# Molecular Dynamics of Polymyrcene: Rheology and Broadband Dielectric Spectroscopy on a Stockmayer Type A Polymer 

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#### Abstract

Molecular dynamics of polymyrcene (PM) covering a wide range of molecular weights from $6.7 \times 10^{3} \leq M_{\mathrm{w}} \leq 3.47 \times 10^{5} \mathrm{~g} / \mathrm{mol}$ (weight-average molecular weight $M_{\mathrm{w}}$ ) with a molar mass dispersity $Đ \leq 1.16$ were investigated by oscillatory shear rheology and broadband dielectric spectroscopy. The analysis of the zero-shear viscosity $\left(\eta_{0}\right)$ versus molecular weight in a double-logarithmic plot reveals a scaling exponent of $\sim 1.2$ below the critical molecular weight and $\sim 3.7$ above a critical molecular weight of $M_{c} \cong 4.4 \times 10^{4} \mathrm{~g} / \mathrm{mol}$. However, at molecular weights greater than the reptation molecular weight $M_{\mathrm{r}}$, a molecular weight substantially larger than the entanglement molecular weight $M_{e}$, the zero shear viscosity scaling decreases. A scaling of $\eta_{0} \propto M^{3.0}$, which might be attributed to a pure tubereptation behavior, was found. The exponent of 1.2 is attributed to a Rouse-like dynamic and  is interpreted in terms of PM's bottlebrush-like nature arising from tightly packed C6/C8 pendant groups. Dielectric spectroscopy measurements revealed two relaxation processes typical for fully amorphous glassy polymers: The first is a segmental mode process, with a dynamic glass transition process $(\alpha)$, due to the segmental motions and the second one is a local relaxation process in the glassy state $(\beta)$. Additionally, above the glass transition temperature at low frequency, another relaxation process was observed, which appears to be the normal mode process ( n ) due to the fluctuation of the end-to-end vector. This polymer is assigned to be a new Stockmayer type A polymer, whose normal mode relaxation is strongly dependent on its molecular weight. These findings allow for the rare possibility to explore the global dynamics of PM by using both oscillatory shear rheology and broadband dielectric spectroscopy methods over a wide range of temperatures to investigate molecular dynamics using the time-temperature superposition principle.


## - INTRODUCTION

Today there is a growing interest in modern polymer chemistry toward the development of bio-based and biocompatible polymers as well as renewable alternatives to petrochemicalbased materials. ${ }^{1-5}$ One of the most used bio-based polymers is polyisoprene, frequently applied in the rubber industry as natural rubber. In addition to cis-1,4-polyisoprene, natural rubber, attractive renewable feedstocks include the family of acyclic terpenes as monomers (especially monoterpenes (C10) and sesquiterpenes (C15)), which offer an extensive variety of chemical structures. ${ }^{6-8}$ Among these, 7-methyl-3-methylene-octa-1,6-diene, $\mathrm{C}_{10} \mathrm{H}_{16}$, or $\beta$-myrcene can be a further promising bio-based alternative as monomers for specific applications, e.g., in rubber science due to its low glass transition temperature $T_{g}$ (see Table 1) and thus deserves further investigation. To our knowledge, the polymerization of myrcene was first described as early as 1913, but the polymer itself was not investigated in terms of polymer physics. ${ }^{9}$ Polymyrcene (PM; see Figure 1) or its derivatives may replace petrochemically sourced polymers or shares of such polymers, for example, the soft block of thermoplastic elastomers. ${ }^{10-12}$ As one example, $\beta$-myrcene can be naturally found in bay leaves, hop, wild thyme, and ylang ylang fruits and is produced on a large scale as one of the products of the pyrolysis of turpentine oil at $450-600{ }^{\circ} \mathrm{C}$ ( $\approx 37000 \mathrm{t} /$ year) $){ }^{13,14}$ Because $\beta$-myrcene possesses an anioni-

Table 1. Weight-Average Molecular Weights $M_{w}$, Dispersity $Ð$ as Determined by SEC, and Glass Transition Temperatures from DSC, Rheological Measurements (LVE), and Broadband Dielectric Spectroscopy (BDS) ${ }^{a}$

| sample ID | $M_{\mathrm{w}}(\mathrm{g} / \mathrm{mol})$ | $Đ$ | $T_{\mathrm{g}, \text { DSC }}(\mathrm{K})$ | $T_{\mathrm{g}, \mathrm{LVE}}(\mathrm{K})$ | $T_{\mathrm{g}, \mathrm{BDS}}(\mathrm{K})$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| PM6.7 | 6700 | 1.14 | 205 | 206 | 205 |
| PM10.7 | 10700 | 1.11 | 205 | 205 | 206 |
| PM11.6 | 11600 | 1.11 | 207 | 208 | 209 |
| PM36.6 | 36600 | 1.11 | 208 | 208 | 209 |
| PM42.9 | 42900 | 1.13 | 208 | 208 | 208 |
| PM74.1 | 74100 | 1.12 | 207 | 208 | 208 |
| PM85.6 | 85600 | 1.12 | 208 | 208 | 208 |
| PM115.9 | 115900 | 1.13 | 208 | 209 | 209 |
| PM155.1 | 155100 | 1.13 | 208 | 208 | 208 |
| PM192 | 192000 | 1.12 | 208 | 209 | 209 |
| PM347.7 | 347700 | 1.16 | 208 | 208 | 209 |

${ }^{a}$ See the text below for details about the $T_{\mathrm{g}}$ determination.

[^0]


Figure 1. Anionic polymerization of myrcene in cyclohexane using secBuLi as an initiator. Under these experimental conditions more than 90 $\mathrm{mol} \%$ of the 1,4 -isomer was obtained (determined by ${ }^{1} \mathrm{H}$ NMR).
cally polymerizable conjugated diene structure, linear backbone polymyrcene with a high content of cis-1,4 units and a narrow molecular weight distribution can be obtained by anionic polymerization if nonpolar solvents are used (see Figure 1). ${ }^{5,15-17}$ Additionally, the C-C double bonds of the side groups make this polymer interesting for further functionalization. ${ }^{10}$ Similar to polyfarnesene (PF; see Figure S1 in the Supporting Information), ${ }^{8}$ PM adopts a bottlebrush-like structure with two or four carbon atoms in the backbone but with shorter C6 and C8 tightly spaced side chains (see the scheme in Figure 1 or Figure S1), where the side arms are not entangled due to their small size. ${ }^{18}$ Additionally, similar to the structure of cis-1,4-polyisoprene or cis-1,4-polyfarnesene, PM possesses components of the repeating unit electrical dipole moment parallel along and perpendicular to the main chain, which can be classified as Stockmayer type A and Stockmayer type B dipoles, respectively. ${ }^{19}$ The polarization in an electrical field, which is the sum of the dipole moments of individual monomer units, gives information about the end-to-end vector of the whole polymer chain. ${ }^{20}$ The fluctuations of the end-to-end vector allow to investigate the global chain dynamics, which are also reflected in the terminal regime of temperature-dependent master curves determined in oscillatory shear rheological measurements. ${ }^{21-23}$
This article represents a detailed study of the molecular dynamics of polymyrcene with different, defined molecular weights, which is crucial for a correlation of molecular weight and material properties, analyzed by a combination of rheological and dielectrical measurements. ${ }^{9}$

