Supplementary Information for

## Glass Transition Temperature Correlation with Chemical Structure for Conjugated Polymers

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## Supplementary Note 1 <br> Chemical names and sources of $\mathbf{3 2}$ polymers examined in this work

PFTBT: $\operatorname{poly}\left((9,9-d i o c t y l f l u o r e n e)-2,7-d i y l-a l t-[4,7-b i s(t h i o p h e n-5-y l)-2,1,3-b e n z o t h i a d i a z o l e]-2^{\prime}, 2^{\prime \prime}-d i y l\right)$. Synthesized.

PCDTBT: poly[N-9'-heptadecanyl-2,7-carbazole-alt-5,5-(4',7'-di-2-thienyl-2', 1', 3'-benzothiadiazole)]. Synthesized.

PFT6BT: poly-((9,9-dioctylfluorene)-2,7-diyl-alt-[4,7-bis(3-hexylthiophen-5-yl)-2,1,3-benzothiadiazole]-2',2"diyl). Synthesized.

PCT6BT: poly-((9-(9-heptadecanyl)-9H-carbazole)-1,4-diyl-alt-[4,7-bis(3-hexylthiophen-5-yl)-2,1,3-benzothiadiazole]-2',2"-diyl). Synthesized.

PDPT6BT: poly-(4-(2-ethylhexyl)-4H-dithieno[3,2-b:2',3'-d]pyrrole-2,6-diyl-alt-[4,7-bis(3-hexylthiophen-5-yl)-2,1,3-benzothiadiazole]-2',2'-diyl)). Synthesized.

PF8BT: poly(9,9-dioctylfluorene-alt-benzothiadiazole). Purchased from Ossila.
PF8T2: $\operatorname{poly}(9,9$-dioctylfluorene-alt-bithiophene). Purchased from Ossila.

TFB: poly(9,9-dioctylfluorene-co-N-(4-butylphenyl)diphenylamine). Data obtained from Liu et. al. ${ }^{1}$
APFO-Green9: Structure shown in Figure 1. Data obtained from Kroon et. al. ${ }^{2}$

APFO-18: Structure shown in Figure 1. Data obtained from Kroon et. al. ${ }^{2}$
PBTTT-C14 HH: poly[2,5-bis(3-tetradecylthiophen-2-yl)thieno[3,2-b]thiophene] with head-to-head configuration. Synthesized.

PT: poly(3-thiophene-2,5-diyl). Purchased from Sigma Aldrich.

P3BT: poly(3-butylthiophene-2,5-diyl). Purchased from Sigma Aldrich.

P3HT: poly(3-hexylthiophene-2,5-diyl). Purchased from Sigma Aldrich.
P3OT: poly(3-octylthiophene-2,5-diyl). Purchased from Sigma Aldrich.

P3DT: poly(3-decylthiophene-2,5-diyl). Purchased from Sigma Aldrich.
P3DDT: poly(3-dodecylthiophene-2,5-diyl). Purchased from Sigma Aldrich.
PF6: poly(9,9-di-n-hexylfluorenyl-2,7-diyl). Purchased from Lumtec.

PF2/6: poly[9,9-bis-(2-ethylhexyl)-9H-fluorene-2,7-diyl]. Data obtained from Papadopoulos et. al. ${ }^{3}$
PF8: poly(9,9-di-n-octylfluorenyl-2,7-diyl). Purchased from Ossila.
PF12: poly(9,9-di-n-dodecylfluorenyl-2,7-diyl). Purchased from Lumtec.
PffBT4T-2OD: poly[(5,6-difluoro-2,1,3-benzothiadiazol-4,7-diyl)-alt-(3,3'"'-di(2-octyldodecyl)$2,2^{\prime}, 5^{\prime}, 2^{\prime}, 5^{\prime}, 2^{\prime}$ '' - quaterthiophen- $5,5^{\prime \prime \prime}$-diyl)]. Purchased from 1-Material.

PTB7: poly[[4,8-bis[(2-ethylhexyl)oxy]benzo[1,2-b:4,5-b']dithiophene-2,6-diyl][3-fluoro-2-[(2-ethylhexyl)carbonyl]thieno[3,4-b]thiophenediyl]]. Purchased from Solarmer.

P(NDI2OD-T2): poly([N,N'-bis(2-octyldodecyl)naphthalene-1,4,5,8-bis(dicarboximide)-2,6-diyl]-alt-5,5'-(2,2'bithiophene)). Purchased from Polyera.

