ($\beta$) = Mg$_2$SiO$_4$ (spinel)</td>
<td>9.1</td>
</tr>
</tbody>
</table>

Olivine

(a) Spinel

(b) $\beta$

Spinel
Heats of formation for various titanium oxides

Values are almost identical

**Figure 7.1** The Gibbs energies of formation of stoichiometric and non-stoichiometric compounds in the system Ti$_3$O$_5$–TiO$_2$ [4]. Composition given as mole fraction O.
Electronegativity, the ability of an atom to attract electrons in a bond
Linus Pauling
Factors involved in the heat of formation: electronegativity and atomic size

Figure 7.2 Schematic categorization of bonding in solids.
Energetics of compound formation

Hess’s Law

\[
\begin{align*}
M(s) + \frac{1}{2}X_2(g) &= MX(s) \\
\text{“Electron gain”}
\end{align*}
\]

e.g. molten Na and Cl\textsubscript{2} gas

**Figure 7.3** Thermodynamic cycle for the formation of MX(s).
Energetics of compound formation

\[
M(s) + \frac{1}{2}X_2(g) = MX(s)
\]

\[
\begin{align*}
M^+(g) + X^-(g) &= MX(s) & -\Delta_{\text{latt}}H_m \\
M(s) &= M(g) & \Delta_{\text{atom}}H_m \\
M(g) &= M^+(g) + e^-(g) & \Delta_{\text{ion}}H_m \\
\frac{1}{2}X_2(g) &= X(g) & \Delta_{\text{diss}}H_m \\
X(g) + e^- &= X^-(g) & \Delta_{\text{eg}}H_m
\end{align*}
\]

\[
\Delta_fH_m(MX) = -\Delta_{\text{latt}}H_m + \Delta_{\text{atom}}H_m + \Delta_{\text{ion}}H_m + \Delta_{\text{diss}}H_m + \Delta_{\text{eg}}H_m
\]

Figure 7.3 Thermodynamic cycle for the formation of MX(s).
Energetics of compound formation

\[ M^+(g) + X^-(g) = MX(s) \quad -\Delta_{latt} H_m \]

\[ \Delta_{latt} H_m = \Phi_{\text{electrostatic}} + \Phi_{\text{repulsion}} + \Phi_{\text{dispersion}} + \Phi_{\text{polarization}} + \Phi_{\text{crystal field}} \]

- Electrostatic attraction +-
- Electron electron repulsion
- Van der Waals or dispersion (d+ makes d- leads to net attraction)
- Polarization (shifting within compound of electrons)
- Crystal field effects
Electrostatic interactions in NaCl

Nearest neighbors of Na$^+$ and Cl.

Repulsive cationic terms, second nearest neighbors

Third nearest neighbors, attraction between M$^+$ and X$^-$

Generally:

$$\Phi_{\text{electrostatic}} = \frac{NM e^2 q_M q_X}{r_{MX}}$$

$M$ is the Madelung constant.
Repulsion and Dispersion Terms

Leonard-Jones (6-12) Potential

\[ V_{\text{LJ}}(r) = \frac{A}{r^{12}} - \frac{B}{r^{6}} \]

12 is repulsive since \( \frac{dE}{dr} = F \) is positive (guessed)
6 is van der Waals attractive force (calculated)

Buckingham Potential

\[ \Phi_{12}(r) = A \exp(-Br) - \frac{C}{r^{6}} \]

Exponential term works better for ceramics
Figure 7.4 Thermodynamic data needed in evaluation of the enthalpy of formation of MX(s). (a) Lattice enthalpy of sodium halides; (b) lattice enthalpy of alkali iodides; (c) electron gain and dissociation enthalpies of halides; (d) ionization and atomization enthalpies of alkali metals.
Trends in Enthalpy of Formation Alkali

\[ \Delta H_{\text{in MX}} = -\Delta_{\text{atom}} H_m + \Delta_{\text{ion}} H_m + \Delta_{\text{latt}} H_m + \Delta_{\text{gph}} H_m \]  

(7.8)

**Figure 7.5** Enthalpy of formation of binary compounds of the alkali metals.
“Extra electrons (12) are not screening the nuclear charge effectively, resulting in a much higher ionization enthalpy for the group 12 elements and a less negative enthalpy of formation for the group 12 compounds compared with the group 2 compounds.” (book)

Figure 7.6 Enthalpy of formation of group 2 and 12 dichlorides and difluorides.
Transition Metal Enthalpy of Formation
17

- p-orbitals: 6 valence electrons (more acidic to right)
- s-orbitals: 2 valence electrons (more basic to right)
- d-orbitals: 10 valence electrons
- Acidic (at high oxidation state)
- Transition Metals
- Basic (at low oxidation state)
- f-orbitals: 14 valence electrons
Hybridization schemes for the \( \sigma \)-bonding frameworks of different geometrical configurations

