

# Fiber Composite Theory for Modeling Oriented Films

## Solutions

- 1.)
  - a.) the fiber structures appear to have a large aspect ratio (via microscopy techniques)
  - b.) entanglements between fibers prevent slippage between the fiber and matrix, resulting in an efficient transfer of stress from the matrix to the fiber
  - c.) the system is well behaved, meaning that the dynamics of fiber formation is uniform throughout the film.
  
- 2.)
  - a.) low molecular weight polymers do not produce crystalline regions that when oriented produce fibers with large aspect ratios
  - b.) incompatibility between the matrix and the fiber results in slippage between the phases, resulting in an inefficient transfer of stress to the fiber
  - c.) a system (say a blend) containing two different polymers that form different types of fibers.
  
- 3.) Slippage between the fiber and matrix could result from poor adhesion between the phases. To account for this, a factor relating the efficiency of stress transfer between the matrix and fiber can be included. The modified infinitely long fiber composite theory model would then be:
$$E = \sum E_f \phi_f + E_m \phi_m$$
where  $\sum$  is an efficiency factor that tends towards  $\sum = 1$  when there is perfect adhesion between the matrix and the fiber.
  
- 4.) Increasing the drawing temperature increases the maximum attainable draw ratio
  
- 5.) Changing the draw ratio results in an exponential increase in the calculated volume fraction of fibers present in the oriented film. This results in a linear increase in machine direction modulus and tensile strength with respect to  $\phi_f$  and a linear increase in transverse direction modulus with respect to  $1/\phi_f$ . The machine direction break strain quickly goes to a very low value at moderate  $\phi_f$ , meaning there is minimal yield in the film. The yield strain and break strain begin to converge and the stress/strain curve becomes more "Hookean"