PII-2T: poly(isoindigo-dithiophene). Synthesized.
PmmpP-4: polyarylene or poly(meta, meta, para-phenylene) with butyloxy side chains. Synthesized.
PmmpP-6: polyarylene or poly(meta, meta, para-phenylene) with hexyloxy side chains. Synthesized.
PmmpP-8: polyarylene or poly(meta, meta, para-phenylene) with octyloxy side chains. Synthesized.
PmmpP-10: polyarylene or poly(meta, meta, para-phenylene) with decyloxy side chains. Synthesized.
M3EH-PPV: poly[2,5-dimethoxy-1,4-phenylene-1,2-ethenylene-2-methoxy-5-(2-ethylhexyloxy)-
1,4-phenylene-1,2-ethenylene]. Data obtained from Steffen et. al. ${ }^{4}$
MDMO-PPV: poly[2-methoxy-5-( $3^{\prime}, 7^{\prime}$-dimethyloctyloxy)-1,4-phenylenevinylene]. Data obtained from Kim et. al. ${ }^{5}$

MEH-PPV: poly[2-methoxy-5-(2-ethylhexyloxy)-1,4-phenylene-1,2-ethenylene]. Data obtained from Kim et. al. ${ }^{5}$

## Supplementary Note 2

## Glass transition measurements of conjugated polymers

The glass transition temperature $\left(T_{\mathrm{g}}\right)$ in this work was measured under a nitrogen environment mostly by oscillatory shear rheometry as shown in Fig. 2 and Supplementary Figures 1-4. Exceptions include the amorphous polymers (PAr's) that show clear glass transition signatures using differential scanning calorimetry (DSC, Supplementary Figure 5), and the unmoldable polymer (PT) where DSC is the only option to probe its $T_{\mathrm{g}}$ (Supplementary Figure 6).
$T_{\mathrm{g}} \mathrm{S}$ can be usually identified as the temperature that shows the local maximum of $G^{\prime \prime}$ and the decrease in $G^{\prime}$ starting from roughly 1 GPa (typical glassy modulus). But, some conjugated polymers exhibit two glass transition temperatures, one for the alkyl side chain and one for the backbone; the side chain $T_{\mathrm{g}}$ is the lower temperature transition because the side chains are more flexible than the backbone. The strength of the glass transition, represented by the peak magnitude of the loss modulus $G^{\prime \prime}$, is not necessarily higher for the backbone $T_{\mathrm{g}}$ than the that of the side chain, especially for highly crystalline conjugated polymers with branched side chains, as shown in Supplementary Figure 4. We speculate that the strength of the glass transition is controlled by the occupied volume of the segmental moiety that participates in the transition process. For conjugated polymers with high crystallinity and branched side chains, the $T_{\mathrm{g}}$ response of the side chain could be amplified because of the larger occupied volume of the branched side chain when compared to that of linear side chains, while the $T_{\mathrm{g}}$ response of the backbone could be diminished because of many backbone segments being fixed on a crystal lattice and not participating in the glass transition.

This behavior is demonstrated by comparing the $T_{\mathrm{g}}$ for PII-2T, PffBT4T-2OD, and P(NDI2OD)-T2, all of which share the same two branched octyl-decyl side chains (2OD) per repeat unit but have drastically different backbone structures. As shown in Supplementary Figure 4, their side chain $T_{\mathrm{g}} \mathrm{s}$ vary between -50 and $-60^{\circ} \mathrm{C}$ and seem more apparent than their backbone $T_{\mathrm{g}} \mathrm{s}$, which are $65^{\circ} \mathrm{C}$ for PII-2T, $74^{\circ} \mathrm{C}$ for P (NDI2OD)-T2 and $28^{\circ} \mathrm{C}$ for PffBT4T-2OD. PTB7, which has shorter branched side chains (ethyl-butyl) than 2OD and thus a lower side chain $T_{\mathrm{g}}$ at $-80^{\circ} \mathrm{C}$, is also added to Supplementary Figure 4 for comparison. The backbone $T_{\mathrm{g}} \mathrm{S}$ of these branched
semicrystalline conjugated polymers are identified by fitting the Gaussian peaks to the temperature dependence of the loss modulus.



Supplementary Figure 1. $\boldsymbol{T}_{\mathrm{g}}$ measurements of the push-pull conjugated polymers. Results shown for a three molecular weights of PCDTBT ( $107^{\circ} \mathrm{C}, 116^{\circ} \mathrm{C}, 119^{\circ} \mathrm{C}$ ), b PFTBT ( $126^{\circ} \mathrm{C}$ ), PFT6BT ( $79^{\circ} \mathrm{C}$ ) and PDPT6BT $\left(90^{\circ} \mathrm{C}\right)$, and $\mathbf{c}$ PF8BT $\left(112^{\circ} \mathrm{C}\right)$ and PF82T $\left(102^{\circ} \mathrm{C}\right)$. Oscillatory frequency of $1 \mathrm{rad} / \mathrm{s}, 5^{\circ} \mathrm{C} / \mathrm{min}$ heating and strain amplitude of 0.001 .