<table>
<thead>
<tr>
<th>Coordination number</th>
<th>Arrangement of donor atoms</th>
<th>Orbitals hybridized</th>
<th>Hybrid orbital description</th>
<th>Example</th>
</tr>
</thead>
<tbody>
<tr>
<td>2</td>
<td>Linear</td>
<td>( s, p_z )</td>
<td>( sp )</td>
<td>[Ag(NH(_3))(_2)](^+)</td>
</tr>
<tr>
<td>3</td>
<td>Trigonal planar</td>
<td>( s, p_x, p_y )</td>
<td>( sp^2 )</td>
<td>[HgI(_2)](^-)</td>
</tr>
<tr>
<td>4</td>
<td>Tetrahedral</td>
<td>( s, p_x, p_y, p_z )</td>
<td>( sp^3 )</td>
<td>[FeBr(_4)](^2-)</td>
</tr>
<tr>
<td>4</td>
<td>Square planar</td>
<td>( s, p_x, p_y, d_{x^2-y^2} )</td>
<td>( sp^3 d )</td>
<td>[Ni(CN)(_4)](^2-)</td>
</tr>
<tr>
<td>5</td>
<td>Trigonal bipyramidal</td>
<td>( s, p_x, p_y, p_z, d_z )</td>
<td>( sp^3 d )</td>
<td>[CuCl(_3)](^3+)</td>
</tr>
<tr>
<td>5</td>
<td>Square-based pyramidal</td>
<td>( s, p_x, p_y, p_z, d_{x^2-y^2} )</td>
<td>( sp^3 d )</td>
<td>[Ni(CN)(_3)](^3+)</td>
</tr>
<tr>
<td>6</td>
<td>Octahedral</td>
<td>( s, p_x, p_y, p_z, d_{x^2}, d_{x^2-y^2}, d_{y^2} )</td>
<td>( sp^3 d^2 )</td>
<td>[Co(NH(_3))(_6)](^3+)</td>
</tr>
<tr>
<td>6</td>
<td>Trigonal prismatic</td>
<td>( s, d_{x^2}, d_{y^2}, d_{x^2-y^2}, d_{z^2} )</td>
<td>( sd^5 ) or ( sp^3 d^2 )</td>
<td>[ZrMe(_6)](^2-)</td>
</tr>
<tr>
<td>7</td>
<td>Pentagonal bipyramidal</td>
<td>( s, p_x, p_y, p_z, d_{x^2}, d_{x^2-y^2}, d_{y^2} )</td>
<td>( sp^3 d^2 )</td>
<td>[V(CN)(_5)](^4-)</td>
</tr>
<tr>
<td>7</td>
<td>Monocapped trigonal prismatic</td>
<td>( s, p_x, p_y, p_z, d_{x^2}, d_{x^2-y^2}, d_{z^2} )</td>
<td>( sp^3 d^3 )</td>
<td>[NbF(_5)](^2-)</td>
</tr>
<tr>
<td>8</td>
<td>Cubic</td>
<td>( s, p_x, p_y, p_z, d_{x^2}, d_{x^2-y^2}, f_{xy} )</td>
<td>( sp^3 d^2 f )</td>
<td>[PaF(_6)](^3-)</td>
</tr>
<tr>
<td>8</td>
<td>Dodecahedral</td>
<td>( s, p_x, p_y, p_z, d_{x^2}, d_{x^2-y^2}, d_{y^2}, d_{z^2} )</td>
<td>( sp^3 d^4 )</td>
<td>[Mo(CN)(_6)](^4-)</td>
</tr>
<tr>
<td>8</td>
<td>Square antiprismatic</td>
<td>( s, p_x, p_y, p_z, d_{x^2}, d_{x^2-y^2}, d_{y^2}, d_{z^2} )</td>
<td>( sp^3 d^4 )</td>
<td>[TaF(_6)](^3-)</td>
</tr>
<tr>
<td>9</td>
<td>Tricapped trigonal prismatic</td>
<td>( s, p_x, p_y, p_z, d_{x^2}, d_{x^2-y^2}, d_{y^2}, d_{z^2} )</td>
<td>( sp^3 d^5 )</td>
<td>[ReH(_3)](^2-)</td>
</tr>
</tbody>
</table>

Electron Configuration in the Aufbau principle

\( s = 2 \)  
\( p = 6 \)  
\( d = 10 \)  
\( f = 14 \)  

14 valence electrons
Depending on the crystallographic environment the d-orbital energies split. This impacts the Enthalpy of Formation.

https://chem.libretexts.org/Bookshelves/Inorganic_Chemistry/Supplemental_Modules_and_Web_sites_(Inorganic_Chemistry)/Crystal_Field_Theory/Crystal_Field_Theory

Crystal Field Theory

\[ E \propto \frac{q_1 q_2}{r} \]

- \( E \) is the bond energy between the charges and
- \( q_1 \) and \( q_2 \) are the charges of the interacting ions and
- \( r \) is the distance separating them.