## - EXPERIMENTAL SECTION

Materials and Methods. Secondary butyllithium (sec-BuLi, 1.4 $\mathrm{mol} / \mathrm{L}$ in hexane, Sigma-Aldrich), butyllithium ( $n-\mathrm{BuLi}$ ), calcium hydride, and 1,1-diphenylethylene (DPE, 98\%, Alfa Aesar) were used as received without any purification. Cyclohexane (99\%, Fisher) was stirred over calcium hydride for several days. To remove traces of water, sec-BuLi and DPE were added. The red color of the solution displays the absence of water. Methanol ( $>98.5 \%$, VWR Chemicals), which was used for the termination of the polymerization reactions, was frozen with liquid nitrogen and subsequently thawed to remove oxygen. This was necessary to prevent radical formation and a coupling of two growing polymer chains leading to a doubling of the molecular weight during the termination reaction. This procedure was repeated until no more gas bubbles were observed. Myrcene ( $90 \%$, tech., Acros Organics) was dried by the addition of $n$-BuLi to the monomer until a slight yellow color appeared, indicating the absence of water and the beginning of the polymerization process. Then the monomer was carefully distilled under reduced pressure at approximately $130^{\circ} \mathrm{C}$.

Synthesis of Polymyrcene (PM). Prior to the synthesis of PM, dry cyclohexane (e.g., 100 mL of cyclohexane for 5 g of myrcene) was distilled into the reaction flask. The monomer was then added through a syringe under a counter flow of argon. The polymerization was initiated
by the addition of sec-BuLi. A slight yellowish color was observed for high sample concentrations and low molecular weight samples, which means there was a high concentration of macroanions in the reaction flask. The mixture was stirred for 12 h and finally quenched with degassed methanol. The cyclohexane was removed by freeze-drying of the polymer solution.

This procedure leads to a chain microstructure composed of primarily $1,4-($ cis and trans $)$-addition products (i.e., C6 pendant groups) and $<10 \mathrm{~mol} \%$ of the 3,4 -addition products (C8 pendant units), as determined from $400 \mathrm{MHz}^{1} \mathrm{H}$ NMR. Samples with molecular weight dispersities $Đ$ of 1.11 to 1.16 were obtained. Low dispersities are needed for a correlation of material properties, such as relaxation times, to a respective molecular weight. All polymer samples used in this study are labeled using the abbreviation of the polymer and the weightaverage of the molecular weight in $\mathrm{kg} / \mathrm{mol}$. For example, a polymyrcene sample with a molecular weight of $6700 \mathrm{~g} / \mathrm{mol}$ is labeled PM6.7.

Molecular Weight Determination. The PMs were characterized by size exclusion chromatography (SEC) and ${ }^{1} \mathrm{H}$ NMR to determine the molecular weight of the PM samples and their dispersity $Đ$ (see Table 1).

The weight-average molecular weight $M_{w}$ of the polymer samples was determined via size exclusion chromatography coupled with multiangle laser light scattering (MALLS). The SEC equipment equipment is an Agilent 1200 (Polymer Standard Service, Mainz, Germany). The MALLS unit is a PSS SLD7000/BI-MwA (Brookhaven Instruments). Two PSS SDV Lux $300 \times 8 \mathrm{~mm}$ i.d. columns with pore sizes of $10^{3}$ and $10^{5} \AA$ were used. The mobile phase was THF stabilized with 250 ppm BHT at $30^{\circ} \mathrm{C}$ with a flow rate of $1 \mathrm{~mL} \mathrm{~min}{ }^{-1}$.


Figure 2. Normalized SEC traces for the PM samples versus the elution volume. The SEC traces determined by the DRI detector are displayed.

The refractive index increment $(\mathrm{d} n / \mathrm{d} c)$, which was used to calculate $M_{w}$, was determined by the measurement of a concentration series with a DnDc -2010 differential refractometer from Brookhaven Instruments Corp. (Holtsville, NY). The concentration series consisted of 10 solutions of PM in THF with concentrations ranging from 1.4 to $14.3 \mathrm{~g} /$ L. A THF density of $\rho=0.877 \mathrm{~g} / \mathrm{cm}^{3}$ was used, and a $\mathrm{d} n / \mathrm{d} c$ value of $0.1685 \pm 0.0071 \mathrm{~mL} / \mathrm{g}$ for PM in THF at $T=30^{\circ} \mathrm{C}$ was determined. ${ }^{24}$

The total number-average molecular weight $M_{\mathrm{n}}$ was determined by an end-group analysis using ${ }^{1} \mathrm{H}$ NMR whenever the signal of the end group was sufficient for analysis. For the NMR experiments the samples were dissolved in deuterated chloroform ( $\mathrm{CDCl}_{3}, 99.8 \%$, SigmaAldrich), and signals were referenced to the solvent peak at $\delta 7.26 \mathrm{ppm}$. A Bruker Avance III Microbay 400 MHz spectrometer was used, and 512 scans were performed. Characteristic peaks at 1.59 and 1.67 ppm (methyl groups at $\mathrm{C} 8,6 \mathrm{H}$; see Figure 3) in relation to peaks at 0.86 ppm (methyl protons of sec-BuLi, 6H) were used to calculate $M_{n}$ of the PM samples (see Figure 3). ${ }^{25,26}$

Differential Scanning Calorimetry (DSC). Glass transition temperatures ( $T_{\mathrm{g}}$ ) were determined by differential scanning calorimetry (DSC) using a TA Instruments Q200 differential scanning calorimeter. The experiments were conducted using cooling and


Figure 3. The $400 \mathrm{MHz}{ }^{1} \mathrm{H}$ NMR spectrum of PM in $\mathrm{CDCl}_{3}$ (512 scans). Inset: structure of cis-1,4-PM (A), trans-1,4-PM (B), and 3,4PM (C). ${ }^{26}$
heating rates of $10 \mathrm{~K} / \mathrm{min}$ on samples with a mass $m \sim 10 \mathrm{mg}$. The PM samples were dried in a vacuum oven at 343 K prior to the DSC measurements in order to avoid the influence of moisture, residual solvent, and adsorbed impurities. The $T_{\mathrm{g}}$ was determined to be the inflection point of the heat capacity change in the second heating run. Glass transition temperatures for the PMs under study are presented in Table 1.

Densitiy Measurements. The density of the PM samples was measured in order to calculate the entanglement molecular weight $M_{e}$ by using the Doi and Edwards relation (see eq 2). ${ }^{27}$ The density was determined at room temperature using a high-precision helium pycnometer AccuPyc II 1340 from Micrometrics Instrument Corporation. The sample chamber was calibrated with different density standards before running each measurement. Prior to the measurements all PM samples were extensively dried and purged in order to avoid the influence of moisture and adsorbed impurities. The reported values of the density represents an average of ten consecutive measurements with a determined standard deviation of $0.002 \mathrm{~g} / \mathrm{cm}^{3}$. The obtained densities $(\rho)$ of the PM samples were between 0.89 - and $0.91 \mathrm{~g} / \mathrm{cm}^{3}$ (see Table S3 in the Supporting Information).