Supplementary Figure 2. $\boldsymbol{T}_{g}$ measurements of polythiophenes. Results shown for a PBTTT-C14 HH ( $5^{\circ} \mathrm{C}$ ) with head-to-head thiophenes, b regioregular P3BT $\left(50^{\circ} \mathrm{C}\right)$, P3OT $\left(-17^{\circ} \mathrm{C}\right)$, P3DT $\left(-27^{\circ} \mathrm{C}\right)$ and P3DDT $\left(-18{ }^{\circ} \mathrm{C}\right)$. Oscillatory frequency of $1 \mathrm{rad} / \mathrm{s}, 5^{\circ} \mathrm{C} / \mathrm{min}$ heating and strain amplitude of 0.001 .


Supplementary Figure 3. ${\text { Tg measurements of polyfluorenes, namely PF6 }\left(101{ }^{\circ} \mathrm{C}\right) \text {, } \mathrm{PF} 8\left(71{ }^{\circ} \mathrm{C}\right) \text { and PF12 }}^{\circ}$ $\left(16{ }^{\circ} \mathrm{C}\right)$ with hexyl, octyl, and dodecyl side chains, respectively. Oscillatory frequency of $1 \mathrm{rad} / \mathrm{s}, 5^{\circ} \mathrm{C} / \mathrm{min}$ heating and strain amplitude of 0.001 .








Supplementary Figure 4. Rheology identifies $\boldsymbol{T}_{\mathbf{g}} \mathbf{s}$ of conjugated polymers. a $T_{\mathrm{g}}$ measurements by rheology for semicrystalline conjugated polymers with branched alkyl side chains, including PII-2T, PffBT4T-2OD, $\mathrm{P}\left(\right.$ NDI2OD-T2) and PTB7, conducted at a heating rate of $5^{\circ} \mathrm{C} / \mathrm{min}$, an oscillatory frequency of $1 \mathrm{rad} / \mathrm{s}$ and a strain amplitude of 0.001 . The side chain $T_{\mathrm{g}}$ is more apparent and at a lower temperature than the backbone $T_{\mathrm{g}}$. The data for PTB7 stop at $100^{\circ} \mathrm{C}$, above which the glue (polycyanoacrylate, only used for PTB7) between the plate and sample softens and the data no longer represent the modulus of the sample. The extraction of backbone $T_{\mathrm{g}} \mathrm{s}$ of $\mathbf{b}$ PffBT4T-2OD, $\mathbf{c}$ PII-2T, d P(NDI2OD-T2), e PTB7 are shown by fitting the temperature dependence of the loss modulus with Gaussian peaks. The peak temperature that corresponds to each Gaussian fit is shown in the legend, and the backbone $T_{\mathrm{g}} \mathrm{S}$ are marked in bold. Chemical structures of these low bandgap polymers with branched side chains are also shown.


Supplementary Figure 5. Second DSC heating scans of PmmpP-4, PmmpP-6, PmmpP-8, PmmpP-10 at $10{ }^{\circ} \mathbf{C} / \mathbf{m i n} . T_{\mathrm{g}}$ are identified as the midpoints of the step changes in heat flow: $164{ }^{\circ} \mathrm{C}$ for $\mathrm{PmmpP}-4,117{ }^{\circ} \mathrm{C}$ for PmmpP-6, $87{ }^{\circ} \mathrm{C}$ for $\mathrm{P} m m p \mathrm{P}-8,5{ }^{\circ} \mathrm{C}$ for $\mathrm{P} m m p \mathrm{P}-10$.


Supplementary Figure 6. Second DSC heating scan of the unsubstituted polythiophene (PT) powder at $10^{\circ} \mathbf{C} / \mathbf{m i n}$. $T_{\mathrm{g}}$ of PT is identified at $215^{\circ} \mathrm{C}$ where a small step change in heat flow is apparent (more clearly seen in the derivative).

## Supplementary Note 3

Summary of $T_{g}$ s and other parameters used in this work
Supplementary Table 1 summarizes glass transition temperatures used in Figure 3 and Figure 4 of the main text. Effective mobility values ( $\zeta$ ) and side chain mass fraction $(w)$ are calculated for all studied polymers based on the repeat unit structure. The mass density $(\rho)$ is estimated by conforming the sample into a cylinder between two ( $3 \pm 0.1$ )-mm parallel plates, while the density of the unsubstituted polythiophene (PT) is calculated to be $1.55 \mathrm{~g} / \mathrm{ml}$ based on the crystal unit cell ${ }^{6}$. The persistence length $\left(l_{\mathrm{p}}\right)$ is estimated by the Freely Rotating Model $^{7}$ when experimental values from small-angle neutron scattering (SANS) ${ }^{8}$ or static light scattering (SLS) ${ }^{9,10}$ are not available in the literature. Packing length is calculated from the estimated $l_{\mathrm{p}}$ and $\rho$ according to Supplementary Equation (1) and summarized in Supplementary Table 1.