Figure 1: Distributing a charge of \(-6\) uniformly over a spherical surface surrounding a metal ion causes the energy of all five d orbitals to increase due to electrostatic repulsions, but the five d orbitals remain degenerate. Placing a charge of \(-1\) at each vertex of an octahedron causes the d orbitals to split into two groups with different energies: the \( d_{x^2-y^2} \) and \( d_{xy} \) orbitals increase in energy, while the \( d_{x^2} \), \( d_{y^2} \), and \( d_{z^2} \) orbitals decrease in energy. The average energy of the five d orbitals is the same as for a spherical distribution of a \(-6\) charge, however. Attractive electrostatic interactions between the negatively charged ligands and the positively charged metal ion (far right) cause all five d orbitals to decrease in energy but does not affect the splittings of the orbitals. The two \( e_g \) orbitals point directly at the six negatively charged ligands, which increases their energy compared with a spherical distribution of negative charge. In contrast, the three \( t_{2g} \) orbitals point between the negatively charged ligands, which decreases their energy compared with a spherical distribution of charge.

Ligands are classified as strong or weak based on the spectrochemical series:

\[
I^- < Br^- < Cl^- < SCN^- < F^- < OH^- < \text{ox}^2^- < \text{QNO}^- < \text{H}_2\text{O} < \text{SCN}^- < \text{EDTA}^4^- < \text{NH}_3 < \text{en} < \text{NO}_2^- < \text{CN}^- \]

Note that SCN\(^-\) and NO\(_2^-\) ligands are represented twice in the above spectrochemical series since there are two different Lewis base sites (e.g., free electron pairs to share) on each ligand (e.g., for the SCN\(^-\) ligand, the electron pair on the sulfur or the nitrogen can form the coordinate covalent bond to a metal). The specific atom that binds in such ligands is underlined.
Depending on the crystallographic environment the d-orbital energies split.
Depending on the crystalloigraphic environment the d-orbital energies split

Crystal Field Stabilization Energy (CFSE)

\[ \Delta_{\text{oct}} = 10Dq \]

\[ +0.6\Delta_{\text{oct}} = +6Dq \]

\[ -0.4\Delta_{\text{oct}} = -4Dq \]

\[ 3 \left( \frac{2}{5} \Delta_o \right) = 2 \left( \frac{3}{5} \Delta_o \right) \]
Depending on the crystallographic environment the d-orbital energies split.

The electronic absorption spectrum of \([\text{Ti(OH}_2\text{)}_6]^{3+}\) in aqueous solution.
Depending on the crystallographic environment the d-orbital energies split. This impacts the Enthalpy of Formation. 

Values of $\Delta_{\text{oct}}$ for some $d$-block metal complexes.
Depending on the crystallographic environment the d-orbital energies split. This impacts the Enthalpy of Formation.

https://chem.libretexts.org/Bookshelves/Inorganic_Chemistry/Supplemental_Modules_and_Web_sites_(Inorganic_Chemistry)/Crystal_Field_Theory/Crystal_Field_Theory

Figure 3: Spatial arrangement of ligands in the an octahedral ligand field with respect to the five d-orbitals.

- $d_{xy}$: lobes lie in-between the x and the y axes.
- $d_{xz}$: lobes lie in-between the x and the z axes.
- $d_{yz}$: lobes lie in-between the y and the z axes.
- $d_{x^2-y^2}$: lobes lie on the x and y axes.
- $d_{z^2}$: there are two lobes on the z axes and there is a donut shape ring that lies on the xy plane around the other two lobes.
Depending on the crystallographic environment the d-orbital energies split. This impacts the Enthalpy of Formation.

https://chem.libretexts.org/Bookshelves/Inorganic_Chemistry/Supplemental_Modules_and_Web_sites_(Inorganic_Chemistry)/Crystal_Field_Theory/Crystal_Field_Theory

![Figure 3: Spatial arrangement of ligands in an octahedral ligand field with respect to the five d-orbitals.](https://chem.libretexts.org/Bookshelves/Inorganic_Chemistry/Supplemental_Modules_and_Web_sites_(Inorganic_Chemistry)/Crystal_Field_Theory/Crystal_Field_Theory)

**Octahedral Complexes**

In an octahedral complex, there are six ligands attached to the central transition metal. The d-orbital splits into two different levels (Figure 4). The bottom three energy levels are named $d_{xy}$, $d_{xz}$, and $d_{yz}$ (collectively referred to as $t_{2g}$). The two upper energy levels are named $d_{x^2-y^2}$, and $d_{z^2}$ (collectively referred to as $e_g$).