Rheological Measurements. Oscillatory shear measurements were performed on a strain-controlled ARES G2 rheometer (TA Instruments) equipped with a force rebalance transducer capable of measuring a torque of $50 \mathrm{nN} \cdot \mathrm{m}-200 \mathrm{mN} \cdot \mathrm{m}$. All PM samples were dried under vacuum at a temperature $T=373 \mathrm{~K}$ for 12 h to remove water and then were loaded onto parallel plates with diameters of 13 and 8 mm for the acquisition of the storage and loss moduli ( $G^{\prime}$ and $G^{\prime \prime}$ ), measured over an angular frequency range of $\omega_{1}=0.1-100 \mathrm{rad} / \mathrm{s}$ under a nitrogen atmosphere. The strain amplitude $\gamma_{0}$ was selected to be within the linear viscoelastic range, $\gamma_{0}<5 \%$. The master curves for the shear moduli $G^{\prime}$ and $G^{\prime \prime}$ were constructed by assuming time-temperature superposition (TTS) at the indicated reference temperature $\left(T_{\text {ref }}=293 \mathrm{~K}\right.$, see Figure 4).

The reference temperature of 293 K was chosen so that a comparison of the zero shear viscosities of the PM samples as a function of molecular weight to the literature data of the dielectric normal mode relaxation times at an isofrictional state ${ }^{28}$ for polyisoprene (PI) and polyfarnesene (PF) is possible (see also final results in Figure 11). The mechanical segmental relaxation time $\left(\tau_{0}=1 / \omega_{1}\right)$ at $T_{\text {ref }}$ is obtained at the frequency $\omega_{1}$, at which the storage $G^{\prime}$ and the loss $G^{\prime \prime}$ moduli cross each other in the glassy state region (see Figure S2). Glass transition temperatures from linear viscoelastic experiments (LVE, $T_{g, L V E}$; see Table 1) were obtained by the local maximum in $G^{\prime \prime}$, which corresponds to the transition in the shift factors from WLF (Williams-LandelFerry) to Arrhenius behavior. The transition from WLF to Arrhenius


Figure 4. Dynamic rheological master curves of the storage and loss moduli for all PM samples from the terminal region to the glassy state at a reference temperature of $T_{\text {ref }}=293 \mathrm{~K}$. The curves were shifted vertically. The scale factors are listed at the left side of the $y$-axis. The molecular weights of the PM polymers below and above critical molecular weight $M_{c}$ are also indicated by the line between PM42.9 and PM74.1. The crossing of the storage $G^{\prime}$ and the loss moduli $G^{\prime \prime}$, from the terminal region to the rubber plateau, in the sample's master curves was used as criteria to distinguish between entangled and unentangled PM samples. In order to make the separation of the samples more clear, the master curves of the two samples (PM42.9 and PM74.1) at the border of critical molecular weight of $M_{c}$ are compared in Figure S3.
behavior indicates the breakdown of the time-temperature superposition below $T_{g}$. The master curve of Figure 5, in which the


Figure 5. Storage and loss modulus of PM115.9 at $T_{\text {ref }}=293 \mathrm{~K}$ from the terminal regime (a) via the rubber plateau (b) and the transition zone (c) to the glassy state (d). Inset: horizontal shift factor $a_{T}$ used to generate the master curve. The solid red line represents fits using the WLF equation. The dashed vertical line represents the glass transition temperature from DSC measurements. In rheological experiments $T_{g}$ was obtained by the local maximum of $G^{\prime \prime}$ at a frequency of $0.01 \mathrm{rad} / \mathrm{s}$.
rheological data are shifted beyond $T_{\mathrm{g}}$ and the Arrhenius behavior of $a_{T}$ becomes clearly visible, is only shown in the Supporting Information. The $T_{\mathrm{g}, \mathrm{LVE}}$ and $T_{\mathrm{g}, \mathrm{BDS}}$ are identical with those determined from DSC within experimental uncertainty. For the transition between the Newtonian flow range at low frequencies and the rubbery range at higher frequencies the same procedure can be applied (see Figure S2). ${ }^{29}$ Relaxation times at another reference temperature can be obtained by $\tau\left(T_{\text {ref }}\right)=\tau(T) \log a_{T}$.

Broadband Dielectric Spectroscopy Measurements. Broadband dielectric spectroscopy (BDS) measurements were performed using a Novocontrol high-resolution Alpha dielectric analyzer Concept 40 over the frequency range of $10^{-1}$ to $10^{7} \mathrm{~Hz}$, aided by a Quattro Cryosystem temperature controller with a temperature stability of $\Delta T<$
0.1 K, under a dry nitrogen atmosphere. Polished gold electrodes with diameters of 15 and 10 mm were placed on the bottom and top of the samples, respectively, to create a parallel plate capacitor cell. Three fused $\mathrm{SiO}_{2}$ fibers with diameters of $50 \mu \mathrm{~m}$ were used as spacers. The sandwiched polymer films were positioned in the Novocontrol spectrometer. The dielectric permittivity and conductivity were measured isothermally in steps of 10 K using an AC voltage amplitude of 1.5 V over a broad temperature range ranging from 123 to 393 K . This was done in both cooling and heating in order to verify reproducibility. Prior to measurements, each sample was annealed in the Novocontrol sample cell at 393 K in a heated stream of nitrogen for 2 h to remove moisture acquired during sample loading and air bubbles.

## ■ RESULTS AND DISCUSSION

The mechanical shear response of polymer melts in the linear regime can provide a clear signature of various processes, such as the melt flow, rubbery plateau, glassy dynamics, and subglass transition relaxations. ${ }^{30,31}$ A crucial component is the combination of measurements at various frequencies and temperatures. To do so, master curves for $T_{\text {ref }}=293 \mathrm{~K}\left(T_{\mathrm{g}}+87 \mathrm{~K}\right)$ were generated by frequency-scale shifting the isothermal frequency sweep data, within the linear regime, from 393 to 213 K (with increments of 10 K ) for all PM samples, as shown in Figure 4. Analyzing Figure 5, which displays the master curve of PM115.9, two relaxation processes can be clearly determined in the rheological data: the lower frequency process (around $\omega_{1}=1$ $\mathrm{rad} / \mathrm{s}$ ) is attributed to the chain relaxation, while the higher frequency relaxation (around $\omega_{1}=10^{9} \mathrm{rad} / \mathrm{s}$ ) is associated with the segmental relaxation ( $\alpha$-process). Time-temperature superposition (TTS) works well (for the temperatures above $T_{\mathrm{g}}$ ) for the LVE spectra, and the segmental relaxation is confirmed to be associated with the observed $\alpha$-process by fitting the temperature dependence of the frequency-scale horizontal shift factors $\left(a_{T}\right)$ with the WLF equation. The frequency shift factors between 393 and 213 K are well fitted by the WLF equation. The glass transition temperature can be quantified from rheometry data by the local maximum in $G^{\prime \prime}$ (around $\omega_{1}=10^{10} \mathrm{rad} / \mathrm{s}$ at $T_{\text {ref }}=293 \mathrm{~K}$ ) because the loss modulus defines the relaxation process. To approximate a frequency-independent $T_{g}$, the data were shifted to a low angular frequency such as $0.01 \mathrm{rad} / \mathrm{s}$. Alternatively, the peak in $\tan \delta(=$ $\left.G^{\prime \prime} / G^{\prime}\right)$ can be used to determine $T_{g}$, or the Vogel-Fulcher temperature from the WLF fit ( $T_{\mathrm{g}}=50 \mathrm{~K}+T_{0}$ ). The VogelFulcher temperature $T_{0}$ is the temperature, at which the system deviates from the equilibrium, where the domain of cooperativity grows toward the infinite size at the Kauzmann zero entropy temperature. ${ }^{32-35}$ A tabulated summary of the quantitative agreement of the glass transition temperatures ( $T_{\mathrm{g}, \mathrm{DSC}}, T_{\mathrm{g}, \mathrm{LVE}}$, and $T_{\mathrm{g}, \mathrm{BDS}}$ ) for all samples in this work is shown in Table 1.
The insets in Figures 5 and 6 show the correlation between the horizontal shift factors $a_{T}$ and the inverse temperature for the PM samples.
The temperature dependence of the experimental multiplicative horizontal shift factors, $a_{T}$, used to construct the master curves in Figures 4 and 5 obeyed the WLF equation given by