Supplementary Table 1. Summary of the experimentally measured backbone glass transition temperature ( $T_{\mathrm{g}}$ ), predicted $T_{\mathrm{g}}$ by Equation (4), determination method, effective mobility value ( $\zeta$ ), side chain mass fraction ( $w$ ), mass density at $298 \mathrm{~K}(\rho)$, persistence length $\left(l_{p}\right)$, number of Kuhn monomers ( $N_{k}$ ), number average molecular weight $\left(M_{n}\right)$, and packing length $(p)$ of conjugated polymers examined in this work.

| Group | Polymer | $\begin{gathered} M_{\mathrm{n}} \\ {[\mathrm{kDa}]} \end{gathered}$ | Method | $\begin{gathered} \text { Exp. } \\ T_{g} \\ {\left[{ }^{\circ} \mathrm{C}\right]} \end{gathered}$ | $\begin{gathered} \text { Pred. } \\ \boldsymbol{T}_{\mathrm{g}} \\ {\left[{ }^{\circ} \mathrm{C}\right]} \end{gathered}$ | $\zeta[-]$ | $w[-]$ | $\begin{gathered} \rho \\ {[\mathrm{g} / \mathrm{ml}]} \end{gathered}$ | $\begin{gathered} l_{\mathrm{p}} \\ {[\mathrm{~nm}]} \end{gathered}$ | $\begin{aligned} & N_{\mathrm{k}} \\ & {[-]} \end{aligned}$ | $p$ [ ${ }^{\text {d }}$ ] |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | P3HT RR | 14.5 * | rheo | $1^{*}$ | 18 | 0.873 | 0.515 | 1.1 | 2.7 | 6.3 | 1.17 |
|  |  | 15.3* | rheo | 3* | 18 | 0.873 | 0.515 | 1.1 | 2.7 | 6.6 | 1.17 |
|  |  | 24.2* | rheo | 10* | 18 | 0.873 | 0.515 | 1.1 | 2.7 | 11 | 1.17 |
|  |  | 21.5* | rheo | $10^{*}$ | 18 | 0.873 | 0.515 | 1.1 | 2.7 | 9.3 | 1.17 |
|  |  | 27.7* | rheo | $11^{*}$ | 18 | 0.873 | 0.515 | 1.1 | 2.7 | 12 | 1.17 |
|  |  | 36.6* | rheo | $14^{*}$ | 18 | 0.873 | 0.515 | 1.1 | 2.7 | 16 | 1.17 |
|  | P3HT RRa | 41.7* | rheo | 4* | 18 | 0.873 | 0.515 | 1.1 | 2.7 | 18 | 1.17 |
|  |  | 44.9* | rheo | $6^{*}$ | 18 | 0.873 | 0.515 | 1.1 | 2.7 | 20 | 1.17 |
|  | P3DDT RR | 44.7 | rheo | -18 | -32 | 0.918 | 0.670 | 0.99 | 2.7 | 13 | 1.96 |
|  | P3OT RR | 22.6 | rheo | -17 | -4 | 0.892 | 0.580 | 1.03 | 2.7 | 8.4 | 1.46 |
|  | P3BT RR | 35.0 | rheo | 50 | 49 | 0.844 | 0.410 | 1.15 | 2.7 | 18 | 0.930 |
|  | P3DDT RRa | 46.4 | rheo | -30 | -32 | 0.918 | 0.670 | 0.99 | 2.7 | 13 | 1.96 |
|  | P3DT RR | 47.7 | rheo | -27 | -20 | 0.907 | 0.635 | - | 2.7 | 16 | $1.72{ }^{\text {j }}$ |
|  | P3OT RRa | 22.6 | rheo | -19 | -4 | 0.892 | 0.580 | 1.03 | 2.7 | 8.4 | 1.46 |
|  | P3BT RRa | 29.2 | rheo | 45 | 49 | 0.844 | 0.410 | 1.15 | 2.7 | 15 | 0.930 |
|  | $\begin{gathered} \hline \text { PBTTT-C14 } \\ \text { HH } \end{gathered}$ | 16.8 | rheo | 5 | -8 | 0.896 | 0.560 | 1.05 | 4.1 | 4.1 | 0.997 |
|  | PffBT4T-2OD | 12.9 | rheo | 28 | 11 | 0.879 | 0.541 | - | 3.7 | 3.7 | $1.04{ }^{\text {j }}$ |
|  | PTB7 | 19.8 | rheo | 40 | 27 | 0.864 | 0.549 | - | 8.7 | 1.9 | $0.562^{\mathrm{j}}$ |
|  | PDPT6BT | 3.5 | rheo | 90 | 76 | 0.820 | 0.374 | 1.25 | 4.2 | 1.1 | 0.622 |
|  | PT | - | DSC | 215 | 186 | 0.720 | 0.000 | $1.55{ }^{\text {k }}$ | 2.7 | - | 0.410 |