![Figure 4](https://chem.libretexts.org/Bookshelves/Inorganic_Chemistry/Supplemental_Modules_and_Web_sites_(Inorganic_Chemistry)/Crystal_Field_Theory/Crystal_Field_Theory)

The reason they split is because of the electrostatic interactions between the electrons of the ligand and the lobes of the d-orbital. In an octahedral, the electrons are attracted to the axes. Any orbital that has a lobe on the axes moves to a higher energy level. This means that in an octahedral, the energy levels of $e_g$ are higher (0.6$\Delta$), while $t_{2g}$ is lower (0.4$\Delta$). The distance that the electrons have to move from $t_{2g}$ to $e_g$ and it dictates the energy that the complex will absorb from white light, which will determine the color. Whether the complex is paramagnetic or diamagnetic will be determined by the spin state. If there are unpaired electrons, the complex is paramagnetic; if all electrons are paired, the complex is diamagnetic.
Depending on the crystallographic environment the d-orbital energies split. The trend in values of $\Delta_{\text{oct}}$ for the complexes $[\text{M(NH}_3\text{)}_6]^{3+}$ where M = Co, Rh, Ir. Field strength increases as one proceeds down a column.

$\Delta_{\text{oct}}$

Mn(II) < Ni(II) < Co(II) < Fe(II) < Cr(III) < Co(III) < Ru(III) < Mo(III) < Rh(III) < Pd(II) < Ir(III) < Pt(IV)
Depending on the crystallographic environment the d-orbital energies split. This impacts the Enthalpy of Formation.

Values of $\Delta_{\text{oct}}$ for some $d$-block metal complexes.
Depending on the crystallographic environment the d-orbital energies split. This impacts the Enthalpy of Formation.

https://chem.libretexts.org/Bookshelves/Inorganic_Chemistry/Supplemental_Modules_and_Web_sites_(Inorganic_Chemistry)/Crystal_Field_Theory/Crystal_Field_Theory

**Tetrahedral Complexes**

In a tetrahedral complex, there are four ligands attached to the central metal. The d orbitals also split into two different energy levels. The top three consist of the \( d_{x^2-y^2} \), \( d_{xy} \), and \( d_{xz} \) orbitals. The bottom two consist of the \( d_{x^2-y^2} \) and \( d_{yz} \) orbitals. The reason for this is due to poor orbital overlap between the metal and the ligand orbitals. The orbitals are directed on the axes, while the ligands are not.

The difference in the splitting energy is tetrahedral splitting constant \((\Delta_t)\), which is less than \((\Delta_o)\) for the same ligands:

\[
\Delta_t = 0.44 \Delta_o \tag{2}
\]

Consequently, \(\Delta_t\) is typically smaller than the spin pairing energy, so tetrahedral complexes are usually **high spin**.
Depending on the crystallographic environment the d-orbital energies split. This impacts the Enthalpy of Formation.

https://chem.libretexts.org/Bookshelves/Inorganic_Chemistry/Supplemental_Modules_and_Web_sites_(Inorganic_Chemistry)/Crystal_Field_Theory/Crystal_Field_Theory

![Image](https://chem.libretexts.org/ContentImages/crystal_field_theory.png)

**Figure 3:** Spatial arrangement of ligands in the an octahedral ligand field with respect to the five d-orbitals.

**Square Planar Complexes**

In a square planar, there are four ligands as well. However, the difference is that the electrons of the ligands are only attracted to the $xy$ plane. Any orbital in the $xy$ plane has a higher energy level (Figure 6). There are four different energy levels for the square planar (from the highest energy level to the lowest energy level): $d_{x^2-r^2}$, $d_{xy}$, $d_{zd}$, and both $d_{xz}$ and $d_{yz}$.

![Image](https://chem.libretexts.org/ContentImages/crystal_field_theory_square_planner.png)

**Figure 6:** Splitting of the degenerate d-orbitals (without a ligand field) due to an square planar ligand field.

The splitting energy (from highest orbital to lowest orbital) is $\Delta_{sp}$ and tends to be larger than $\Delta_s$.

$$\Delta_{sp} = 1.74 \Delta_s \quad (3)$$

Moreover, $\Delta_{sp}$ is also larger than the pairing energy, so the square planar complexes are usually **low spin** complexes.
Depending on the crystallographic environment the d-orbital energies split.
Depending on the crystallographic environment the d-orbital energies split. This impacts the Enthalpy of Formation.

For the complex ion $[\text{Fe(OH)}_3]^3-$ determine the number of $d$ electrons for Fe, sketch the $d$-orbital energy levels and the distribution of $d$ electrons among them, list the number of lone electrons, and label whether the complex is paramagnetic or diamagnetic.

**Solution**

- **Step 1:** Determine the oxidation state of Fe. Here it is Fe$^{3+}$. Based on its electron configuration, Fe$^{3+}$ has 5 d-electrons.
- **Step 2:** Determine the geometry of the ion. Here it is an octahedral which means the energy splitting should look like:

  ![Energy Level Diagram](https://chem.libretexts.org/Bookshelves/Inorganic_Chemistry/Supplemental_Modules_and_Websites_(Inorganic_Chemistry)/Crystal_Field_Theory/Crystal_Field_Theory)

- **Step 3:** Determine whether the ligand induces a strong or weak field spin by looking at the spectrochemical series. $\text{Cl}^-$ is a weak field ligand (i.e., it induces high spin complexes). Therefore, electrons fill all orbitals before being paired.