$$
\begin{equation*}
\log a_{T}=-\frac{C_{1}\left(T-T_{\mathrm{ref}}\right)}{C_{2}+T-T_{\mathrm{ref}}} \tag{1}
\end{equation*}
$$

where $C_{1}$ and $C_{2}$ are nearly universal constants that depend mainly on the relative difference to $T_{g}$, respective the chosen reference temperature $T_{\text {ref }}$, which is 293 K in the specific case. The $a_{T}$ shift factors for all PM samples collapse onto a single


Figure 6. Complex viscosity versus reduced frequency for the PM samples at $T_{\text {ref }}=293 \mathrm{~K}$. Insets: (a) Frequency shift factors ( $a_{T}$ ) used to generate the master curves. The solid red line represents fits using the WLF equation. (b) Zero shear viscosities at $T_{\text {ref }}=293 \mathrm{~K}$ as a function of $M_{\mathrm{w}}$ for the PM materials. The dotted vertical line represents the approximate critical molecular weight $M_{c} \cong 4.4 \times 10^{4} \mathrm{~g} / \mathrm{mol}$ for PM. Slope values are also indicated.
curve, which can be described by a single WLF curve (solid red line in the insets of Figures 5 and 6). The fact that TTS is obeyed implies that the segmental dynamics of the polymer chains show a strong dependence on $T$. The best fit curve to the data using the WLF equation gives $C_{1}=4.7$ and $C_{2}=130.5 \mathrm{~K}\left(\right.$ at $T_{\mathrm{g}}+87$ $\mathrm{K})$. The fit parameter $C_{1}$ correlates the mobility of the polymer chains at $T_{\text {ref }}$ to their maximal mobility. The parameter $C_{2}$ reflects the non-Arrhenius character of the polymer and represents a measure of the fragility that classifies the polymers in "strong" and "fragile" according to the Angell plot. ${ }^{36,37}$ Normally, the values of the horizontal shift factors, $a_{T}$, at $T_{\mathrm{g}}$ should be zero if $T_{\text {ref }}=T_{\mathrm{g}}$; in our case, $a_{T}$ is greater than 12 because our $T_{\text {ref }}$ was chosen to be 293 K intentionally in order to compare the zero shear viscosities ( $\eta_{0}$, measured via oscillatory shear and applying the Cox-Merz rule) of PMs at 293 K with dielectric normal mode relaxation times at an isofrictional state for polyisoprene (PI) and polyfarnesene (PF) (see their comparison in Figure 11). At isofrictional conditions, the normal mode relaxation is normalized to the segmental relaxation in order to eliminate a large influence on $\eta_{0}$ caused by only small differences in $T_{g}$.

In order to quantify the relaxation times determined from BDS and LVE in Figure S2, we analyzed the molecular dynamics of PM samples where we demonstrated that there is a good coincidence of the terminal relaxation times obtained from LVE measurements and normal-mode relaxation times obtained from dielectric spectroscopy.

Figure 6 shows the absolute value of the complex viscosities ( $\left|\eta^{*}\right|$ ) versus the reduced frequency $\left(a_{T} \omega_{1}\right)$ constructed at $T_{\text {ref }}=$ 293 K for all PM samples under investigation. The zero shear viscosities, measured at low shear rates, are obtained from the plateau of the reduced complex viscosity plotted against reduced frequency $\left(a_{T} \omega_{1}\right)$. These values are displayed as a function of $M_{w}$ at $T_{\text {ref }}=293 \mathrm{~K}$ in the inset (b) of Figure 6. The zero shear rate viscosity (zero shear viscosities, $\eta_{0}$ ) is widely used as a fundamental descriptor of the flow resistance of polymer melts characterizing both the rheological response at a low stress as well as low shear rates and the influence of the molecular architecture on the resistance to flow. For the case of amorphous flexible linear polymer melts it is well-known that the dynamics of short polymer chains are governed solely by the Rouse
behavior, while that of long chains follows a reptation behavior due to the presence of physical entanglements. ${ }^{38-40}$ Consequently, according to the tube model by de Gennes ${ }^{41}$ and Doi and Edwards, ${ }^{42}$ the prediction for the scaling of the zero-shear viscosity $\eta_{0}$ is expected to depend approximately linear on the molecular weight for low molecular weights. The viscosity depends directly on the molecular weight of the chain $M_{w}{ }^{1}$ if $M_{w}$ $<M_{c}$ (specific critical molecular weight). For $M_{w}>M_{c}$ the molecular weight dependence of the zero-shear viscosity increases $\eta_{0} \propto M_{\mathrm{w}}{ }^{3.4}$. For a molecular weight $M_{\mathrm{w}}>M_{\mathrm{r}}$ the zero-shear viscosity shows the following dependence $\eta_{0} \propto$ $M_{\mathrm{w}}{ }^{3} \cdot{ }^{36,37} M_{\mathrm{r}}$ is the reptation molecular weight, which is defined within this article as the molecular weight at which the experimental viscosity reverts to the expected $M_{\mathrm{w}}{ }^{3}$ dependence and is based on a combination of reptation and constraint release. As seen in the inset (b) of Figure 6, the dynamics of entangled polymyrcene chains display a transition in the slope of $\log \eta_{0}$ versus $\log M_{\mathrm{w}}$ to $\propto 3.7 \pm 0.3$ at higher molecular weights, indicative of the transition to entangled chain dynamics. The dynamics of entangled chains are understood in terms of reptation and the characteristic limiting processes, including the contour length fluctuations, originally proposed by Doi, ${ }^{42}$ and the constraint release. ${ }^{43}$ The effect of these competing processes in the transition regime between Rouse and pure reptation dynamics may reflect the different values of the power law from the prediction for the scaling of $\eta_{0}$ with molecular weight. This can be seen in experimental data at $T_{\text {ref }}=293 \mathrm{~K}$ of the zero-shear viscosity as a function of molecular weight of polyisoprene and polybutadiene polymer melts, which shows for the entangled region $\eta_{0} \propto M_{\mathrm{w}}{ }^{3.7}$ and $\eta_{0} \propto M_{\mathrm{w}}{ }^{3.29}$, respectively. ${ }^{40}$ While the dynamics of entanglements at higher $M_{\mathrm{w}}$ are observed by the rubbery plateau and the presence of the crossover of $G^{\prime}$ and $G^{\prime \prime}$ as observed in Figure 5 for PM115.9 and Figure 4 from PM74.1 to PM347.7. A further, second transition, denoted by $M_{r}\left(M_{r}=\right.$ $190550 \mathrm{~g} / \mathrm{mol}$, with the number of entanglements $Z=10$ ), is observed from entangled behavior due to pure reptation (Figure 6). Nevertheless, considering the relatively modest number of PM samples explored in this molecular weight range, the pure reptation molecular weight should be used with caution. The tube model by Doi and Edwards predicts that the large-scale dynamics of chains in an amorphous linear polymer melt emerge simply from a fundamental length scale called the tube diameter interpreted as the end-to-end distance of entanglements. ${ }^{39}$ Experimentally, $M_{\mathrm{e}}$ is determined from the plateau modulus $G_{n}^{0}$, known as the signature of entanglements during stressrelaxation, that can be obtained from the elastic $G^{\prime}$ modulus from the master curve in the rubbery region. In case $G^{\prime}$ did not exhibit a clear plateau, $G_{n}^{0}$ was determined from the value of $G^{\prime}$ around the middle of the elastic plateau between the two intersections of $G^{\prime}$ and $G^{\prime \prime}$ below and above the rubber plateau at the minimum of $\tan \delta:{ }^{39,40}$