| 2 | PFTBT | 16.0* | rheo | 132* | 121 | 0.779 | 0.329 | 1.35 | 5.5 | 4.4 | 0.369 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 11.7* | rheo | $126 *$ | 121 | 0.779 | 0.329 | 1.35 | 5.5 | 3.2 | 0.369 |
|  |  | 9.3 * | rheo | 122* | 121 | 0.779 | 0.329 | 1.35 | 5.5 | 2.6 | 0.369 |
|  | PCDTBT | $6.7{ }^{\wedge}$ | rheo | 107 | 125 | 0.776 | 0.340 | 1.30 | 5.9 | 1.6 | 0.381 |
|  |  | $7.6^{\wedge}$ | rheo | 116 | 125 | 0.776 | 0.340 | 1.30 | 5.9 | 1.9 | 0.381 |
|  |  | $15^{\wedge}$ | rheo | 119 | 125 | 0.776 | 0.340 | 1.30 | 5.9 | 3.7 | 0.381 |
|  | PCT6BT | 21.6 | rheo | 74 | 76 | 0.820 | 0.471 | 1.15 | 5.9 | 4.3 | 0.535 |
|  | PFT6BT | 34.7 | rheo | 79 | 72 | 0.823 | 0.464 | 1.15 | 5.5 | 7.7 | 0.540 |
|  | PF6 | 44 | rheo | 101 | 89 | 0.808 | 0.512 | 1.10 | $7.0{ }^{\text {g }}$ | 8.2 | 0.413 |
|  | PF8 | 31 | rheo | 71 | 60 | 0.834 | 0.582 | 1.03 | $7.0{ }^{\text {g }}$ | 4.9 | 0.516 |
|  | PF2/6 | $98^{\text {a }}$ | DSC | $59^{\text {a }}$ | 60 | 0.834 | 0.582 | - | $7.0^{\mathrm{g}}$ | 16 | $0.516^{\text {j }}$ |
|  | PF12 | 33.5 | rheo | 16 | 20 | 0.870 | 0.676 | 0.99 | $7.0^{\text {g }}$ | 4.1 | 0.692 |
|  | PF82T | 21.4 | rheo | 102 | 92 | 0.805 | 0.409 | 1.20 | 4.9 | 6.5 | 0.477 |
|  | PF8BT | 88 | rheo | 112 | 103 | 0.795 | 0.433 | 1.15 | $10^{\text {h }}$ | 11 | 0.294 |
|  | РmmpP-4 | 27.7 | DSC | 164 | 161 | 0.743 | 0.306 | - | 0.9 | 45 | $3.03{ }^{\text {j }}$ |
|  | РтmрР-6 | 67.0 | DSC | 117 | 125 | 0.775 | 0.397 | - | 0.9 | 94 | $3.49^{\text {j }}$ |
|  | Ртmp $\mathrm{P}-8$ | 46.5 | DSC | 87 | 98 | 0.800 | 0.467 | - | 0.9 | 58 | $3.95{ }^{\text {j }}$ |
|  | Pmmp-10 | 48.7 | DSC | 58 | 76 | 0.820 | 0.567 | 0.99 | 0.9 | 54 | 4.45 |
|  | P (NDI2OD-T2) | 109 | rheo | 74 | 47 | 0.846 | 0.568 | - | 3.4 | 25 | $1.54{ }^{\text {j }}$ |
|  | PII-2T | $12.1{ }^{\text {b }}$ | rheo | 65 | 47 | 0.846 | 0.577 | - | 6.2 | 1.9 | $0.684^{\text {j }}$ |
|  | M3EH-PPV | $>20^{\text {c }}$ | DSC | $113{ }^{\text {c }}$ | 105 | 0.794 | 0.526 | - | $6.0^{\text {i }}$ | 5.2 | $0.441^{\text {j }}$ |
|  | MEH-PPV | $45^{\text {d }}$ | DSC | $66^{\text {d }}$ | 63 | 0.832 | 0.615 | - | $6.0^{\text {i }}$ | 9.6 | $0.543^{\text {j }}$ |
|  | MDMO-PPV | $123{ }^{\text {d }}$ | DSC | $50^{\text {d }}$ | 45 | 0.848 | 0.653 | - | $6.0^{\text {i }}$ | 24 | $0.601^{\mathrm{j}}$ |
|  | TFB | $57^{\text {e }}$ | DSC | $140{ }^{\text {e }}$ | 140 | 0.762 | 0.412 | - | 2.4 | 29 | $1.36{ }^{\text {j }}$ |
|  | APFO-18 | $8^{\text {f }}$ | DSC | $142^{\text {f }}$ | 173 | 0.731 | 0.272 | - | 5.5 | 1.8 | $0.603^{\text {j }}$ |
|  | APFO-Green9 | $10^{\text {f }}$ | DSC | $192{ }^{\text {f }}$ | 204 | 0.704 | 0.230 | - | 5.5 | 1.9 | $0.715^{\mathrm{j}}$ |