  ![Spectrochemical Series](https://chem.libretexts.org/Bookshelves/Inorganic_Chemistry/Supplemental_Modules_and_Websites_(Inorganic_Chemistry)/Crystal_Field_Theory/Crystal_Field_Theory)

- **Step four:** Count the number of lone electrons. Here, there are 5 electrons.
- **Step five:** The five unpaired electrons means this complex ion is paramagnetic (and strongly so).

$$26-3 = 23 = 2+2+6+2+6+(5 \text{ d}). \text{ Unpaired electrons} \Rightarrow \text{Paramagnetic}$$
Depending on the crystallographic environment the d-orbital energies split. This impacts the Enthalpy of Formation.

A tetrahedral complex absorbs at 545 nm. What is the respective octahedral crystal field splitting ($\Delta_o$)? What is the color of the complex?

**Solution**

\[
\Delta_t = \frac{\hbar c}{\lambda}
\]
\[
= \frac{(6.626 \times 10^{-34} J \cdot s)(3 \times 10^8 m/s)}{545 \times 10^{-9} m}
\]
\[
= 3.65 \times 10^{-19} J
\]

However, the tetrahedral splitting ($\Delta_t$) is ~4/9 that of the octahedral splitting ($\Delta_o$).

\[
\Delta_t = 0.44\Delta_o
\]
\[
\Delta_o = \frac{\Delta_t}{0.44}
\]
\[
= \frac{3.65 \times 10^{-19} J}{0.44}
\]
\[
= 8.30 \times 10^{-18} J
\]

This is the energy needed to promote one electron in one complex. Often the crystal field splitting is given per mole, which requires this number to be multiplied by Avogadro’s Number ($6.022 \times 10^{23}$).

This complex appears red, since it absorbs in the complementary green color (determined via the color wheel).
Depending on the crystallographic environment the d-orbital energies split. This impacts the Enthalpy of Formation.

Crystal Field Effect

**Figure 7.8** $d$ level splitting for octahedral and tetrahedral crystal fields.
Crystal Field Stabilization Energy

Factors affecting the CFSE

First, note that the pairing energies for first-row transition metals are relatively constant.

Therefore, the difference between strong- and weak-field, or low and high-spin cases comes down to the magnitude of the crystal field splitting energy ($\Delta$).

1. **Geometry** is one factor, $\Delta_o$ is larger than $\Delta_t$

In almost all cases, the $\Delta_t$ is smaller than $P$ (pairing energy), so...

Tetrahedral complexes are always weak-field (high spin)

Square planar complexes may either be weak- or strong-field.

2. **Oxidation State of Metal Cation**

A greater charge on cation results in a greater magnitude of $\Delta$

Why? A greater charge pulls ligands more strongly towards the metal, therefore influences the splitting of the energy levels more.

3. **Size of the Metal Cation**

For second and third-row transition metal ions, $\Delta_o$ is larger than first-row.

Less steric hindrance between the ligands – better overlap w/orbitals.
Crystal Field Stabilization Energy

4. Identity of the ligands.

A spectrochemical series has been developed and sorted by the ability to split metal d-orbitals.

\[
\begin{align*}
\text{I}^- &< \text{Br}^- < \text{S}^{2-} < \text{Cl}^- < \text{SCN}^- < \text{NO}_3^- < \text{N}_3^- < \text{F}^- < \text{OH}^- < \text{C}_2\text{O}_4^{2-} < \text{H}_2\text{O} < \\
\text{NCS}^- &< \text{CH}_3\text{CN} < \text{py} \text{ (pyridine)} < \text{NH}_3 < \text{en} \text{ (ethylenediamine)} < \text{bipy} \text{ (2,2'}'\text{-bipyridine)} < \text{NO}_2^- < \text{PPh}_3 < \text{CN}^- < \text{CO}
\end{align*}
\]

As the ligands decrease in size, their ability to split the d-orbitals increases. The larger and bulkier ligands exhibit more steric hindrance and approach the metal less effectively.

One might expect that ligands with a negative charge might split the d-orbitals better, but this is not always the case. Notice that water is higher in the series than OH\(^-\), even though O on OH\(^-\) has a high concentration of charge.