$$
\begin{equation*}
M_{\mathrm{e}}=\rho R T / G_{n}^{0} \tag{2}
\end{equation*}
$$

where $\rho\left(\approx 0.91 \mathrm{~g} / \mathrm{cm}^{3}\right)$ is the polymer density, $R$ is the ideal gas constant, and $T$ is the reference temperature, at which $G_{n}^{0}$ was determined. The measured values for the density of all PM samples can be found in Table S3. The preceding equation establishes a clear relationship between microscopic, chemistrydependent details and the global chain dynamics of polymer melts. The value of the plateau of the elastic $G^{\prime}$ modulus in Figure 5 is $G_{n}^{0}=124.4 \mathrm{kPa}$, and consequently we obtain a value of $M_{\mathrm{e}}=17800 \mathrm{~g} / \mathrm{mol}$. The obtained value for PM's $M_{\mathrm{e}}$ is between those of PI $\left(M_{e}=5 \times 10^{3} \mathrm{~g} / \mathrm{mol}\right)$ and PF $\left(M_{e}=5 \times 10^{4} \mathrm{~g} / \mathrm{mol}\right)$
and is similar to the polymyrcene entanglement molecular weight reported by Fetters et al. ${ }^{44}$ The molecular weight $M$ of the related monomers is $M=68.12 \mathrm{~g} / \mathrm{mol}$ for isoprene, $M=$ $136.23 \mathrm{~g} / \mathrm{mol}$ for myrcene, and $M=204.36 \mathrm{~g} / \mathrm{mol}$ for farnesene.

Typical dielectric spectra for the dielectric loss at selected temperatures and as a function of frequency are presented in Figure 7. Clearly, three relaxation processes are observed for


Figure 7. PM 6.7 dielectric loss spectra at selected temperatures as indicated versus frequency. Three relaxation processes are observed: the normal mode ( n ), the $\alpha$-relaxation, and the $\beta$-relaxation. The solid lines represent the HN fits.

PM: the frequency corresponding to the peak in the imaginary part of the loss spectra $\epsilon^{\prime \prime}$ at high temperature and rather low frequency is related to the chain, which can relax by what is known as the dielectric normal mode ( n ), reflecting the fluctuation of the end-to-end vector characterizing the global chain dynamics. The n relaxation follows a non-Arrhenius behavior and is mainly influenced by $M_{\mathrm{w}}$ (see Figure 10). At lower temperatures the second dipolar-like relaxation is observed, which is related to the segmental dynamics or dynamic glass transition process $(\alpha)$ of the polymer and is often well described by the empirical Havriliak-Negami (HN) function in the frequency domain. ${ }^{29}$ The $\alpha$-process and the dielectric normal mode process are resolved by fitting two HN functions to the two relaxation processes (see Figure 7). The empirical HN function with additional conductivity contribution is ${ }^{29,45,46}$

$$
\begin{equation*}
\epsilon^{*}(\omega)=\epsilon_{\infty}+\sum_{j=2} \frac{\Delta \epsilon}{\left[1+\left(i \omega \tau_{\mathrm{HN} j}\right)^{m}\right]^{n}}-i\left(\frac{\sigma_{0}}{\epsilon_{0} \omega}\right)^{s} \tag{3}
\end{equation*}
$$

where $\sigma_{0}$ is the dc conductivity, $\omega$ is the angular frequency of the external applied electric field, $s$ is the exponent describing conductivity slope and should ideally be $1, \epsilon_{0}$ is the permittivity in free space, $\Delta \epsilon$ is the dielectric relaxation strength of the $j$ process, $\tau_{\mathrm{HNj}}$ is the HN characteristic relaxation time related to $\tau_{\max } m$ (that is inversely related to the width of the relaxation) and $n$ (that is the high-frequency asymmetry parameter) are the shape parameters, and $j$ is the index over which the relaxation processes are summed. The secondary relaxation spectra ( $\beta$ relaxation processes) were analyzed using a symmetric ColeCole function (corresponding to a shape parameter $\beta=1$ in the HN equation). The characteristic relaxation times for each process were estimated as the reciprocal of the peak frequency $\tau$ $=1 / 2 \pi f_{\max }$. The $\alpha$-relaxation time (obtained by fitting the peak in the imaginary part of the loss spectra at different temperatures by using the HN function) follows a non-Arrhenius behavior and is mainly influenced by the temperature. Although $T_{g} \mathrm{~s}$ of the

PM samples are not very different, the $T_{\mathrm{g}}$ increases slightly as the degree of polymerization increases followed by a saturation at high molecular weights. This small molecular weight dependence of $T_{\mathrm{g}}$ is well-known for polymers and can be described by the so-called Flory-Fox equation. ${ }^{8,47-49}$ The third relaxation process, on the high-frequency side and below $T_{g}$, is attributed to a local relaxation in the glassy state $(\beta)$, and its temperature evolution follows an Arrhenius behavior.

