## Quiz 9 Polymer Properties March 8, 2017

- 1) Through modification of the Arrhenius equation  $\eta = \eta_0 \exp\left(\frac{-E_a}{kT}\right)$  using the Vogel temperature,  $T_V$  and the idea that  $E_a$  is a free energy rather than an enthalpy,  $E_a = \Delta H T\Delta S$ , show that it is possible to obtain the WLF expression,
  - $\eta = \eta_0 \exp\left(\frac{-C_1(T T_0)}{C_2 + (T T_0)}\right)$ . Do this by finding expressions for  $\Delta H$ ,  $\Delta S$  and  $T_v$  in terms

of  $C_1$ ,  $C_2$  and  $T_0$ .

- 2) Explain what the Vogel temperature is and, using a cartoon of circles in flow, explain to what  $\Delta H$  and  $\Delta S$  correspond.
- 3) The hydrodynamic radius corresponds to something like a harmonic mean while the radius of gyration corresponds to a second order moment, a type of arithmetic mean. Explain why this might be the case. Where is the harmonic mean usually used? Which size is larger for an expanded coil, R<sub>H</sub> or R<sub>g</sub>? What about for a sphere?
- 4) Starting with the power series expression for intrinsic viscosity,

$$\eta = \eta_0 \left( 1 + c \left[ \eta \right] + k_1 c^2 \left[ \eta \right]^2 + k_2 c^3 \left[ \eta \right]^3 + \dots + k_{n-1} c^n \left[ \eta \right]^n \right)$$

Explain the origin of the Kraemer equation,

$$\frac{\ln(\eta_r)}{c} = [\eta] + k_1 [\eta]^2 c$$