The dipole moment of H\(_2\)O is larger than NH\(_3\), but NH\(_3\) is higher in the series. PPh\(_3\) is high in the series, but also very bulky, neutral and has a small dipole moment.
Transition metal lattice stabilization due to d-orbital splitting

First series chlorides, oxides and fluorides
Increasing d electrons

\[
\Delta_{f}H_{m}(MX) = -\Delta_{\text{latt}}H_{m} + \Delta_{\text{atom}}H_{m} + \Delta_{\text{ion}}H_{m} + \Delta_{\text{diss}}H_{m} + \Delta_{\text{eg}}H_{m}
\]

Figure 7.9 Thermodynamic data (b)–(d) needed in analysis of the enthalpy of formation of the binary transition metal compounds given in (a). (b) Atomization enthalpy of first series transition metals; (c) sum of first and second ionization enthalpies of first series transition metals; (d) derived lattice enthalpy of transition metal dihalides.

Crystal Field Stabilization due to d-orbital splitting (not for Ca, Mn, Zn)
Heat of Formation for Transition Metal Oxides in Different Oxidation States

Figure 7.11 Enthalpy of formation of binary oxides of the 3d transition metals (a) and (c). Frost diagram for the same 3d metals (b) Enthalpy of formation of binary oxides of the group 6 transition metals.
Acid-Base Model for Heat of Formation of Ternary Oxides

\[ AO + B_xO_y = AB_xO_{1+y} \]

**Basicity**

- \( MgO < CaO < SrO < BaO \)

**Acidity**

- \( Al < Si < P < S \)

**Na\(_2\)O**

- Base transfers its oxygen
- Si\(_2\)O\(_3\)

**SiO\(_2\)**

- Acid accepts oxygen
- Si\(_4\)O\(_{4-}\)

**SiNa\(_2\)O\(_3\)**

- Acidity
<table>
<thead>
<tr>
<th>Group</th>
<th>Period</th>
<th>Elements</th>
<th>d-orbitals</th>
<th>Acidic (at high oxidation state)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>1</td>
<td>H</td>
<td>10 valence electrons</td>
<td>5 B, 6 C, 7 N, 8 O, 9 F, 10 Ne</td>
</tr>
<tr>
<td>2</td>
<td>2</td>
<td>Li, Be</td>
<td></td>
<td>13 Al, 14 Si, 15 P, 16 S, 17 Cl, 18 Ar</td>
</tr>
<tr>
<td>3</td>
<td>3</td>
<td>Na, Mg</td>
<td></td>
<td></td>
</tr>
<tr>
<td>4</td>
<td>4</td>
<td>K, Ca, Sc</td>
<td></td>
<td></td>
</tr>
<tr>
<td>5</td>
<td>5</td>
<td>Rb, Sr, Y</td>
<td></td>
<td></td>
</tr>
<tr>
<td>6</td>
<td>6</td>
<td>Cs, Ba, La</td>
<td>Basic (at low oxidation state)</td>
<td>Transition Metals</td>
</tr>
<tr>
<td>7</td>
<td>7</td>
<td>Fr, Ra, Ac</td>
<td>f-orbitals</td>
<td>58 Ca, 59 Pr, 60 Nd, 61 Pm, 62 Sm, 63 Eu, 64 Gd, 65 Tb, 66 Dy, 67 Ho, 68 Er, 69 Tm, 70 Yb, 71 Lu</td>
</tr>
</tbody>
</table>

Basic s-orbitals 2 valence electrons (more basic to right)

Acidic p-orbitals 6 valence electrons (more acidic to right)
**Figure 7.14** Enthalpy of formation of selected ternary oxides from their binary constituents.
Figure 7.15  (a) Enthalpy of formation of ternary oxides and nitrides from their binary constituent compounds as a function of the ratio of ionic potential \( \frac{e}{\text{ionic radius (Å)}} \). Reprinted with permission from [16] Copyright (1997) American Chemical Society. (b) Gibbs energy of the oxide–sulfide equilibrium for group 1 and 2 metals at 1773 K as a function of the optical basicity of the metal.
Atomic Size

Perovskite structure
Calcium titanate CaTiO$_3$
Embed cations in the structure for engineered properties
One is solar energy absorption in Graetzel cells
These are the most promising low-temperature formation PV devices
(silicon solar cells require high temperature reduction of silica and chemical purification)

Cubic/Orthorhombic-like structure
Can accommodate many transition metals
ABX$_3$
A is much larger than B cations, X is anion (oxide)
B has 6-fold coordination surrounded by octahedron of anions
A has 12-fold cubahedral coordination

Red O$^{2-}$
Blue Ti$^{4+}$
Green Ca$^{2+}$ or Ba$^{2+}$
A is simple cubic
With O in the face center positions
And B in the body center positions

\[ t = \frac{r_{AO}}{\sqrt{2r_{BO}}} = \frac{r_A + r_O}{\sqrt{2(r_B + r_O)}} \]

\[ 0.8 < t < 1.1 \]

**Figure 7.16** The perovskite-type structure. Small black circles represent the B atom, large grey circles represent O atoms and open circles represent the A atom.
Figure 7.16 The perovskite-type structure. Small black circles represent the B atom, large grey circles represent O atoms and open circles represent the A atom.