The use of the horizontal (frequency) axis shift principle to describe the polymer behavior over an extended frequency range, as applied to rheological data, can also be applied to dielectric spectroscopy data. However, this principle is often not used because of the already extremely broad frequency range accessible to dielectric spectroscopy techniques at a single measured temperature, at which 8-9 decades in frequency can be measured, compared to rheology where usually around 3-4 decades are measured. Nevertheless, this principle in dielectric spectroscopy should be used with caution; this method works reasonably in a limited frequency range, but some parts of the shifted data corresponding to different relaxation processes does not overlap (e.g., the peaks of the secondary $\beta$-relaxation process); this behavior is related to different temperature dependencies of the relaxation times of the respective processes. The dielectric modulus has mainly been used for the construction of the dielectric master curves when compared to the results of mechanical spectroscopy. This was demonstrated by Kremer et al. for the case of PI, where the comparison of temperature dependencies of the relaxation times obtained from the two methods indicates a very good coincidence of the terminal relaxation times determined by rheology and the normal mode relaxation times determined from dielectric measurements. ${ }^{29}$ Similar agreement between the relaxation times in the master curves constructed from rheological and dielectric measurements are also observed for PM115.9 (see Figure S2).
In order to show the dielectric spectral shape of the $\alpha$-peak and the normal mode with temperature, we plot in Figure 8 the


Figure 8. Rescaled dielectric spectra for PM115.9 for indicated temperatures, where $\epsilon^{\prime \prime}$ is rescaled by the maximum height $\epsilon_{\alpha, \max }^{\prime \prime}$ and $f$ by the frequency $f_{\alpha, \max }$ of the $\alpha$-peak.
dielectric spectra of PM115.9 and in Figure 9 the dielectric spectra for all PMs in this study, for which $\log \epsilon^{\prime \prime} / \epsilon_{\alpha, \text { max }}^{\prime \prime}$ is plotted versus rescaled frequency $\log f / f_{\alpha, \text { max }}$, where $\epsilon_{\alpha, \text { max }}^{\prime \prime}$ and $f_{\alpha, \text { max }}$ are the height and the frequency, respectively, of the alpha peak. The rescaled dielectric data in Figure 8 show the segmental mode process and the dynamic glass transition process $(\alpha)$ at $\log f /$ $f_{\alpha, \text { max }}=0$. The peak below this value is related to the normal mode relaxation process where $\log f / f_{\alpha, \max }=-7$. As expected, for


Figure 9. Rescaled dielectric spectra of polymyrcene samples investigated: PM6.7 ( $T=213-233 \mathrm{~K}$ ), PM11.6 ( $T=213-243 \mathrm{~K}$ ), PM14.8 $(T=223-233 \mathrm{~K})$, PM36.6 $(T=223-253 \mathrm{~K}, \mathrm{PM} 42.9(T=$ 233-253 K), PM74.1 ( $T=233-263 \mathrm{~K}$ ), PM85.6 ( $T=243-273 \mathrm{~K})$, PM115.9 $(T=233-293 \mathrm{~K})$, PM155.1 $(T=263-283 \mathrm{~K})$, PM347.7 ( $T$ $=273-293 \mathrm{~K}$ ): dielectric pemittivity $\epsilon^{\prime \prime}$ rescaled by its $\alpha$-peak height $\epsilon_{\alpha, \max }^{\prime \prime}$ and $f$ rescaled by the frequency $f_{\alpha, \text { max }}$ of the $\alpha$-peak.
higher $M_{w}$, the normal mode process for all PM samples shifts to lower reduced frequencies. In the frequency range of the $\alpha$ process the data agree well, and one can observe that the envelope of the $\alpha$-peak is temperature and molecular weight independent. For one sample, namely PM74.1, a broad $\alpha$-peak is observed, where the left wing is following a different behavior with respect to the other samples for reasons not known yet. One may suspect the molecular weight dispersity to play a role in the peak broadness; however, according to Table 1, PM74.1 has a $Đ$ of 1.12 , which is similar to the other polymer samples. The peak position of the normal mode seems to be between PM42.9 and PM85.6, in agreement with measured $M_{w}$ s.

Figure 10 shows the relaxation rates of the glassy state, segmental relaxations and the normal mode relaxation as a


Figure 10. Relaxation rates for the glassy state $\beta$-relaxation, $\omega_{\beta}$, the segmental relaxation process, $\omega_{\alpha}$, and the normal mode relaxation, $\omega_{n}$, for PM with different $M_{\mathrm{w}}$ versus 1000/T. The solid lines are VFT and Arrhenius fits. The dashed line labeled $T_{g}$ (BDS) indicates the extrapolation of the VFT fits to $1 / \omega=100 \mathrm{~s}$. The VFT fit parameters are presented in Table S2. The $T_{\mathrm{g}}$ values obtained from BDS measurements are similar to those from LVE and DSC within experimental uncertainty (see Table 1).
function of the inverse temperature. The glassy state $\beta$-relaxation $\left(\omega_{\beta}\right)$ processes are observed below $T_{\mathrm{g}}$ and coincide for all PM samples under study, reflecting a similar motion. Analyzing further the activation plot, the temperature evolution of the $\beta$ relaxation peak follows an Arrhenius behavior, $\omega_{\beta}(T)=\omega_{0}$ $\exp \left(-E_{\mathrm{a}} / R T\right)$, with an activation energy of $E_{\mathrm{a}}=25 \mathrm{~kJ} / \mathrm{mol}$. We speculate that the origin of the $\beta$-relaxation processes is
connected to the polymyrcene side group motions in the glassy state. Because the polymyrcene structure consists of two or four carbon atoms in the backbone repeat unit and C6 or C8 (see Figure 3), as a pendant group, it is expected that at high molecular weights the chains adopt a cylindrical bottlebrush-like structure with tightly spaced side chains similar to a previously studied bottlebrush-like polymer, namely polyfarnesene, PF. ${ }^{8}$ Given that the backbone units of PF are identical with PM and have slightly longer pendant groups consisting of C11 and C13, we may expect PF to display a higher activation energy of its side group motions compared to PM. This is indeed confirmed as the activation energy of PF was found to be $E_{\mathrm{a}}=28 \mathrm{~kJ} / \mathrm{mol}$, which supports our hypothesis regarding the origin of the $\beta$-relaxation processes. ${ }^{8}$ Turning to the activation plot for the different processes, displayed in Figure 10, at higher temperatures, the segmental relaxation seems to follow a Vogel-FulcherTammann (VFT) temperature dependence, typical for the most glassy polymer systems. The empirical Vogel-FulcherTammann equation is given as $\omega_{\alpha}=\omega_{\infty} \exp \left(-B T_{0} / T-T_{0}\right)$ where $\omega_{\infty}=\tau_{\infty}{ }^{-1}$, the high-temperature limit of the relaxation rate; $B$ is a constant related to fragility-a measure of the extent of deviation from the Arrhenius dependence and $T_{0}$ is the Vogel temperature, which typically lies about $50^{\circ} \mathrm{C}$ below the glass transition temperature. ${ }^{50}$

On the basis of $B$ values from Table $\mathrm{S} 2, \mathrm{PM}$ is considered as a fragile glass. The VFT fit parameters are presented in Table S2. The $\alpha$-process for all materials is very similar and covers relaxation rates over more than 7 decades $\left(\omega / 2 \pi=10^{-1}-10^{6}\right.$ Hz ) and 4 decades in the inverse temperature, $1000 / T$.