${ }^{*}: T_{\mathrm{g}} \mathrm{s}$ and $M_{\mathrm{n}}$ determined from our previous work. ${ }^{11}$
${ }^{\wedge}: M_{\mathrm{n}}$ for PCDTBTs determined by GPC in 1,2,4-trichlorobenzene at $150^{\circ} \mathrm{C}$ using universal calibration.
${ }^{\text {a. }} T_{\mathrm{g}}$ and $M_{\mathrm{n}}$ for PF2/6 from Papadopoulos et. al. ${ }^{3}$
${ }^{\text {b }}: M_{\mathrm{n}}$ for PII-2T determined by GPC in 1,2,4-trichlorobenzene at $160^{\circ} \mathrm{C}$ using calibration relative to polystyrene from Zhou et. al. ${ }^{12}$
${ }^{c}: T_{\mathrm{g}}$ and $M_{\mathrm{n}}$ for M3EH-PPV from Steffen et. al. ${ }^{4}$
${ }^{\mathrm{d}}: T_{\mathrm{g}}$ and $M_{\mathrm{n}}$ for MEH-PPV and MDMO-PPV from Kim et. al. ${ }^{5}$
${ }^{\mathrm{e}}: T_{\mathrm{g}}$ and $M_{\mathrm{n}}$ for TFB from Liu et. al. ${ }^{1}$
${ }^{\mathrm{f}}: T_{\mathrm{g}} \mathrm{S}$ and $M_{\mathrm{n}}$ for APFO-18 and APFO-Green9 from Kroon et. al. ${ }^{2}$
$\mathrm{g}: l_{\mathrm{p}}$ of PFs determined by SANS to be $7.0 \mathrm{~nm} .^{8}$
${ }^{\mathrm{h}}$ : $l_{\mathrm{p}}$ of PF8BT determined by SLS to be $10.0 \mathrm{~nm} .{ }^{9}$
${ }^{\mathrm{i}}: l_{\mathrm{p}}$ of PPVs with alkyl side chains determined by SLS to be $6.0 \mathrm{~nm} .{ }^{10}$
${ }^{\mathrm{j}}: p$ is computed by Supplementary Equation (1) assuming density of $1.0 \mathrm{~g} / \mathrm{ml}$.
${ }^{\mathrm{k}}: \rho$ for PT calculated from the crystal unit cell. ${ }^{6}$
All other $T_{\mathrm{g}} \mathrm{s}$ are measured in this work.
All other $l_{\mathrm{p}} \mathrm{s}$ are predicted by freely rotating chain model in this work.
All other $\rho$ s are obtain by measuring the volume using a parallel plate geometry with a well-defined gap for samples of known mass.
All other $M_{\mathrm{n}} \mathrm{S}$ are determined by GPC in chlorobenzene at $40^{\circ} \mathrm{C}$ using a polystyrene-relative calibration.
All $N_{\mathrm{k}} \mathrm{s}$ are determined from the tabulated $M_{\mathrm{n}}$ and $l_{\mathrm{p}}$ and the repeat unit length, $l_{0}$. (i.e., $N_{\mathrm{k}}=M_{\mathrm{n}} /\left(2 l_{\mathrm{p}} M_{0} / l_{0}\right)$ )