\[ t = \frac{r_{AO}}{\sqrt{2}r_{BO}} = \frac{r_A + r_O}{\sqrt{2}(r_B + r_O)} \]

Figure 7.17 Enthalpy of formation of selected perovskite-type oxides as a function of the tolerance factor. Main figure show data for perovskites where the A atom is a Group 2 element and B is a d or f element that readily takes a tetravalent state [19, 20]. The insert shows enthalpies of formation of perovskite-type oxides where the A atom is a trivalent lanthanide metal [21] or a divalent alkaline earth metal [22] whereas the B atom is a late transition metal atom or Ga/Al.
Methyl Ammonium Lead Halide
Schematic of a sensitized perovskite solar cell in which the active layer consist of a layer of mesoporous TiO$_2$ which is coated with the perovskite absorber. The active layer is contacted with an n-type material for electron extraction and a p-type material for hole extraction. b) Schematic of a thin-film perovskite solar cell. In this architecture in which just a flat layer of perovskite is sandwiched between two selective contacts. c) Charge generation and extraction in the sensitized architecture. After light absorption in the perovskite absorber the photogenerated electron is injected into the mesoporous TiO$_2$ through which it is extracted. The concomitantly generated hole is transferred to the p-type material. d) Charge generation and extraction in the thin-film architecture. After light absorption both charge generation as well as charge extraction occurs in the perovskite layer.
spiro Ometad p-type semi-conductor
Enthalpy of Formation versus Number of Valence Electrons

Figure 7.18 Enthalpy of formation of binary carbides and diborides [25, 26] as a function of the average number of valence electrons per atom.
Zeolites (Natural are aluminosilicate rocks, synthetic can be a variety of materials often based on SiO$_2$)

Microscopic structure of a zeolite (mordenite) framework, assembled from tetrahedra. Sodium is present as an extra-framework cation (in green).

Can form meso or micro pores (colloidal- or nano-scale) (These are terms from gas adsorption field.)
Synthetic Zeolites can have meso (colloidal) or micro (nano) pores depending on the templating material and synthesis conditions. Usually start with TEOS and a surfactant or block copolymer.

Reference 29

Figure 1. Possibilities for silicate self-assembly in hydrothermal syntheses.

Figure 5. Configuration loops present in zeolites.
Surface effect as we saw earlier except that this is on a molecular/nano scale

Enthalpy relative to quartz

Figure 7.19 Enthalpy of transition from the stable polymorph versus volume correlations for micro- and mesoporous SiO₂ and AlPO₄ materials [29, 34].
Energy of Formation for Substitutional Solid Solutions

Atomic Radii => Volume of compounds
    Hume-Rothery Rule limited solubility if size difference exceeds 15%
Electronegativity
    Large difference in binary system leads to negative enthalpy of mixing Pd-Zr and is small for systems with low or no electronegativity and size difference Ti-Zr
Valence electron density
Binary components have the same crystal structure

Large enthalpy of mixing is related to large number of intermetallic phases

Elastic contribution to the enthalpy of mixing, small mixes well with large

\[ \Delta_{\text{mix}} H_m = x_A x_B c_A \frac{\Delta V^2}{3V_A} + x_B x_A c_B \frac{\Delta V^2}{3V_B} \]

\( c_i \) are constants \( x_i \) mole fractions \( V \) molar volumes
Sub-regular solution model
Figure 7.21 Enthalpies of mixing of selected NaCl-type systems involving the alkali earth oxides. The solid and dashed lines show scaling with the volume mismatch and with the square of the volume mismatch, respectively.
Energy of Formation for Interstitial Solid Solutions

Elastic interactions
Electronic interactions

Gas solubility in metals
Temperature
Pressure solubility for $H_2$: $x \sim \sqrt{p}$

$$M + \frac{x}{2}H_2(g) = MH_x$$

Sievert's Law
Solubility of gases in metals

Figure 7.22 Enthalpy of solution of hydrogen in transition metals at infinite dilution [45].
55 kJ/mole difference in formation enthalpy
Reduction temperature is 600K higher for hexagonal
Cubic reduced SrMnO_{2.5} is more stable
Octahedral corners shared in cubic, faces shared in hexagonal
High vacancies in faces make reduced hexagonal unfavorable

Figure 7.23 Connectivity of transition metal BO$_6$ octahedra in (a) cubic and (b) hexagonal perovskite SrMnO$_3$. 
Liquid-Liquid Miscibility

Mixing of acidic (SiO$_2$) and Basic (CaO) oxides Si$^{4+}$ has coordination number 4 and Ca$^{2+}$ has 6 SiO$_2$ mixes well with CaO but CaO has a harder time mixing with SiO$_2$