The glass transition temperatures obtained from the dielectric measurements, $T_{\mathrm{g}, \mathrm{BDD}}$, are determined by VFT fits of the mean structural relaxation rates $\omega_{\alpha}$ vs $1000 / T$ extrapolated to the value $1 / \omega=100 \mathrm{~s}$, which is an empirical relation (the $T_{\mathrm{g}}$ values of the intersection of the extrapolated VFT curve with the horizontal line at 100 s ) that is used for obtaining the $T_{\mathrm{g}}$ by broadband dielectric spectroscopy and correlates well with $T_{\mathrm{g}} \mathrm{s}$ from DSC measurements. The values of $T_{\mathrm{g}, \mathrm{BDS}}$ are in agreement with the $T_{\mathrm{g}} \mathrm{s}$ obtained from LVE and DSC measurements and are all listed in Table 1.
A slight increase of $T_{\mathrm{g}}$ (from 205 to 209 K ) with $M_{\mathrm{w}}$ is observed for low-molecular-weight samples due to the influence of end-group contributions; higher molecular weight samples are less influenced by the end-group contributions. In contrast to the $\alpha$ - and $\beta$-relaxation processes, the normal mode relaxation process observed at high temperatures is as expected highly dependent on the molecular weight of PM covering 2 orders of magnitude of molecular weights and 7 decades in relaxation rates. On the basis of the chemical structure of PM and its adopted conformation, where the electrical dipole moment is parallel along the polymer backbone, we attribute this relaxation processes to the normal mode relaxation originating from the collective polymer dynamics. ${ }^{47}$ The normal mode relaxations seems to follow for each molecular weight sample a VFT temperature dependence, typical for the cooperative processes of Stockmayer type A polymers.
The ratio $\tau_{n} / \tau_{\alpha}$ of the normal mode $\tau_{n}$ and the $\alpha$-relaxation time $\tau_{\alpha}$ as a function of the molecular weight $M_{\mathrm{w}}$ of PM compared to linear polyisoprene (PI) ${ }^{51-53}$ and polyfarnesene $(\mathrm{PF})^{8}$ is included in Figure 11. This approach of the data representation is known as an isofrictional condition, where the molecular weight dependence of the monomeric friction coefficient is given by the temperature dependence of the normal mode relaxation normalized by the segmental relaxation
of each material at a fixed temperature. Further in Figure 11b normalization of $M_{w}$ to the $M_{c}$ allows a comparison of the unentangled-entangled transition for each polymer melt (PI, PM, and PF). This can also be seen by the inflection point of the complex viscosity $\left(\frac{\mathrm{d}^{2} \log \eta^{*}{ }^{*} \mid}{\mathrm{d}\left(\log _{a_{T}} \omega\right)^{2}}\right)$ in Figure 6 and the normal mode relaxation times at an isofrictional state of the different polymers collapsing onto each other. At the same time, the zero-shear viscosity experimentally demonstrates the universality of the polymer melts' dynamics, which is highlighted by the three regimes of their dynamical behavior as the molecular weight increases: the Rouse regime, the entanglement regime, and an indicated pure reptation regime. Additionally, the comparative representation of $M_{\mathrm{w}}$ normalized to the $M_{\mathrm{e}}$ of the respective polymers can be found in the Supporting Information (Figure S5).

In Figure 11 three power-law regions for two polymers, namely PI and PM, can be observed. PF shows just two regimes:


Figure 11. Solid symbols: dielectric normal mode relaxation times for polyisoprene (PI: square symbols, reproduced from refs 28 and 51-53), polyfarnesene (PF: circle symbols, reproduced from ref 8), and polymyrcene (PM: triangle symbol) versus (a) $M_{\mathrm{w}}$ at an isofrictional state and (b) normalized $M_{\mathrm{w}} / M_{\mathrm{c}}$. Open symbols: zero shear viscosities at $T_{\text {ref }}=293 \mathrm{~K}$ as a function of (a) $M_{w}$ and (b) normalized $M_{\mathrm{w}} / M_{\mathrm{c}}$ for the PI, ${ }^{40} \mathrm{PF},{ }^{8}$ and PM materials. The dotted vertical lines represent the approximate critical molecular weight $M_{c}$ for PI, $\left.M_{\mathrm{c}(\mathrm{PI})} \cong 10^{4.2} \mathrm{~g} / \mathrm{mol} \cong 1.6 \times 10^{4} \mathrm{~g} / \mathrm{mol}\right)$, PF $\left.M_{\mathrm{c}(\mathrm{PF})} \cong 10^{5} \mathrm{~g} / \mathrm{mol}\right)$, and $P M M_{c(P M)} \cong 10^{4.6} \mathrm{~g} / \mathrm{mol} \cong 4.4 \times 10^{4} \mathrm{~g} / \mathrm{mol}$. Slope values are also indicated.