## Supplementary Note 4

## Attempt to correlate packing length with $\boldsymbol{T}_{\boldsymbol{g}}$

The packing length $(p)$ depends on monomer volume and chain stiffness, so we attempted to correlate $p$ with the glass transition temperatures of conjugated polymers. The persistence length $\left(l_{\mathrm{p}}\right)$ is used to quantify the chain stiffness as the length of chain over which the chain orientation remains correlated. The Kuhn monomer volume ( $v_{0}$ ) represents the volume of monomers within a Kuhn length and is strongly affected by the alkyl side chain length. The packing length $(p)$ is then defined as the ratio of Kuhn monomer volume $\left(v_{0}\right)$ over the square of the Kuhn length $\left(l_{\mathrm{k}}=2 l_{\mathrm{p}}\right),{ }^{13}$ and can be calculated from $l_{\mathrm{p}}$, the molar mass of repeat unit $\left(M_{0}\right)$, the mass density $(\rho)$ and the repeat unit length $\left(l_{0}\right)$ using

$$
\begin{equation*}
p=\frac{v_{0}}{\left(2 l_{\mathrm{p}}\right)^{2}}=\frac{M_{0}}{2 \rho l_{0} l_{\mathrm{p}}} \tag{1}
\end{equation*}
$$

Experimentally measured $l_{\mathrm{p}} \mathrm{s}$ are available for several conjugated polymers in the literature from either static light scattering (SLS) or small angle neutron scattering (SANS), such as 2.8 nm for $\mathrm{P}^{2} \mathrm{HT}^{14,15}, 7.0 \mathrm{~nm}$ for PF-EH ${ }^{8}, 10.0 \mathrm{~nm}$ for $\mathrm{PF}^{2} \mathrm{BT}^{9}$, and 6.0 nm for PPV with alkyl side chains ${ }^{10}$. Alternatively, we can predict the persistence length using the freely rotating chain (FRC) model. ${ }^{7}$ This model is validated by the close match of the predicted $l_{\mathrm{p}}$ for P3HT ( 2.7 nm ) versus results by SANS $(3.0 \mathrm{~nm})^{14}$. This generalized freely rotating model ${ }^{7}$ handles different bond lengths and angles within the repeat unit. Specifically, by first constructing the repeat unit in Avogadro, the lengths of rigid segments and deflection angles are measured after minimizing the energy of the molecule using a force field (MMFF94s) and the steepest descent algorithm. ${ }^{16}$ Then, by allowing each rigid segment to freely rotate about its deflection angle, the tangent-tangent correlation as a function of the number of repeat units is computed by numerically averaging many different possible conformations ( 50,000 in this case). $l_{\mathrm{p}}$ (which is $l_{0} N_{\mathrm{p}}$ ) is then the characteristic length of this exponentially-decaying tangent-tangent correlation function:

$$
\begin{equation*}
\left\langle v_{0} \cdot v_{\mathrm{n}}\right\rangle=\exp \left(-\frac{n}{N_{\mathrm{p}}}\right) \tag{2}
\end{equation*}
$$

where $v_{\mathrm{o}}$ and $v_{\mathrm{n}}$ are backbone tangents, $n$ is the number of repeat units, and $N_{\mathrm{p}}$ is the number of repeat units in a persistence length. Examples of the tangent-tangent correlation function for PBTTT-C14 and PFTBT are shown in Supplementary Figure 7.


Supplementary Figure 7. Extracting the persistence length ( $l_{\mathrm{p}}=N_{\mathrm{p}} \times l_{0}$ ) from the exponentially decaying tangent-tangent correlation obtained from the freely rotating chain model. Results for a PBTTT-C14 ( $l_{\mathrm{p}}=$ $2.98 \times 1.36 \mathrm{~nm}=4.1 \mathrm{~nm})$ and $\mathbf{b} \operatorname{PFTBT}\left(l_{\mathrm{p}}=2.65 \times 2.08 \mathrm{~nm}=5.5 \mathrm{~nm}\right)$.

Using the $l_{\mathrm{p}}$ (obtained by either experiment or FRC ) and the estimated mass density, the packing length for conjugated polymers is calculated according to Supplementary Equation (1) and summarized in Supplementary Table 1. Although the correlation between $T_{\mathrm{g}}$ and the packing length $(p)$ works well for a range of relatively stiff conjugated polymers (e.g., polythiophenes, polyfluorenes, and push-pull polymers) in Supplementary Figure 8, it completely fails to describe polyarylenes (PAr) and TFB, both of which have much smaller persistence lengths due to their kinked backbone structures. As for P(NDI2OD-T2), its Kuhn monomer volume might scale differently with the persistence length, due to its large two-dimensional naphthalene-carboximide unit.


Supplementary Figure 8. Correlation between the packing length ( $p$ ) and the glass transition temperature ( $\boldsymbol{T}_{\mathrm{g}}$ ) on log-log scale for conjugated polymers with alkyl side chains. Outliers are polyarylenes (PAr's), TFB and P (NDI2OD-T2). The solid curve is a power law fit through most of the conjugated polymers.