Increasing basicity

Ortho-silicate Ca$_2$SiO$_4$

$\text{ZrF}_4$ strong acid

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure.png}
\caption{Enthalpy of mixing of (a) binary silicate [48] (reprinted by permission of A. Navrotsky) and (b) fluoride systems [49].}
\end{figure}
Liquid Salt Mixtures

Size parameter, \( d = \frac{d_A - d_B}{d_A + d_B} \)

Common Anions mix with negative enthalpy of mixing
Common cations do not mix due to anion-anion repulsion
Conformational Enthalpy of Polymers

The Rotational Isomeric State Model of Volkenstein and Paul Flory (Nobel Prize)

Carbon has a tetrahedral bonding arrangement
For a chain of carbon, the two side groups interact with the side groups of neighboring carbons

For Butene

“Trans” is sterically the most favorable arrangement
“Gauche +” and “Gauche -” are less favorable

The Boltzmann equation gives the probability of a particular conformation, \( Z \) is the partition function or the sum of all the different Boltzmann expressions in an ensemble

\[
P(\varphi_i) = \frac{\exp(-E(\varphi_i)/kT)}{Z}
\]

\[
Z = \sum_i e^{-\beta E_i}
\]
Conformational Enthalpy of Polymers

The Rotational Isomeric State Model of Volkenstein and Paul Flory (Nobel Prize)

Carbon has a tetrahedral bonding arrangement
For a chain of carbon, the two side groups interact with the side groups of neighboring carbons

“Trans” is sterically the most favorable arrangement
“Gauche +” and “Gauche -” are less favorable

The Boltzmann equation gives the probability of a particular conformation, $Z$ is the partition function or the sum of all the different Boltzmann expressions in an ensemble

$$P(\varphi_i) = \frac{\exp(-E(\varphi_i)/kT)}{Z}$$

$$Z = \sum_i e^{-\beta E_i}$$
Conformational Enthalpy of Polymers

The Rotational Isomeric State Model of Volkenstein and Paul Flory (Nobel Prize)

Carbon has a tetrahedral bonding arrangement
For a chain of carbon the two side groups interact with the side groups of neighboring carbons

For Butene

“Trans” is sterically the most favorable arrangement
“Gauche +” and “Gauche -” are less favorable

The Boltzmann equation gives the probability of a particular conformation, $Z$ is the partition function or the sum of all of the different Boltzmann expressions in an ensemble

$$P(\varphi_i) = \frac{\exp(-E(\varphi_i)/kT)}{Z}$$

$$Z = \sum_i e^{-\beta E_i}$$
Conformational Energy of Polymers

The Rotational Isomeric State Model of Volkenstein and Paul Flory (Nobel Prize)

Carbon has a tetrahedral bonding arrangement
For a chain of carbon, the two side groups interact with the side groups of neighboring carbons

For Butene

\[ Z = 1 + \exp\left(-\frac{E_{g^+}}{kT}\right) + \exp\left(-\frac{E_{g^-}}{kT}\right) = 1 + 2\sigma \]

**Helmholtz Free Energy and Entropy**

\[ F_P = -kT \cdot \ln Z ; \quad S_P = -\frac{\partial F_P}{\partial T} \]

Boltzmann equation where \( Z \) is number of states (which depend on temperature and energy barriers)

**Internal Energy**

\[ U = F_P + S_P T \]

-SUV
-H A(F)
-pGT
Conformational Enthalpy of Polymers

The Rotational Isomeric State Model of Volkenstein and Paul Flory (Nobel Prize)

For a polymer with N carbons there are N-2 covalent bonds. The number of discrete conformation states per chain is $n^{N-2}$ where n is the number of discrete rotational states for the chain, ttt, g$^g$g$^g$g$^g$,$g^g$$^g$g$^g$g$^g$,$g^g$g$^g$ttt, etc. for N = 4; $N_1$=1, $N_4$=4, etc. assuming no end effects.

$$Z = \sum_{\{N_\eta\}} \frac{(N - 2)!}{N_1! \ldots N_v!} \exp(-N_1 E(\varphi_1)/kT) \ldots \exp(-N_v E(\varphi_v)/kT)$$

Average rotational angle

$$\langle \cos \varphi \rangle = \frac{\sum_{i=1}^{\nu} \exp(-E(\varphi_i)/kT) \cos \varphi_i}{\sum_{i=1}^{\nu} \exp(-E(\varphi_i)/kT)} = \frac{1 - \sigma}{1 + 2\sigma}$$

Characteristic Ratio

Characteristic Ratio

$C_\infty = \lim_{N \to \infty} \frac{\langle r^2 \rangle_0}{N l^2} = \frac{(1 + \cos \theta)(1 + \langle \cos \varphi \rangle)}{(1 - \cos \theta)(1 - \langle \cos \varphi \rangle)}$

$0$ is the bond angle

$180^\circ - 109^\circ = 71^\circ$

$E_{g^+} = 2100 \text{ J/mole}$

$C_\infty = 3.6$

Exp. 6.7