Rouse dynamics and an entanglement region. The pure reptation regime was not reached in the case of PF because of the lack of high $-M_{w}$ synthesized samples with narrow molecular weight dispersity. The ratio $\tau_{n} / \tau_{\alpha}$ was observed to be $\propto M^{z}$, with $z=2$ in the Rouse dynamic region, $z=3.4$ and 3.7 for the entangled region, and the transition from the first region to the second region. This is associated with the entanglement molecular weight with $M_{c} \cong 10^{4.2} \mathrm{~g} / \mathrm{mol}\left(\cong 1.6 \times 10^{4} \mathrm{~g} / \mathrm{mol}\right)$ for PI, ${ }^{29,51,54-56}$ and $M_{\mathrm{c}} \cong 10^{4.6} \mathrm{~g} / \mathrm{mol}\left(\cong 4 \times 10^{4} \mathrm{~g} / \mathrm{mol}\right)$ and $M_{c}$ $\cong 10^{5} \mathrm{~g} / \mathrm{mol}$ for PM and PF, respectively. ${ }^{8}$ Note that $z=2$ was
also observed by other studies of the dielectric normal mode for linear PI. ${ }^{56}$ The experimental finding of $M_{c}$ of PM is between $M_{c}$ of PI and PF (its monomer is an isoprene trimer) is not surprising; the backbone segments of PM are analogous to isoprene and $\beta$-myrcene can be considered an isoprene dimer. Above $M_{c}$ the entanglement dynamics dominate until the second crossover between entanglement and pure reptation is achieved at $M_{\mathrm{r}} \cong 10^{5} \mathrm{~g} / \mathrm{mol}$ and $M_{\mathrm{r}} \cong 10^{5.3} \mathrm{~g} / \mathrm{mol}\left(\cong 2 \times 10^{5} \mathrm{~g} /\right.$ mol ) for PI and PM, respectively. At higher molecular weights of $\mathrm{PM}\left(>M_{\mathrm{r}}\right) z$ decreases to a value of 3 , which could be attributed to a pure tube repatation, but has to be considered with caution due to a low number of data points in this molecular weight range. ${ }^{27,41}$ The relation of $M_{\mathrm{r}}$ to $M_{\mathrm{c}}$ with $M_{\mathrm{r}}=5 M_{\mathrm{c}}$ in the case of PM is small compared to other polymers such as polystyrene ( $M_{\mathrm{r}}$ $=15 M_{\mathrm{c}}$ ), polyisobutylene ( $M_{\mathrm{r}}=25 M_{\mathrm{c}}$ ), polybutadiene ( $M_{\mathrm{r}}=$ $\left.100 M_{c}\right)$, and polyethylene $\left(M_{\mathrm{r}}=220 M_{\mathrm{c}}\right) .{ }^{57-60}$ This may be attributed to the chemical structure like the size of groups attached to the polymer backbone as well as the mobility of the backbone itself. The two polymers PI and PM, which were compared in this study, also show this trend of an increasing $M_{c} /$ $M_{\mathrm{r}}$ with a decrease in size of the groups attached to the polymer backbone. Accordingly, $M_{\mathrm{r}}$ of PI is 6.25 its $M_{c}$. The polymer polybutadiene, whose backbone is the same as for PI and PM but does not carry any group, additionally confirms this trend. In order to illustrate the comparison of the normal mode at isofrictional conditions to the chain relaxation, in Figure 11 also $\log \eta_{0}$ versus $M_{\mathrm{w}}$ is presented. In the low- $M_{\mathrm{w}}$ regime, $M_{\mathrm{w}}<M_{\mathrm{c}}$, the slope of PM samples is $\cong 1.2 \pm 0.03$, indicating a Rouse-like behavior up to $M_{c} \cong 1.6 \times 10^{4} \mathrm{~g} / \mathrm{mol}$; this slope is very similar to that found for bottlebrush polymers with atactic polypropylene (a-PP) side chains synthesized via ring-opening metathesis polymerization using Grubbs third-generation catalyst as well for the case of PF bottlebrush polymers with C11 and C13 pendant groups. ${ }^{8,61,62} \mathrm{~A}$ simple comparison between these two materials, PF and PM, shows a clear transition from the Rouse to the entangled region, identical with dielectric findings (PM: $M_{c}$ $\cong 10^{4.6} \mathrm{~g} / \mathrm{mol}\left(\cong 4.4 \times 10^{4} \mathrm{~g} / \mathrm{mol}\right)$ and PF: $\left.M_{\mathrm{c}} \cong 10^{5} \mathrm{~g} / \mathrm{mol}\right)$. The $M_{c}$ of PM and PF is significantly higher than for linear PI where $M_{c} \cong 10^{4} \mathrm{~g} / \mathrm{mol}$; instead, bottlebrush polymers based on atactic polypropylene side chains show no transition to the entanglement region. The bottlebrush polymers based on atactic PP undergo a sphere-to-cylinder conformational transition manifested in the Rouse-like behavior up to $M_{w} \gg M_{c} \cong 10^{6}$ $\mathrm{g} / \mathrm{mol} .{ }^{61}$ The PM pendant groups are much shorter (C6 and $\mathrm{C} 8)$ than in the case of $\mathrm{PF}(\mathrm{C} 11$ and C 13$)$ and below the entanglement molecular weight of linear PI, making it possible that at high molecular weight $\left(M_{\mathrm{c}}>10^{4.6} \mathrm{~g} / \mathrm{mol}, Z \approx 10\right) \mathrm{PM}$ behaves like an entangled polymer melt with a large molecular weight between the backbone entanglements. Given the chemical architecture and dynamics of PM over a broad frequency and temperature range, which are similar to those of PF, we conclude that PM behaves like a bottlebrush polymer melt whose normal mode relaxation is strongly dependent on molecular weight as expected for a Stockmayer type A polymer (see Figure 10).

## ■ CONCLUSION

In summary, a series of narrowly distributed PM samples in the molecular weight range of $M_{\mathrm{w}}=6700$ to $347000 \mathrm{~g} / \mathrm{mol}$ were synthesized, and the molecular chain dynamics of polymyrcene (PM) were investigated by employing oscillatory shear, DSC, and broadband dielectric spectroscopy measurements. The results were compared to structurally similar polymers, but with
shorter and longer side groups such as polyisoprene and polyfarnesene (PF), respectively (see Table 2). Dielectric

Table 2. Comparison of $M_{e}$ and $T_{g}$ of the Polyterpenes Polyisoprene, Polymyrcene, and Polyfarnesene ${ }^{a}$

|  | polyisoprene | polymyrcene | polyfarnesene |
| :--- | :---: | :---: | :---: |
| $M_{\mathrm{e}}(\mathrm{g} / \mathrm{mol})$ | 5000 | 17800 | 50000 |
| $T_{\mathrm{g}}(\mathrm{K})$ | 212 | 208 | 198 |

${ }^{a}$ The values are associated with the cis- 1,4 isomer of the polymers under comparison. The values for PI and PF are taken from the literature. ${ }^{8,54}$
measurements establish that PM is a new Stockmayer type A polymer, exhibiting a global end-to-end relaxation process strongly dependent on $M_{w}$. Considering the zero shear viscosities as a function of $M_{w}$ for the polymyrcene series, we found the scaling exponents of $\sim 1.2$, corresponding to the Rouse-like dynamics and $\sim 3.7$ above a critical molecular weight ( $M_{\mathrm{c}} \cong 10^{4.6} \mathrm{~g} / \mathrm{mol} \cong 4.4 \times 10^{4} \mathrm{~g} / \mathrm{mol}$ ), corresponding to the entanglement regime $\left(M_{c} / M_{e} \sim 2-4\right)$. This deviation of the scaling exponent in the unentangled regime from the expected value of 1 seems to be related to the bottlebrush-like nature of PM and PF, which both carry densely packed groups. Above $M_{c}$, PM behaves as an entangled polymer melt, with a molecular weight between backbone entanglements of $M_{e}=1.78 \times 10^{4} \mathrm{~g} /$ mol . At molecular weights much larger than the reptation molecular weight ( $M_{\mathrm{w}} \gg M_{\mathrm{r}}$, number of entanglements $Z$ ca.10), similar to the linear homopolymers, a scaling exponent of the zero shear viscosities on $M_{w}$ of $\sim 3$ is found, which could be attributed to a pure reptation, but has to be considered with caution due to a large error resulting from only a single data in this molecular weight range.

## ASSOCIATED CONTENT

## (s) Supporting Information

The Supporting Information is available free of charge at https://pubs.acs.org/doi/10.1021/acs.macromol.2c01884.

Figure S1: chemical structure of the monomers and their respective polymers; Table S 1 : isomer contents determined by $400 \mathrm{MHz}{ }^{1} \mathrm{H}$ NMR ( 512 scans); Table S2: VFT fitting parameters of the normal mode and $\alpha$-segmental relaxations of the PM samples; Table S3: density values determined for each of the PM samples; Figure S2: electrical and mechanical master curves for PM115.9 and temperature dependence of the segmental and chain relaxation times determined from dielectric spectra and chain relaxation from mechanical spectra; Figure S3: dynamic master curves of the storage and loss moduli for the PM samples PM42.9 and PM74.1 and respective van Gurp-Palmen plot of the data; Figure S4: storage and loss modulus of PM115.9 beyond $T_{\mathrm{g}}$ indicating the breakdown of TTS at $T_{g}$; Figure S5: dielectric normal mode relaxation times and zero shear viscosities for polyisoprene, polyfarnesene, and polymyrcene versus $Z$, the number of entanglements at an isofrictional state; Figure S6: rheodielectrics setup and rheodielectric kit used for measurements (PDF)

Enlarged versions of figures in this article (ZIP)

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## Notes

The authors declare no competing financial interest.

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## - DEDICATION

This article is dedicated to Professor Hans-Wolfgang Spiess on the occasion of his 80th birthday.

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