## Supplementary Note 5

The Strength of Correlation between $T_{g}$ and Effective Mobility Value
As discussed in the main text, there is only one adjustable parameter in our model. This parameter determines the effective mobility of the repeat unit, namely the relative atomic mobility between a conjugated atom and a non-conjugated atom. The correlation between the glass transition temperature ( $T_{\mathrm{g}}$ ) and the effective mobility value $(\zeta)$ is the strongest (i.e. $R^{2}=0.956$ in Fig. 4a) when the atomic mobility value in a thiophene ring follows $1.2 a=0.72$ (i.e., $a=0.6$ ), or equivalently the mobility per ring is $0.72 \times 5=3.6$. As shown in Supplementary Figure 9, the strength of this correlation decreases as $a$ deviates from 0.6 and eventually becomes poor (i.e. $R^{2}<0.91$ ) for $a$ greater than 0.68 or less than 0.45 .


Supplementary Figure 9 . The strength of correlation represented by the coefficient of determination ( $\boldsymbol{R}^{\mathbf{2}}$ ) between $T_{\mathrm{g}}$ and $\zeta$ depends on $\boldsymbol{a}$. The strongest correlation is achieved when the mobility per ring is 3.6 or equivalently $a=0.6$, while the correlation becomes poor if atoms in a conjugated ring are assigned to be too immobile $(a<0.45)$ or too mobile $(a>0.68)$ relative to the atoms on the side chain.

## Supplementary Note 6

Polymers with Aromatic Groups on Side Chains
Currently, the general correlation between $T_{\mathrm{g}}$ and $\zeta$ is established using conjugated polymers with alkyl side chains. But, for polymers with a phenyl ring attached to the free end of a side chain, a clear deviation from the correlation is expected due to the different atomic mobilities than that of pure alkyl side chains. Specifically, as shown in Supplementary Figure 10a, the values of $\zeta$ for both polystyrene (PS) and poly[2-methoxy-5-(2'-phenylethoxy)-1,4-phenylenevinylene] (MPE-PPV) are underestimated based on the original assignment of atomic mobility in Table 2, since a phenyl ring on a side chain is in fact a lot more mobile than that on a backbone. Increasing the atomic mobility value for an atom in a phenyl ring ( $\zeta_{\text {phenyl, side chain }}$ ) from 0.60 to 0.72 , both PS and MDE-PPV agree with the correlation again in Supplementary Figure 10b. Note that the $T_{\mathrm{g}}$ of PS is $100^{\circ} \mathrm{C}^{17}$, while $T_{\mathrm{g}}$ of MPE-PPV is $111^{\circ} \mathrm{C}^{18}$.


PS



MPE-PPV


Supplementary Figure 10. Incorporating polymers with aromatic groups on the side chain in the model. a. Data for MPE-PPV and PS lie far below the correlation based on the original assignment of the atomic mobility values in Table 2. b Data for MPE-PPV and PS agree with the correlation after increasing the atomic mobility values in phenyl rings on side chains from 0.60 to 0.72 . Chemical structures of PS and MPE-PPV are also shown.

## Supplementary Note 7

## Molecular weight characterization

As shown in Supplementary Table 1, the $M_{\mathrm{n}} \mathrm{S}$ were determined directly by the gel permeation chromatography (GPC) relative to polystyrene standards for the following samples, P3OT RR, P3BT RR, P3DDT RRa, P3DT RR, P3OT RRa, P3BT RRa, PBTTT-C14 HH, PffBT4T-2OD, PTB7, PDPT6BT, PCT6BT, PFT6BT, PF6, PF8, PF12, PF82T, PF8BT, PmmpP-4, PmmpP-6, PmmpP-8, PmmpP-10, and P(NDI2OD-T2). GPC was run on an Agilent Technologies 1260 Infinity Series GPC/SEC. Samples were characterized with a $0.50 \mathrm{ml} / \mathrm{min}$ flow rate at $40{ }^{\circ} \mathrm{C}$ in chlorobenzene. Relative calibration was done using polystyrene standards from Agilent Technologies that range from 364.00 kDa to 0.37 kDa . Most samples were prepared at a concentration of 1.00 $\mathrm{mg} / \mathrm{ml}$, except for PffBT4T-2OD, PDPT6BT, and PF6 ( $0.50 \mathrm{mg} / \mathrm{ml}$ ), P3BT RR ( $0.25 \mathrm{mg} / \mathrm{ml}$ ), and P(NDI2OD-T2) $(0.33 \mathrm{mg} / \mathrm{ml})$. For other samples in Supplementary Table 1, the $M_{\mathrm{n}}$ s were either taken directly from the cited literatures or determined by other methods, such as ${ }^{1} \mathrm{H}-\mathrm{NMR}$, SLS and GPC using universal calibration.

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